



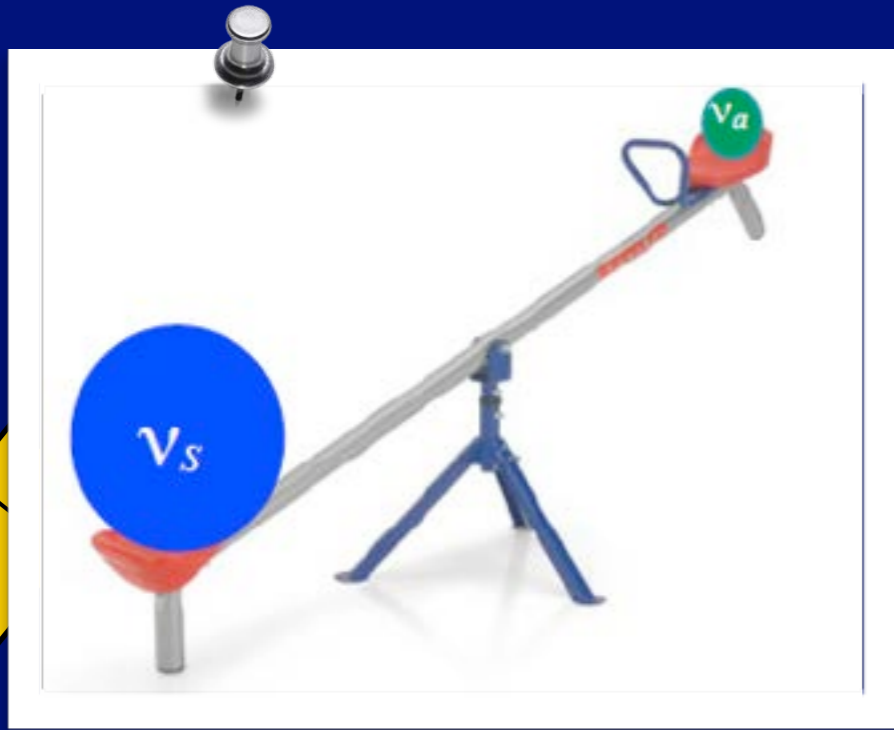
50th Rencontres de Moriond EW 2015

14-21 March 2015

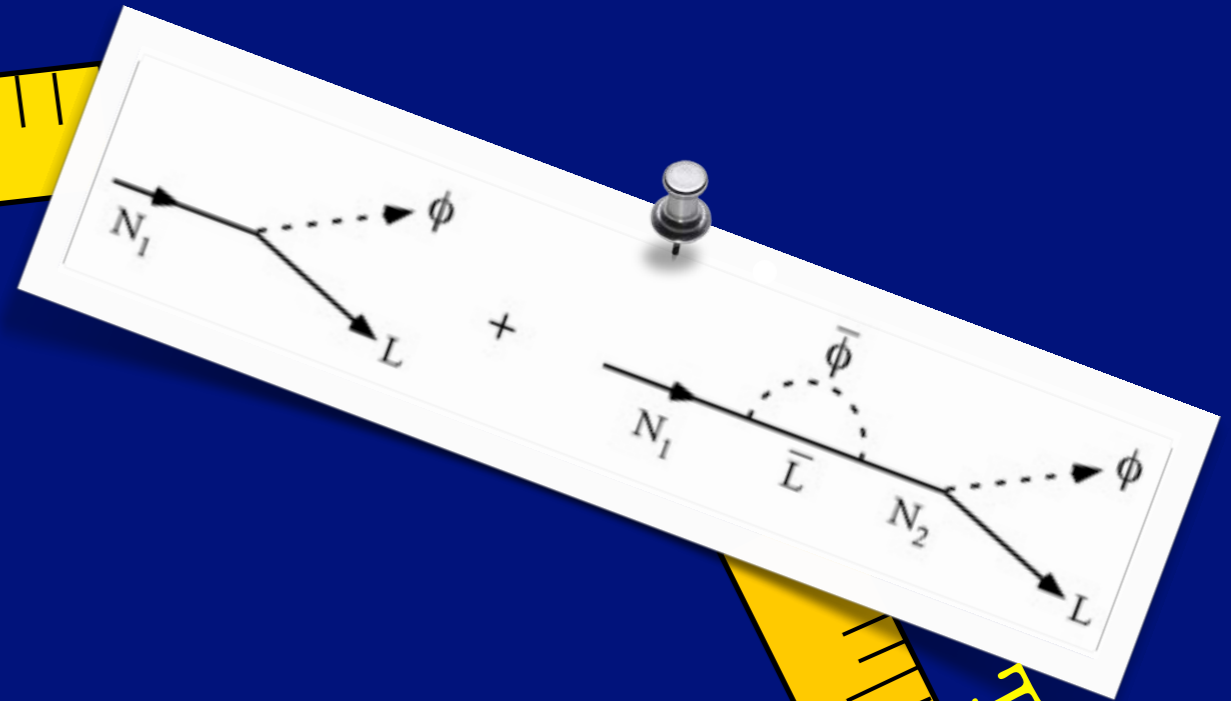
Light sterile ν limits from cosmology

Ninetta Saviano
IPPP, Durham University

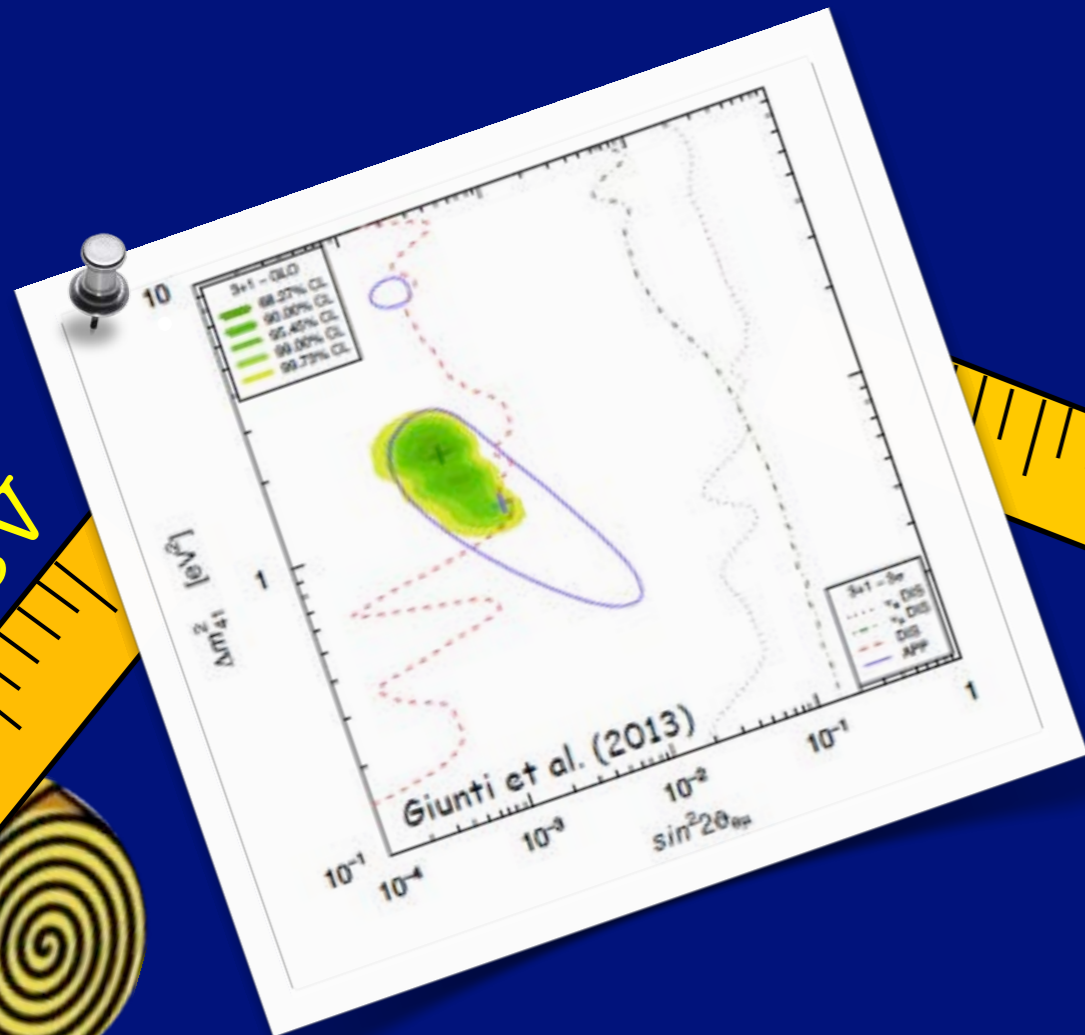
Sterile Neutrinos



M_{GUT}

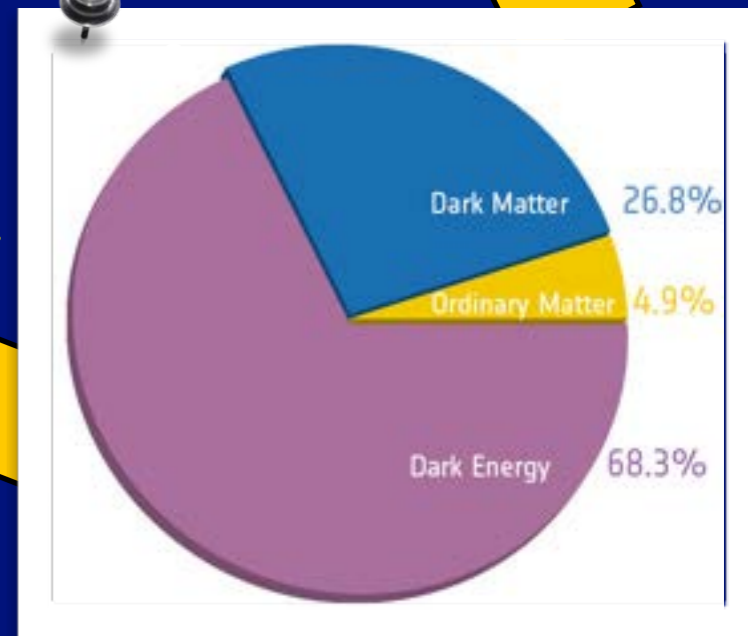


TeV



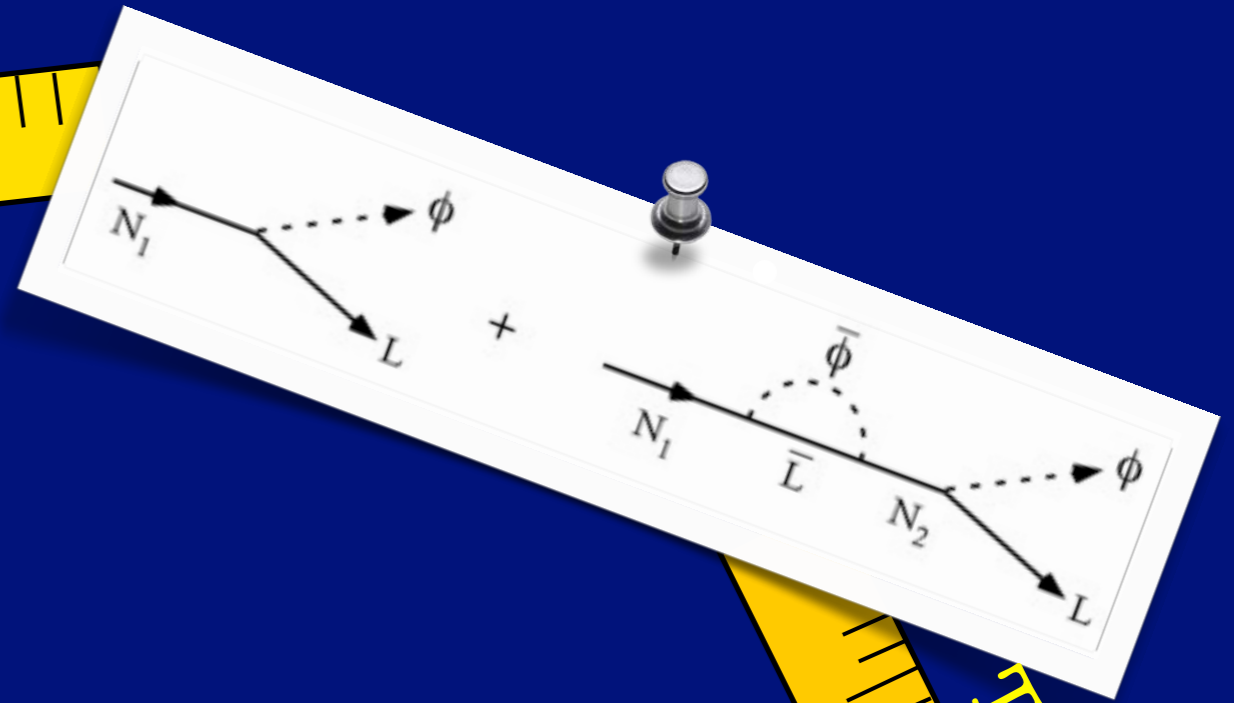
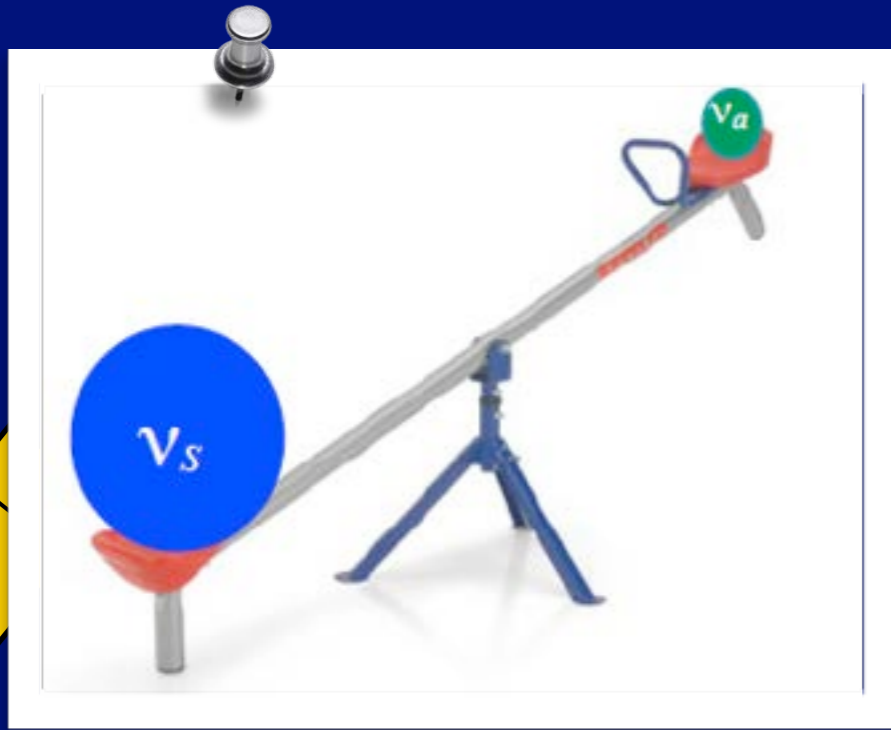
eV

keV

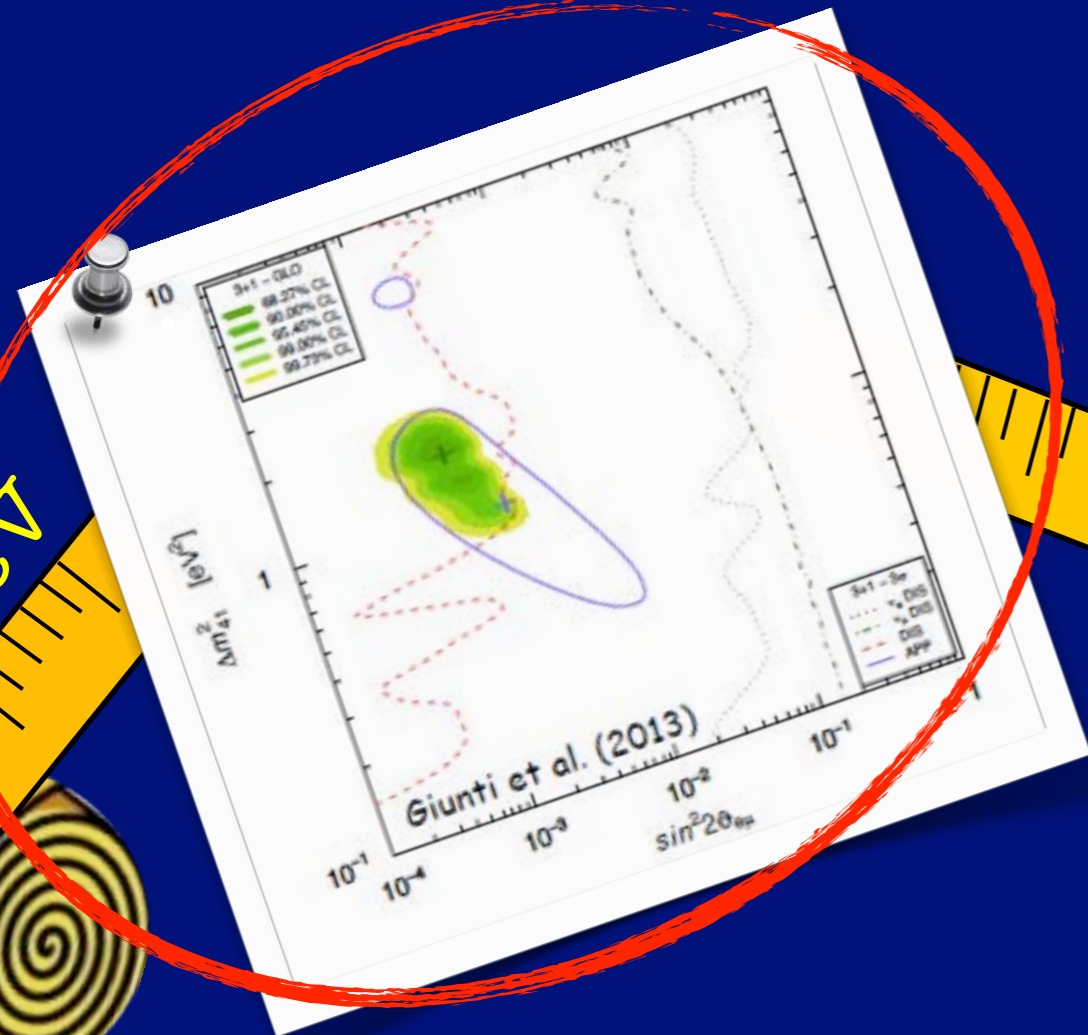


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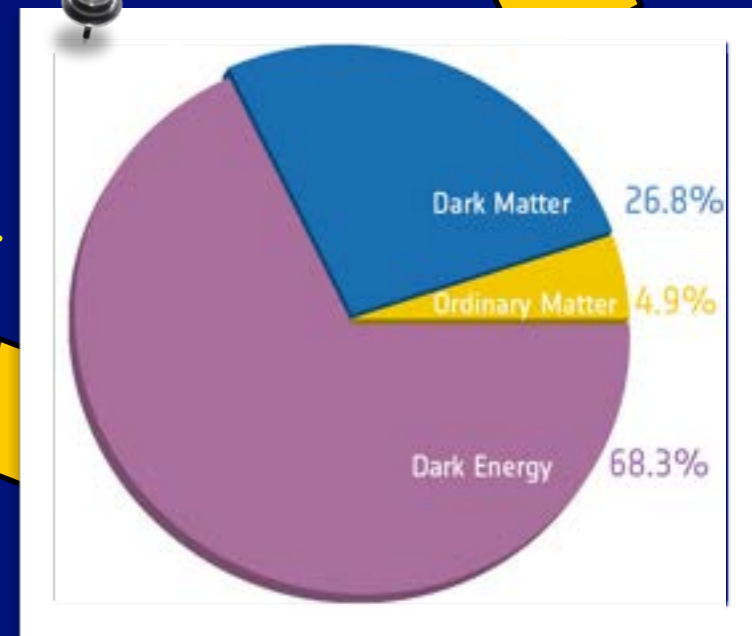


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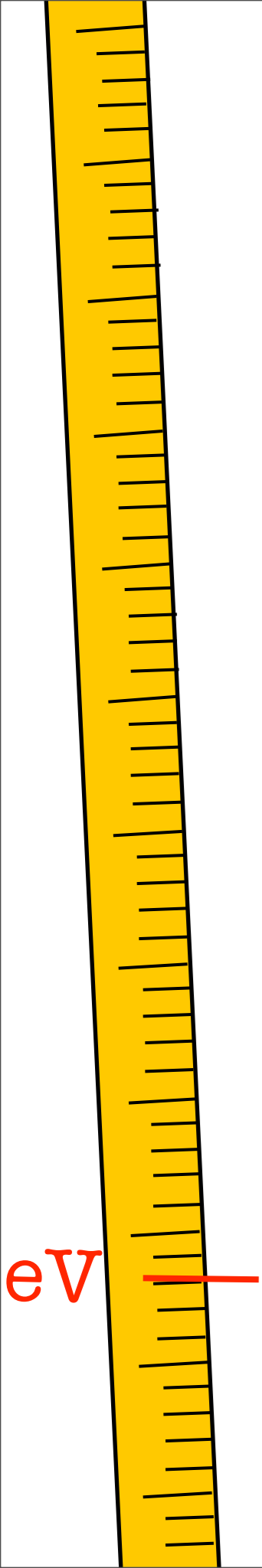


eV

keV



eV Sterile Neutrino

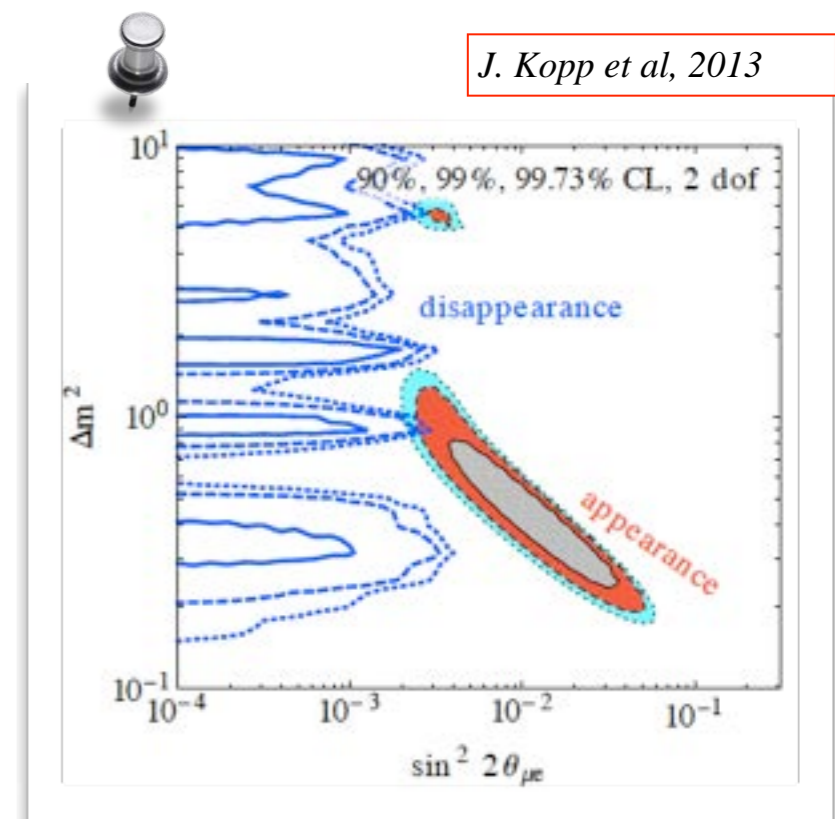
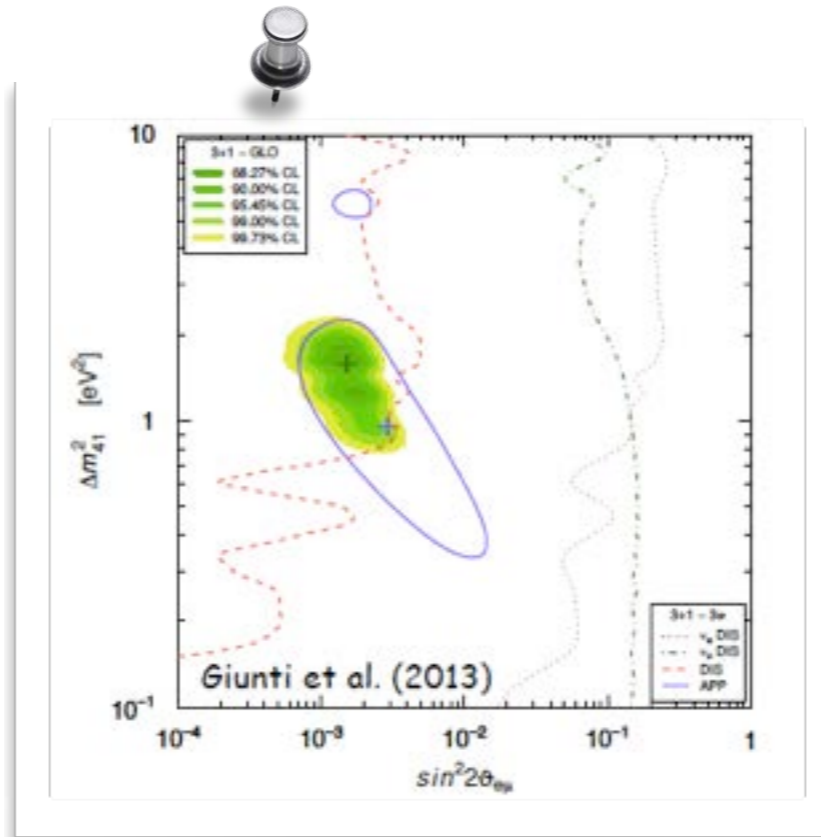


eV Sterile Neutrino

The investigation on Light Sterile Neutrinos has been stimulated by the presence of anomalous results from neutrino oscillation experiments

-  LNSD
-  MiniBooNE
-  Gallium
-  Reactor

see
White paper, Abazajian et al., 2012,
Palazzo, 2013



3+1, 3+2 schemes

(...sometimes in tension among themselves....)

eV

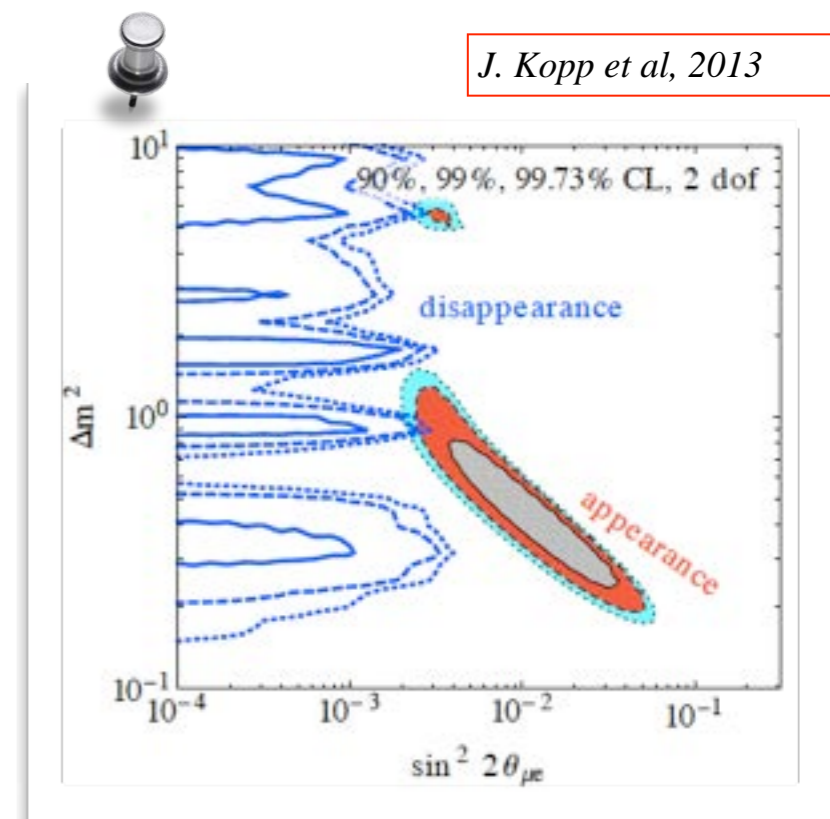
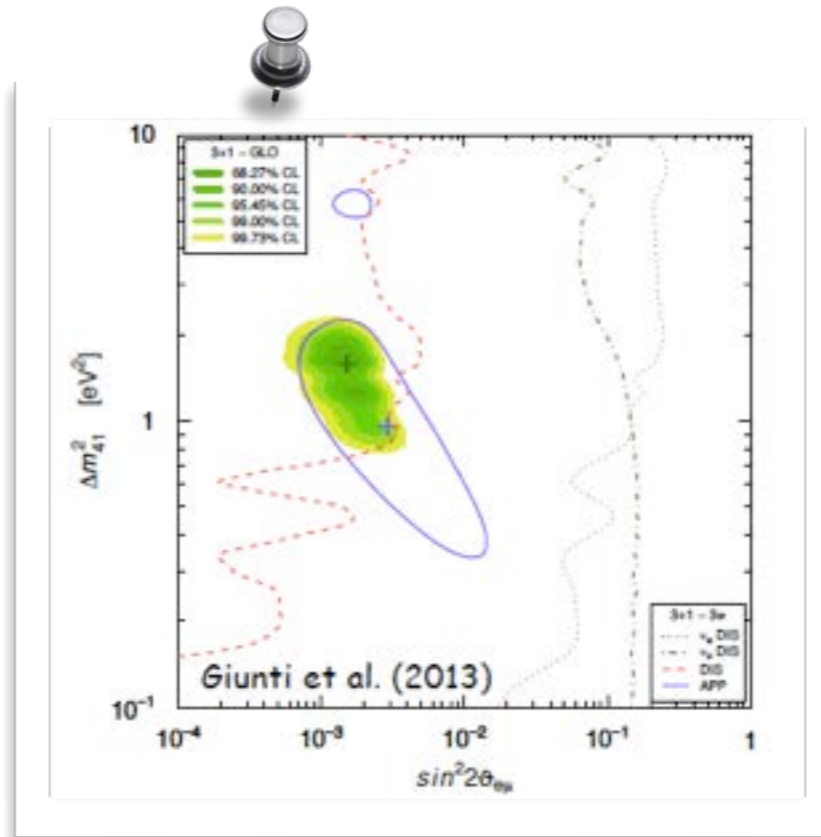
Interpretation: **1** (or more) *sterile neutrino* with $\Delta m^2 \sim O(eV^2)$ and $\theta_s \sim O(\theta_{13})$

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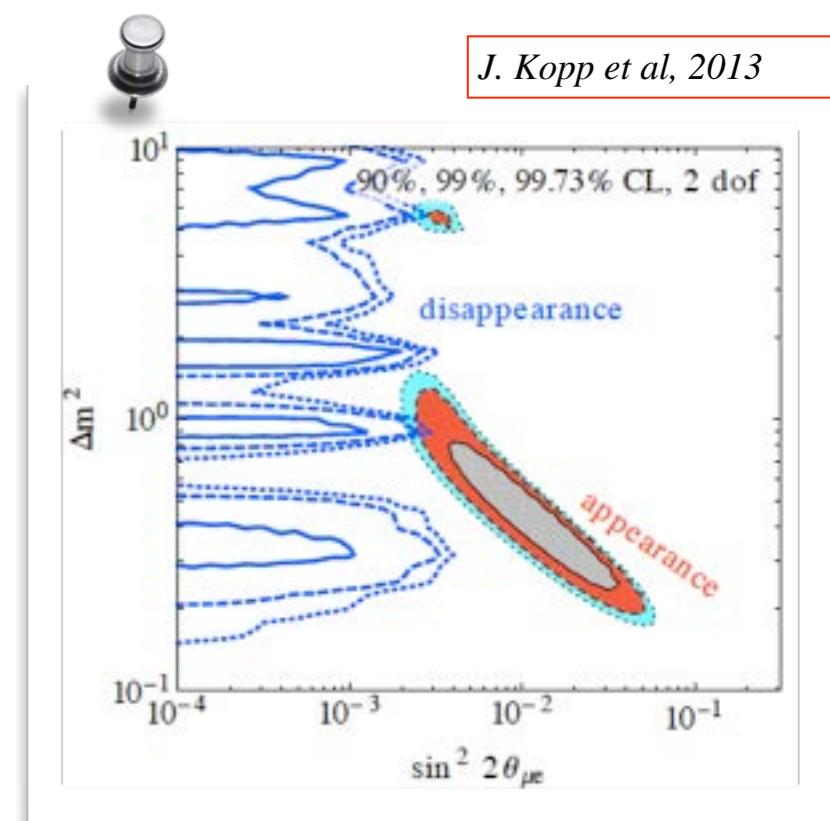
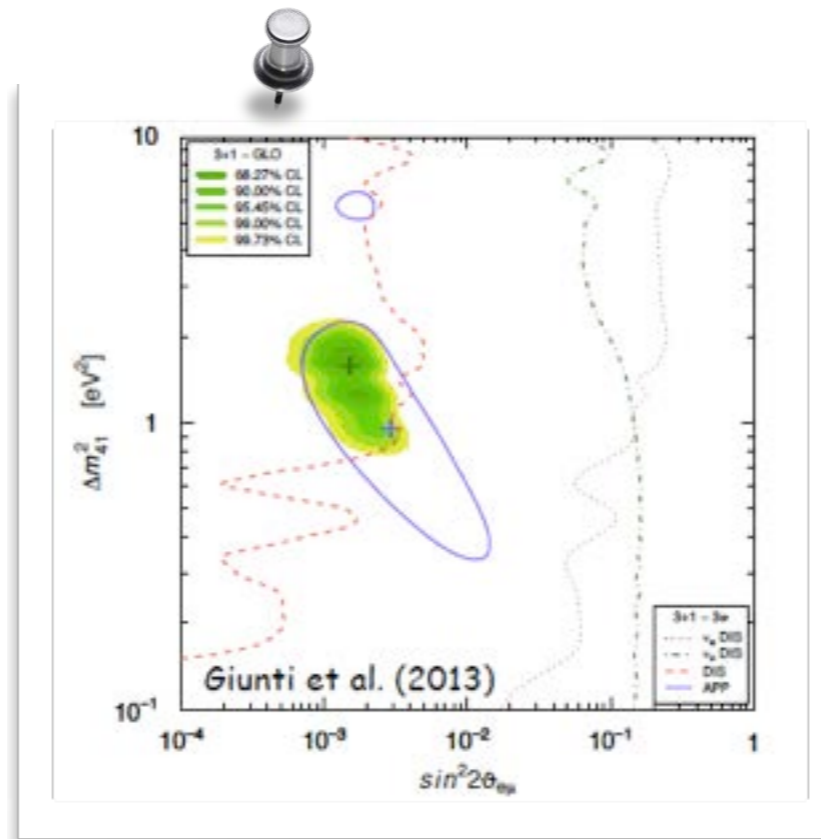
Are eV ν_s compatible with cosmology?

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eV

Interpretation: **1** (or more) *sterile neutrino* with $\Delta m^2 \sim O$ (eV²) and $\theta_s \sim O$ (θ_{13})

Are eV ν_s compatible with cosmology?

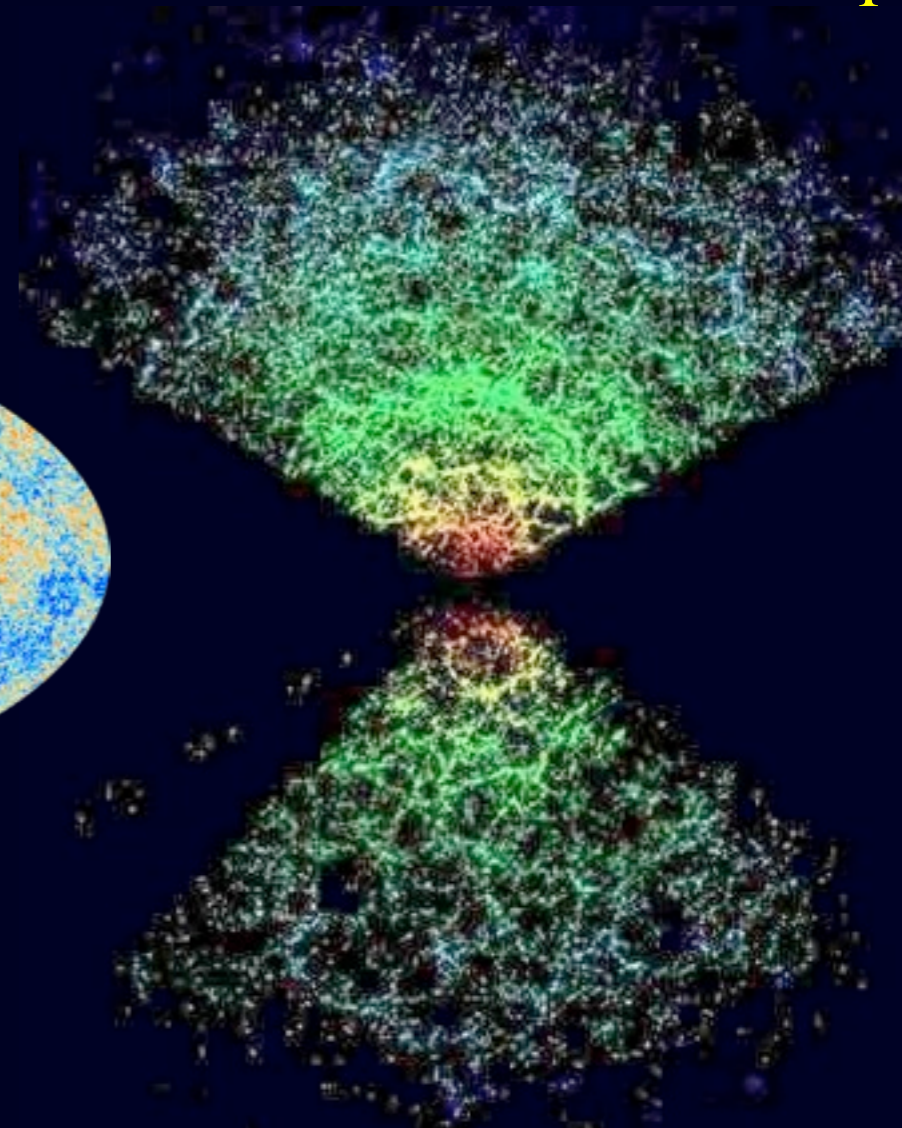
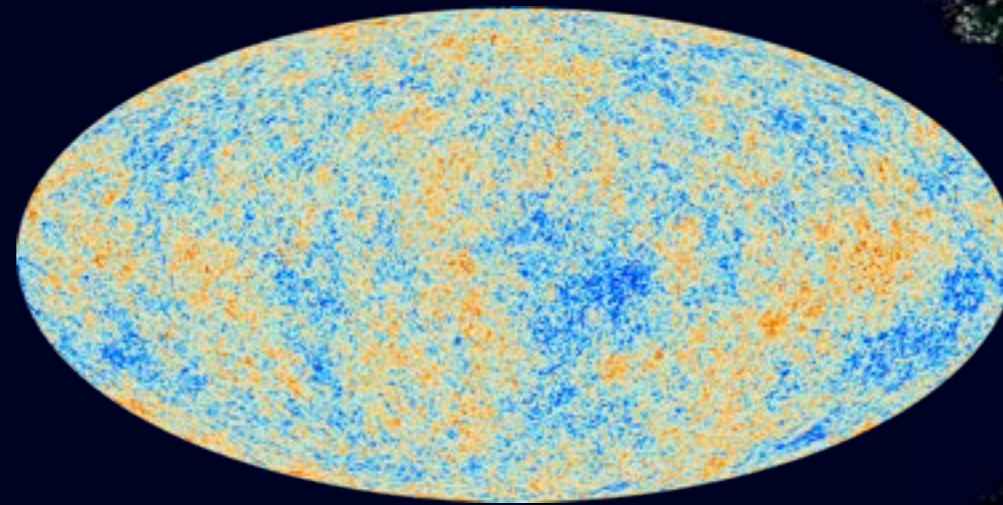
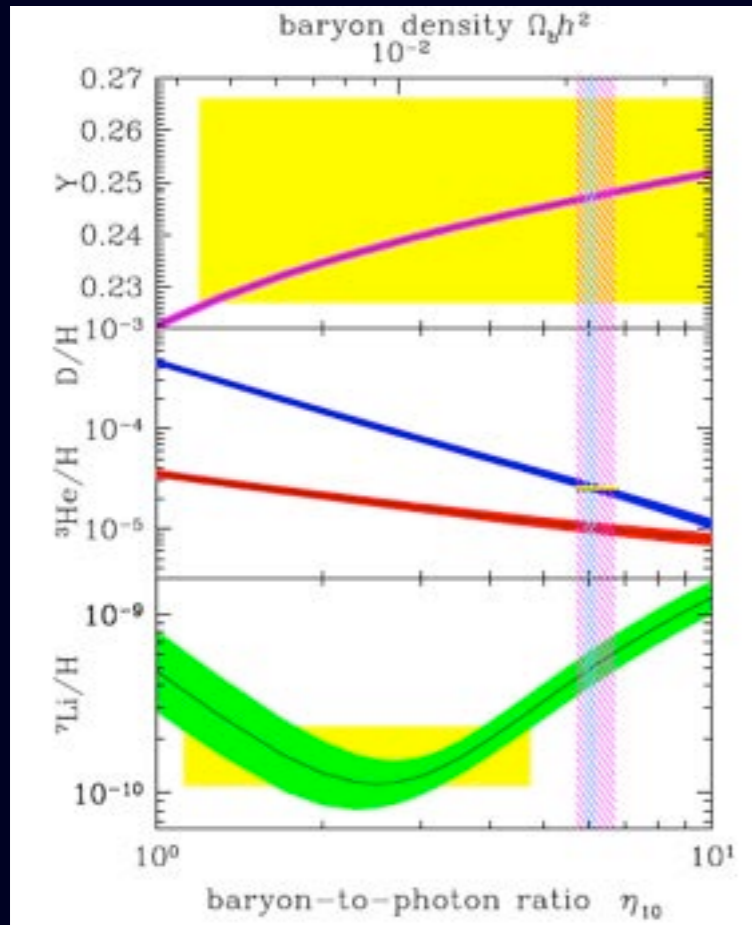
...is necessary to consider the cosmological constraints on extra species and to assess the conditions under which ν_s are produced

Cosmological observations

1 MeV

1 eV

T



Sensitivity to N_{eff} and ν flavour

Sensitivity to N_{eff} and ν masses



Radiation Content in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\varepsilon_R = \varepsilon_\gamma + \varepsilon_\nu + \varepsilon_x$$

The **non-e.m.** energy density is parameterized by the effective numbers of neutrino species N_{eff}

$$\varepsilon_\nu + \varepsilon_x = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 N_{\text{eff}} = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 (N_{\text{eff}}^{\text{SM}} + \Delta N)$$

$$N_{\text{eff}}^{\text{SM}} = 3.046 \quad \text{due to non-instantaneous neutrino decoupling}$$

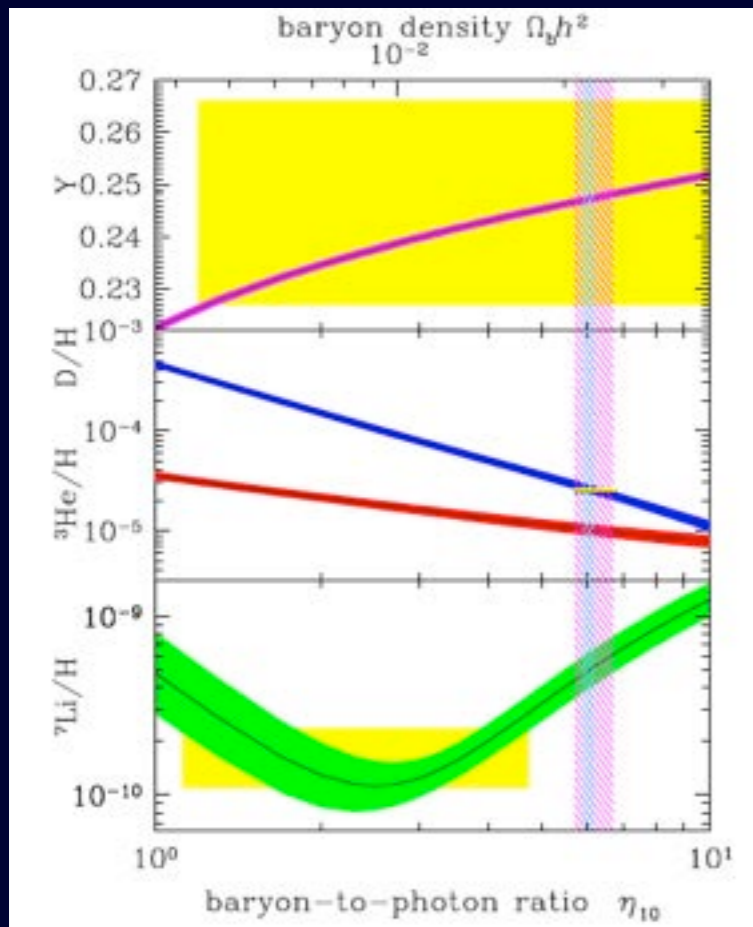
(+ oscillations)

Mangano et al. 2005

ΔN = Extra Radiation: axions and axion-like particles, **sterile neutrinos (totally or partially thermalized)**, neutrinos in very low-energy reheating scenarios, relativistic decay products of heavy particles...

Di Bari et al. 2013, Boehm et al. 2012, Conlon and Marsh, 2013, Gelmini, Palomarez-Ruiz, Pascoli, 2004

Impact on Big Bang Nucleosynthesis



At $T \sim 0.01$ MeV production of the primordial abundances of light elements, in particular ${}^2\text{H}$, ${}^4\text{He}$

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio freezes out*

$$\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T} \rightarrow 1/7$$

Sterile ν influence on BBN :

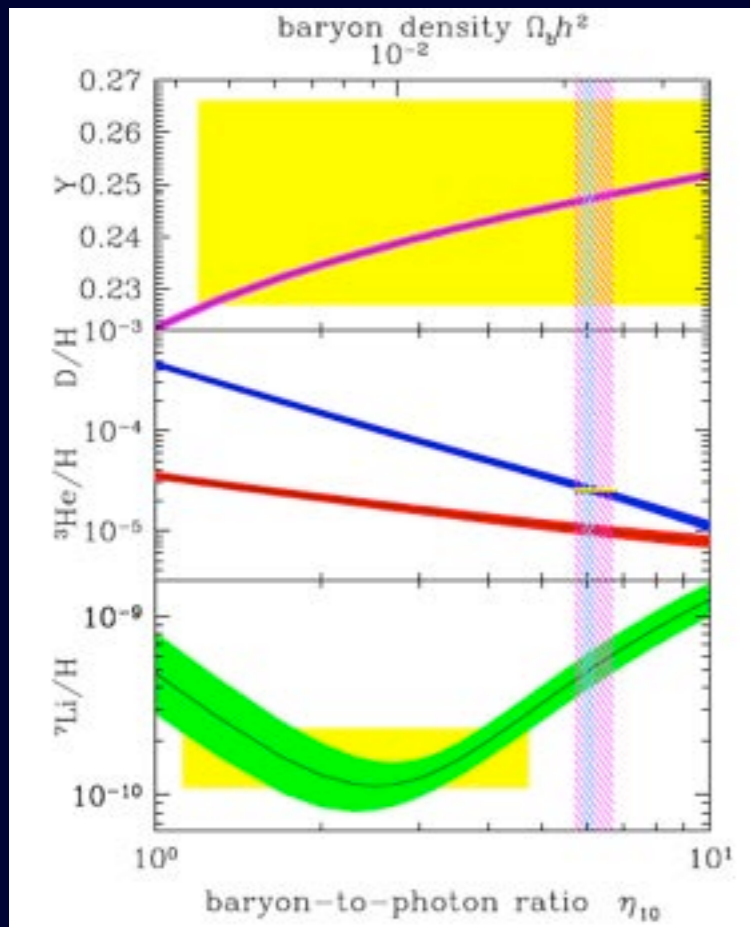
- contribution to the radiation energy density governing H before and during BBN

$$N_{\text{eff}} \uparrow \rightarrow H \uparrow \rightarrow \text{early freeze out} \rightarrow n/p \uparrow \rightarrow {}^4\text{He} \uparrow$$

- oscillating with the active neutrinos, can distort the active spectra which are the basic input for BBN



Impact on Big Bang Nucleosynthesis



At $T \sim 1 - 0.01$ MeV production of the primordial abundances of light elements, in particular ^2H , ^4He

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio freezes out*

$$\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T} \rightarrow 1/7$$

BBN constraint on ΔN_{eff} : **NO strong preference**

$$\Delta N_{\text{eff}} \leq 1 \quad (95\% \text{ C.L.})$$

Hamann et al, 2011

Mangano and Serpico, 2012



From new precise measure of D in damped Lyman- α system

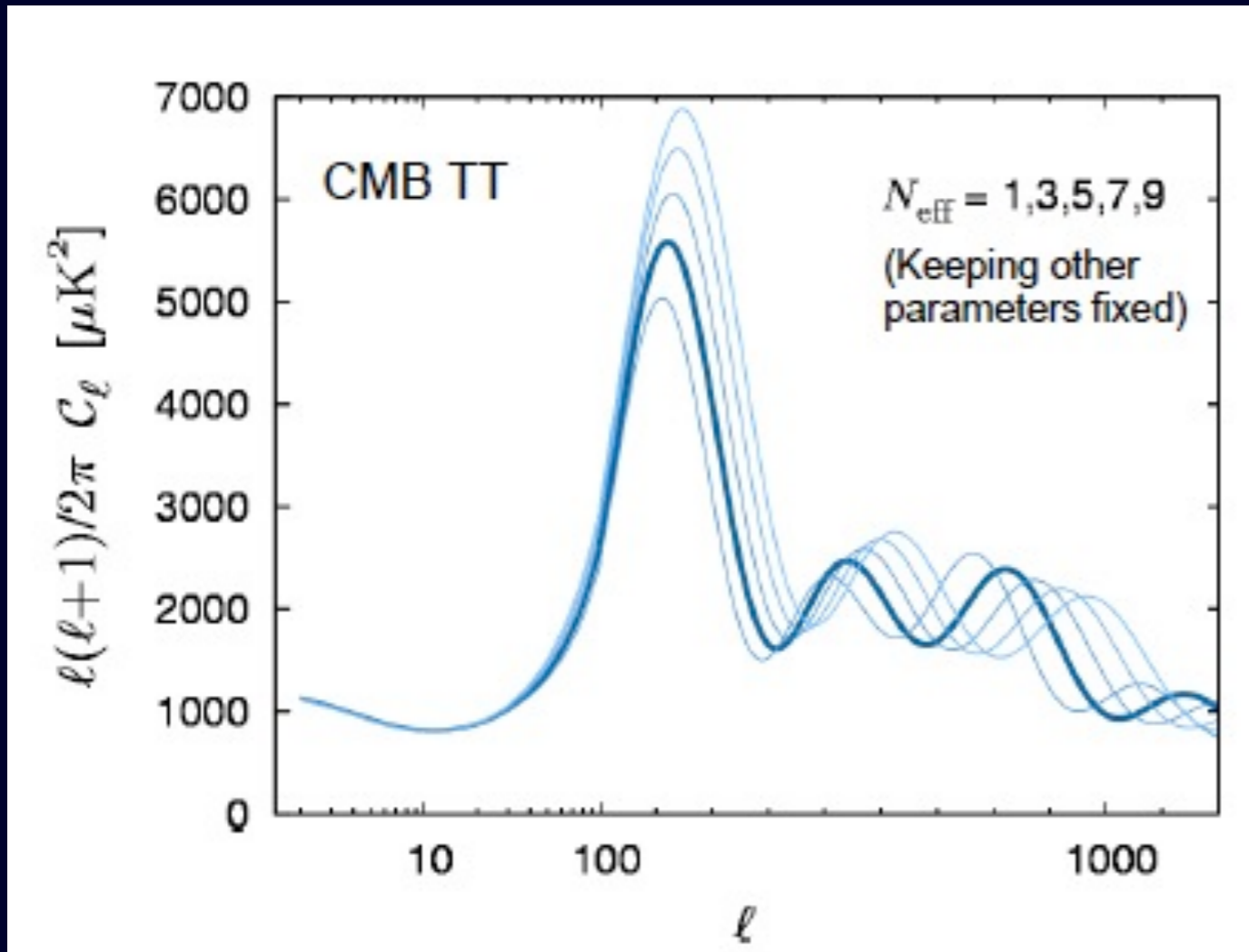
$$N_{\text{eff}} = 3.28 \pm 0.28$$

Cooke, Pettini et al., 2013

1 extra d.o.f. ruled out at 99.3 C.L.

Impact on CMB

If sterile neutrinos are still relativistic at the CMB epoch, they impact the CMB spectrum



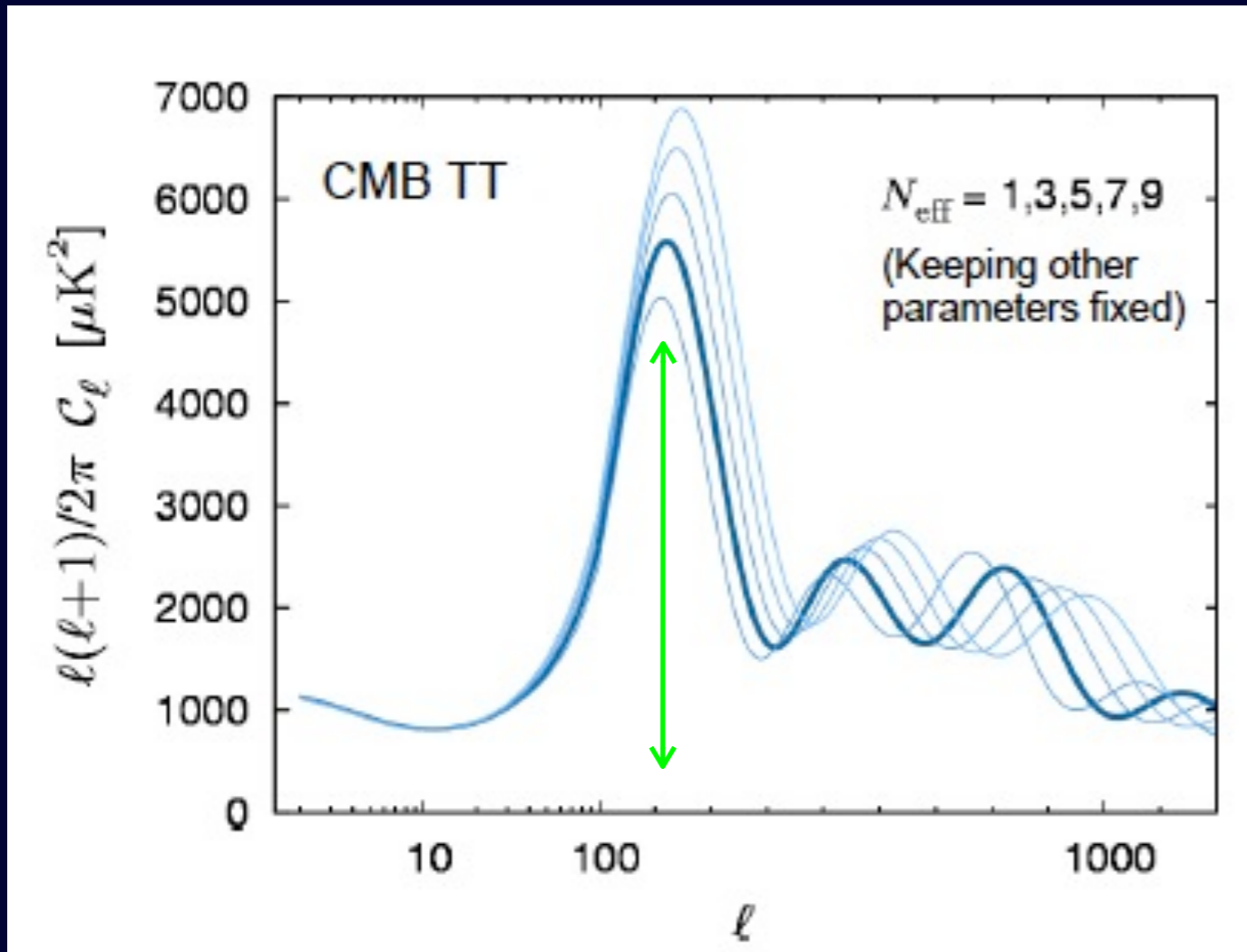
N_{eff} and m_ν affect the time of *matter-radiation equality* \Rightarrow consequences on the amplitude of the first peak and on the peak locations

$$1 + z_{\text{eq}} = \frac{\omega_m}{\omega_\gamma} \frac{1}{1 + 0.227 N_{\text{eff}}}$$



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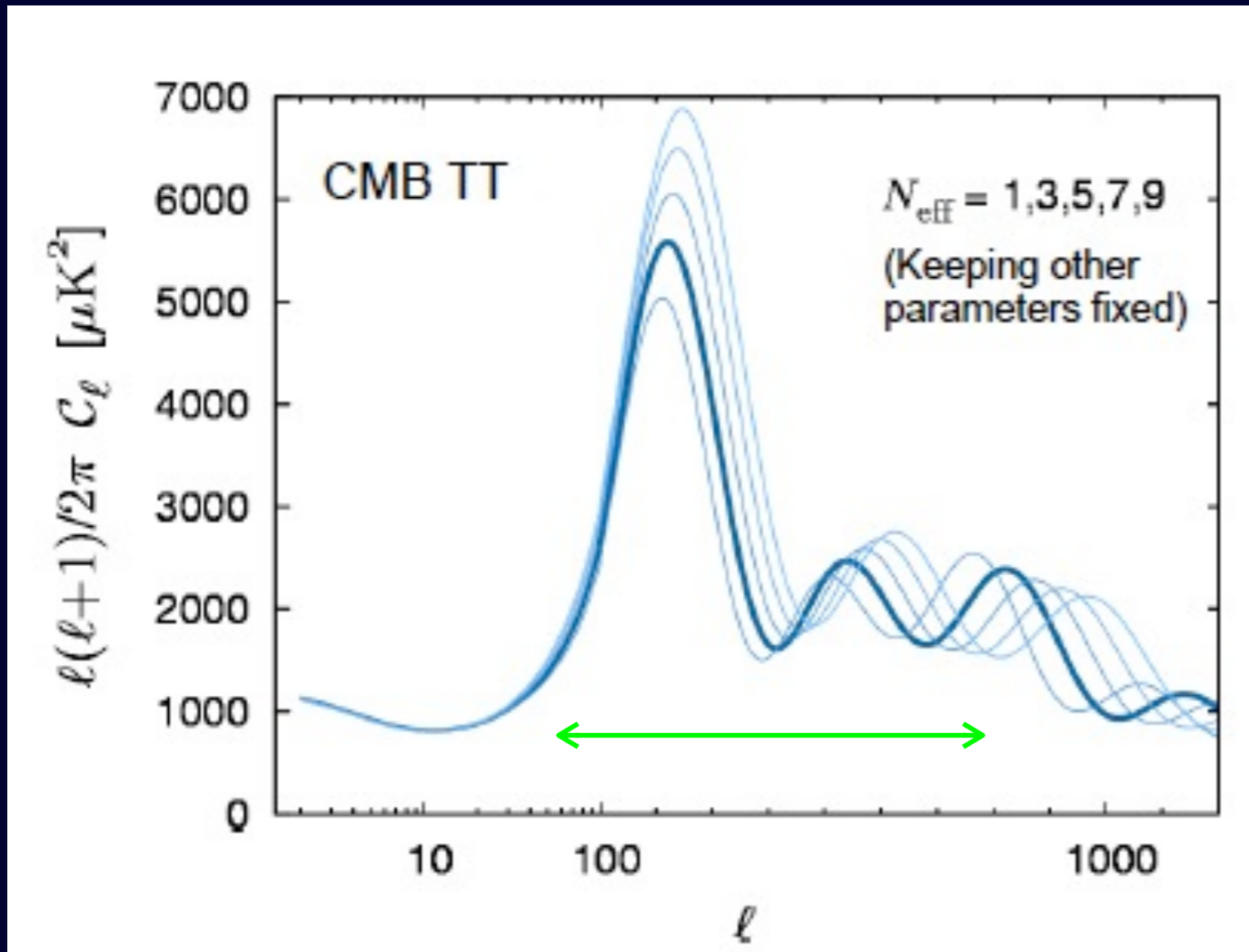
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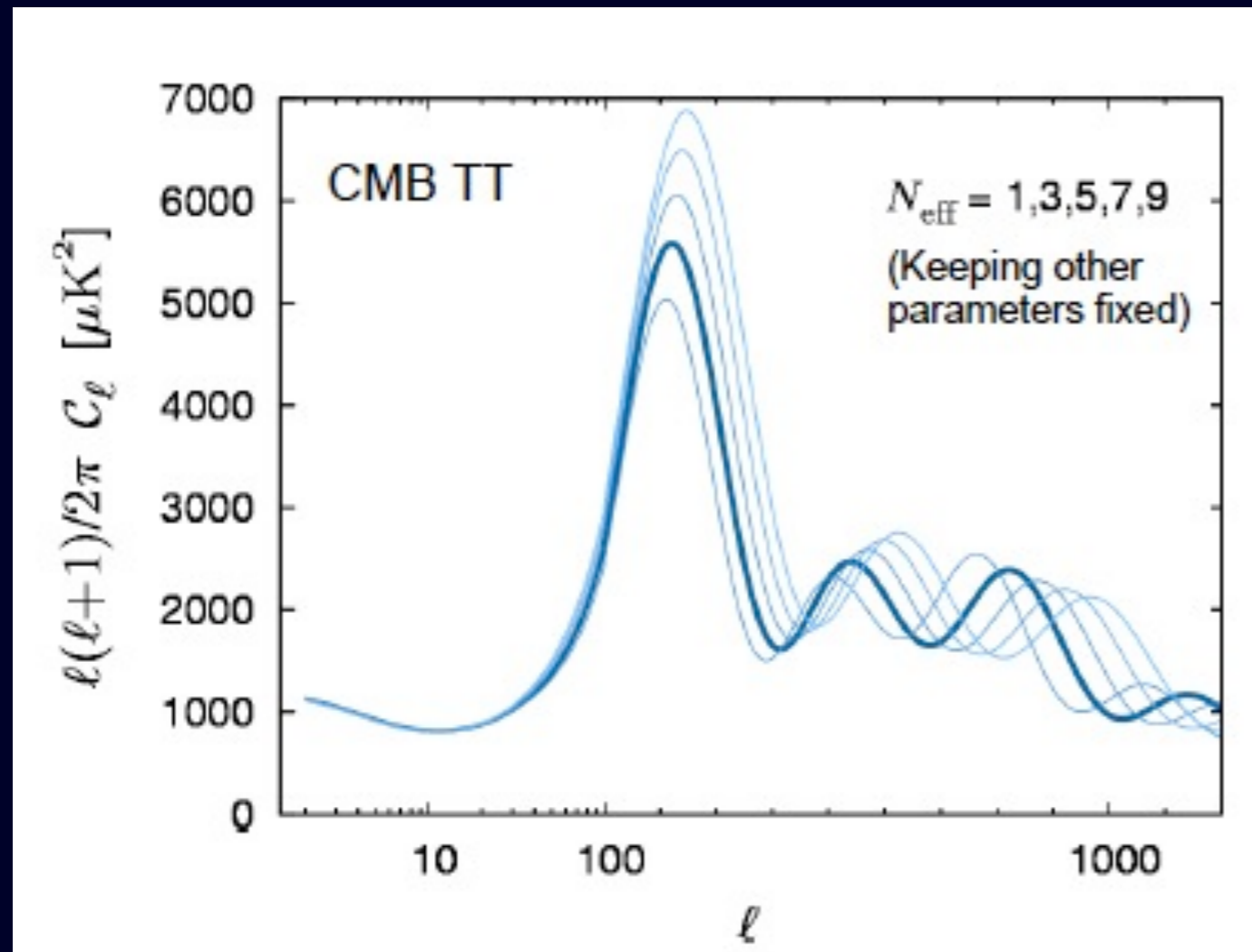
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$$1 + z_{\text{eq}} = \frac{\omega_m}{\omega_\gamma} \frac{1}{1 + 0.227 N_{\text{eff}}}$$

Same data used to measure other cosmological parameters

basic parameters of Λ CDM:

$$(\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, n_s, A_s, \tau)$$

+ derived parameters

$$(H_0, \Omega_k, \Omega_\Lambda, N_{\text{eff}}, \sigma_8, \sum m_\nu, z_{re}, Y_p, w, \Omega_m z_{LS} \dots)$$

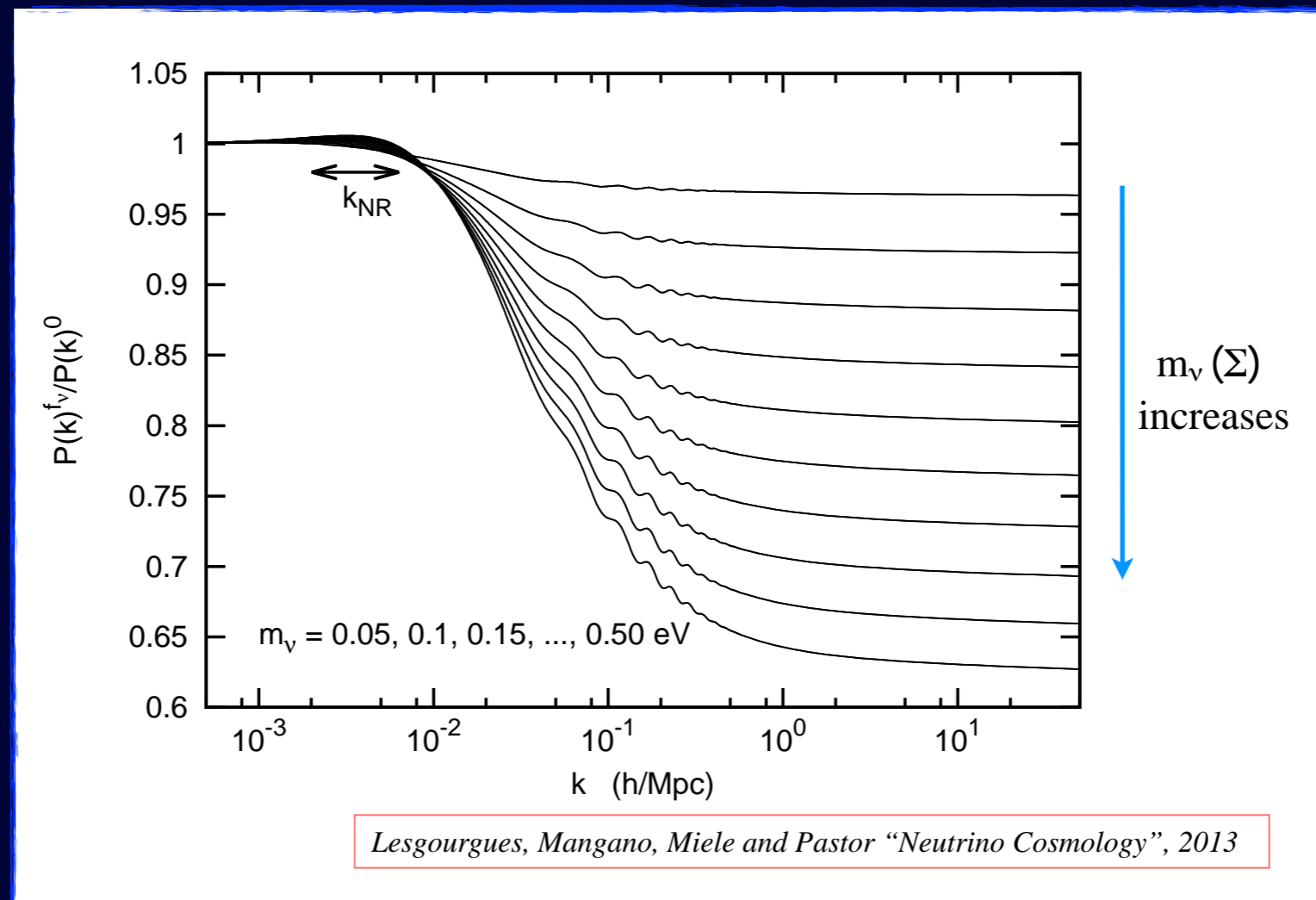
\rightarrow *degeneracies*

\rightarrow *necessary to combine with other cosmological probes*

Impact on the LSS

The small-scale matter power spectrum $P(k > k_{NR})$ is reduced in presence of massive ν :

- ✓ free-streaming neutrinos do not cluster
- ✓ slower growth rate of CDM (baryon) perturbations



N_{eff} and Σm_ν constraints after Planck



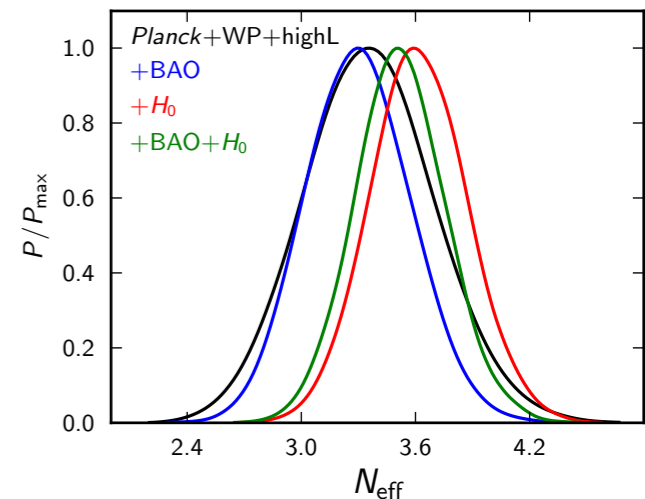
Standard scenario:

✓ $N_{\text{eff}} = 3.30 \pm 0.54$ (95 % C.L.; Planck+WP+highL+BAO)

↪ compatible with the standard value at $1-\sigma$

✓ For 3 degenerate active ν :

$\Sigma m_\nu < 0.23 \text{ eV}$ (95 % C.L.; Planck+WP+highL+BAO)



Planck XVI, 2013

Standard scenario:

✓ the preference for extra radiation is further reduced

$N_{\text{eff}} = 3.15 \pm 0.46$ (95 % C.L.; PlanckTT+lowP+BAO)

✓ For 3 degenerate active ν :

$\Sigma m_\nu < 0.21 \text{ eV}$ (95 % C.L.; Planck TT+WP+ lowP+BAO)



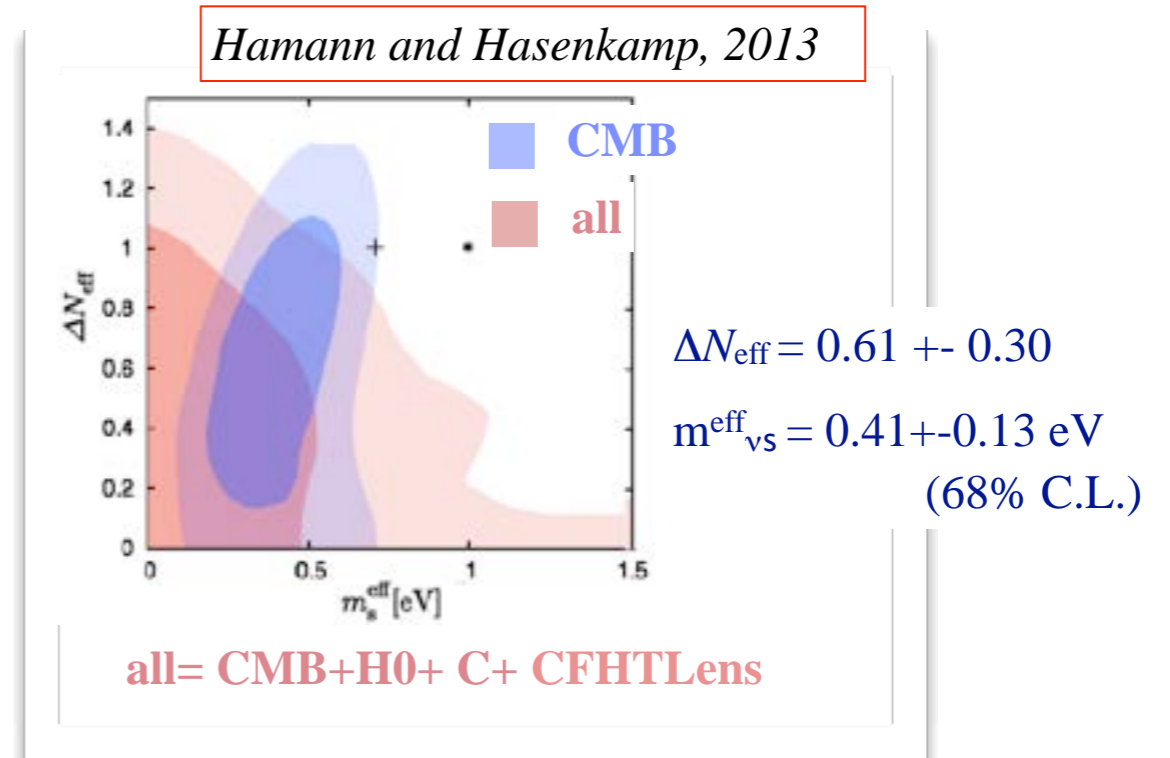
Planck XIII, 2015

see Henrot-Versille's talk

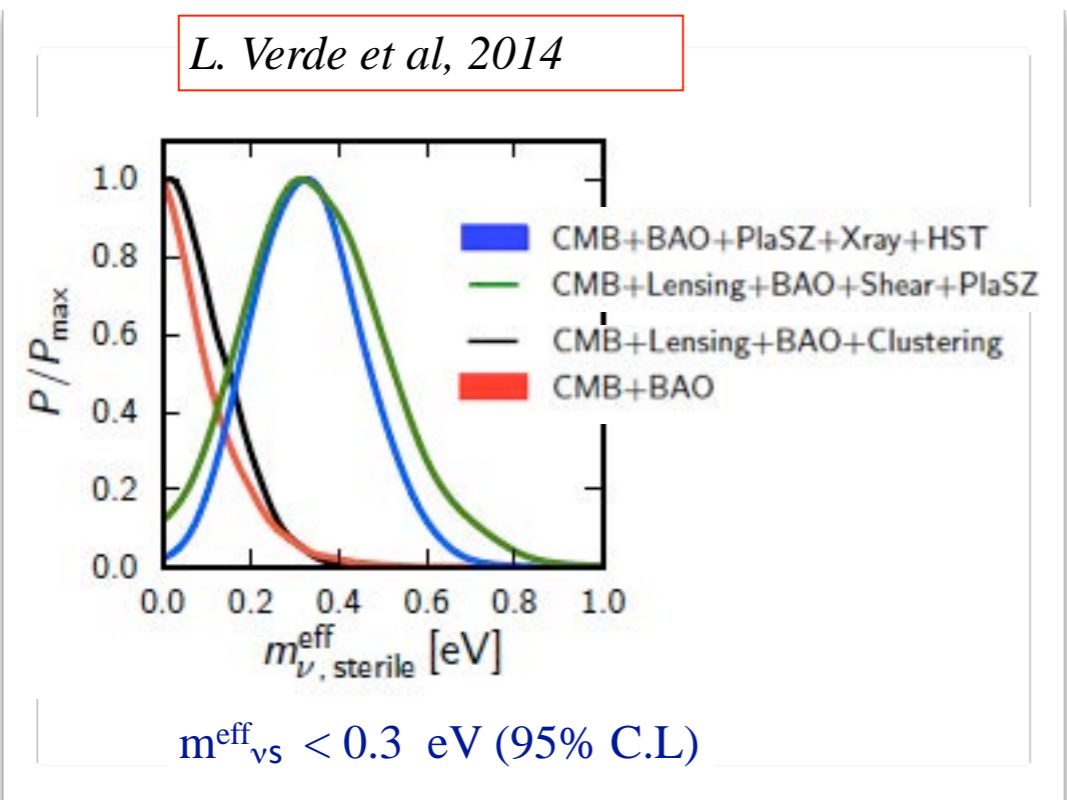
Joint constraints on N_{eff} and $m_{\nu_s}^{\text{eff}}$

model	Planck +	mass bound (eV) (95% C.L.)
Joint analysis N_{eff} & 1 mass ν_s	WP+HighL+BAO	$N_{\text{eff}} < 3.80$ $m_{\nu_s}^{\text{eff}} < 0.42$

Planck XVI, 2013



$$m_{\nu_s}^{\text{eff}} \equiv (94, 1 \Omega_\nu h^2) \text{ eV}$$



model	Planck TT +	mass bound (eV) (95% C.L.)
Joint analysis N_{eff} & 1 mass ν_s (prior $m_{\nu_s} < 10 \text{ eV}$)	lowP+lensing+BAO	$N_{\text{eff}} < 3.7$ $m_{\nu_s}^{\text{eff}} < 0.52$
Joint analysis N_{eff} & 1 mass ν_s (prior $m_{\nu_s} < 2 \text{ eV}$)	lowP+lensing+BAO	$N_{\text{eff}} < 3.7$ $m_{\nu_s}^{\text{eff}} < 0.38$

Planck XIII, 2014

Active-sterile flavour evolution

Sterile ν are produced in the Early Universe by the mixing with the active species in presence of collisions

Evolution equation:

$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

$$\rho_{\mathbf{p}} = \begin{pmatrix} \rho_{ee} & \rho_{e\mu} & \rho_{e\tau} & \rho_{es} \\ \rho_{\mu e} & \rho_{\mu\mu} & \rho_{\mu\tau} & \rho_{\mu s} \\ \rho_{\tau e} & \rho_{\tau\mu} & \rho_{\tau\tau} & \rho_{\tau s} \\ \rho_{se} & \rho_{s\mu} & \rho_{s\tau} & \rho_{ss} \end{pmatrix}$$

↙
 ν ensemble

$$\Omega = \Omega_{\text{vac}} + \Omega_{\text{mat}} + \Omega_{\nu-\nu}$$

↙
Vacuum term

↙
MSW effect with background medium (refractive effect)

↙
refractive ν - ν self-interactions term

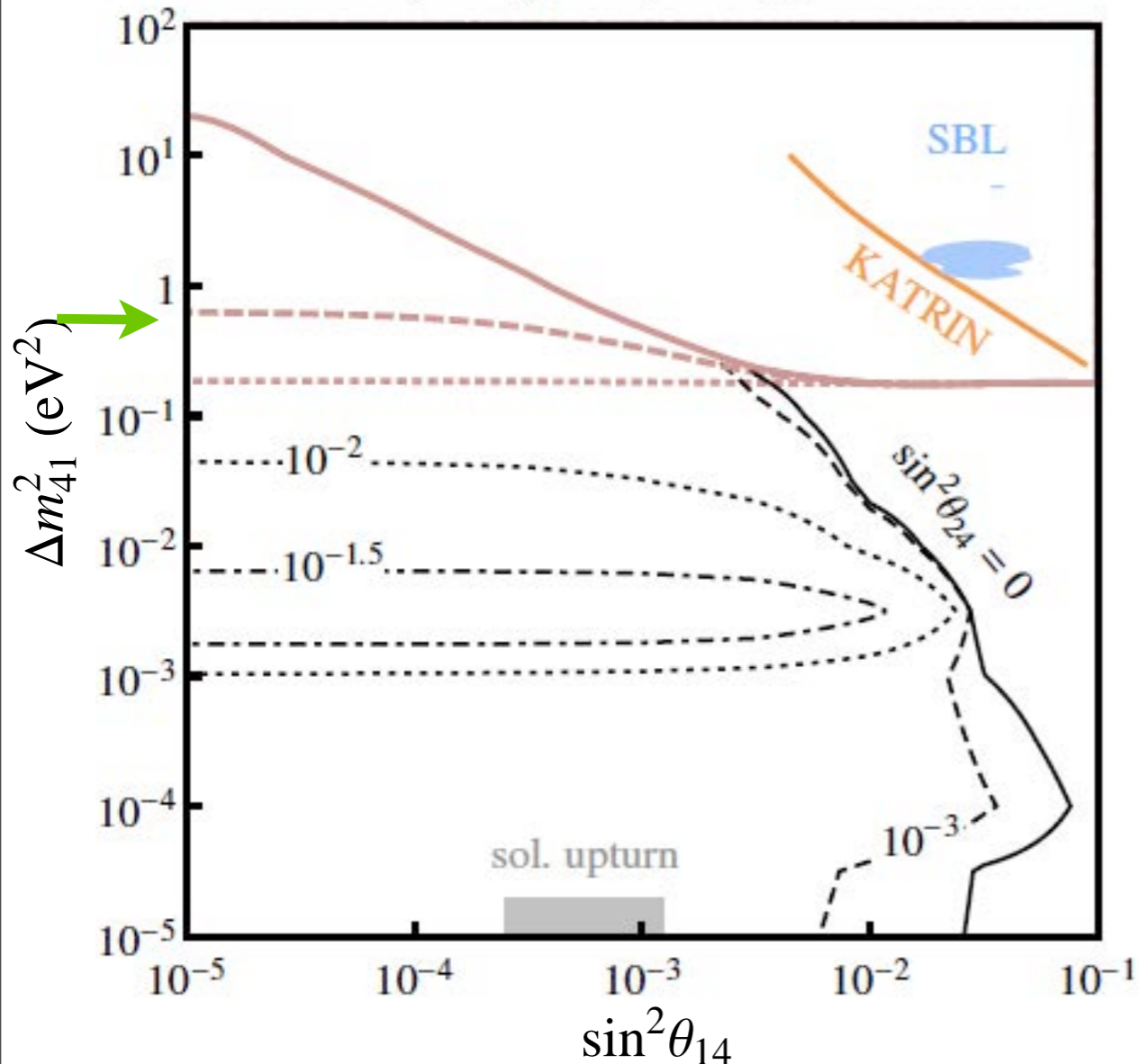
$$C[\rho]$$

Collisional term

creation, annihilation and all the momentum exchanging processes

Bounds on active-sterile mixing parameters after Planck

a) $\Delta m_{41}^2 > 0$, $\sin^2 \theta_{34} = 0$



3+1 Scenario

Mirizzi, Mangano, N.S et al 2013

See also:

Hannestad, Tamborra and Tram 2012

Cirelli, Marandella, Strumia, Vissani, 2004

Archidiacono et al., 2013

Similar bounds would be obtained with Planck 2015 data

Radiation bounds

- Black curves imposing the 95% C.L. Planck constraint $N_{\text{eff}} < 3.8$ on computed $N_{\text{eff}} = \frac{1}{2} \text{Tr}[\rho + \bar{\rho}]$

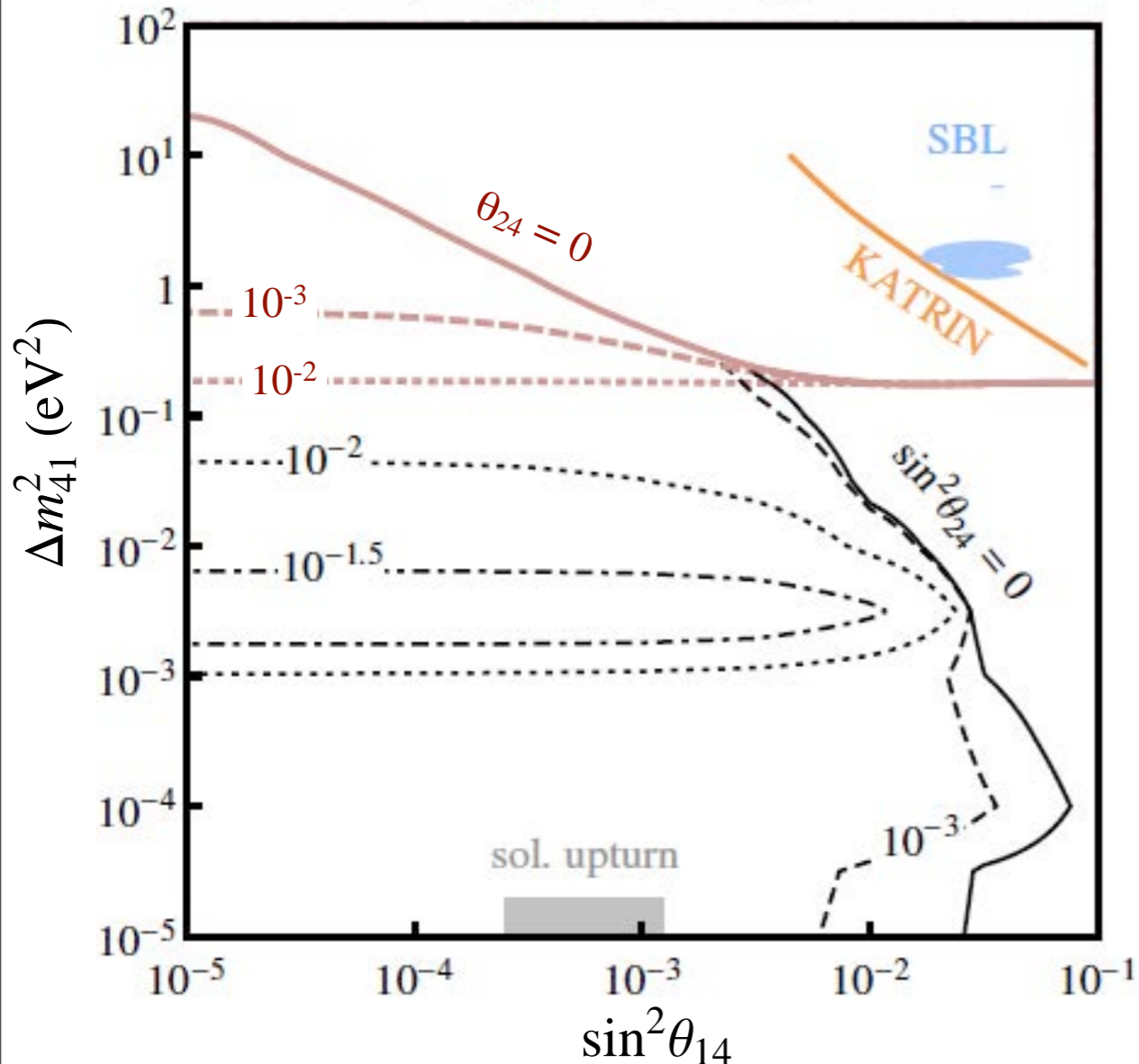
The excluded regions are those on the right or at the exterior of the black contours.

Note: above $m \sim O(1 \text{ eV})$, sterile ν are not relativistic anymore at CMB \rightarrow **NO radiation constraint**

BUT mass constraints become important

Bounds on active-sterile mixing parameters after Planck

a) $\Delta m_{41}^2 > 0, \sin^2 \theta_{34} = 0$



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Mass bounds

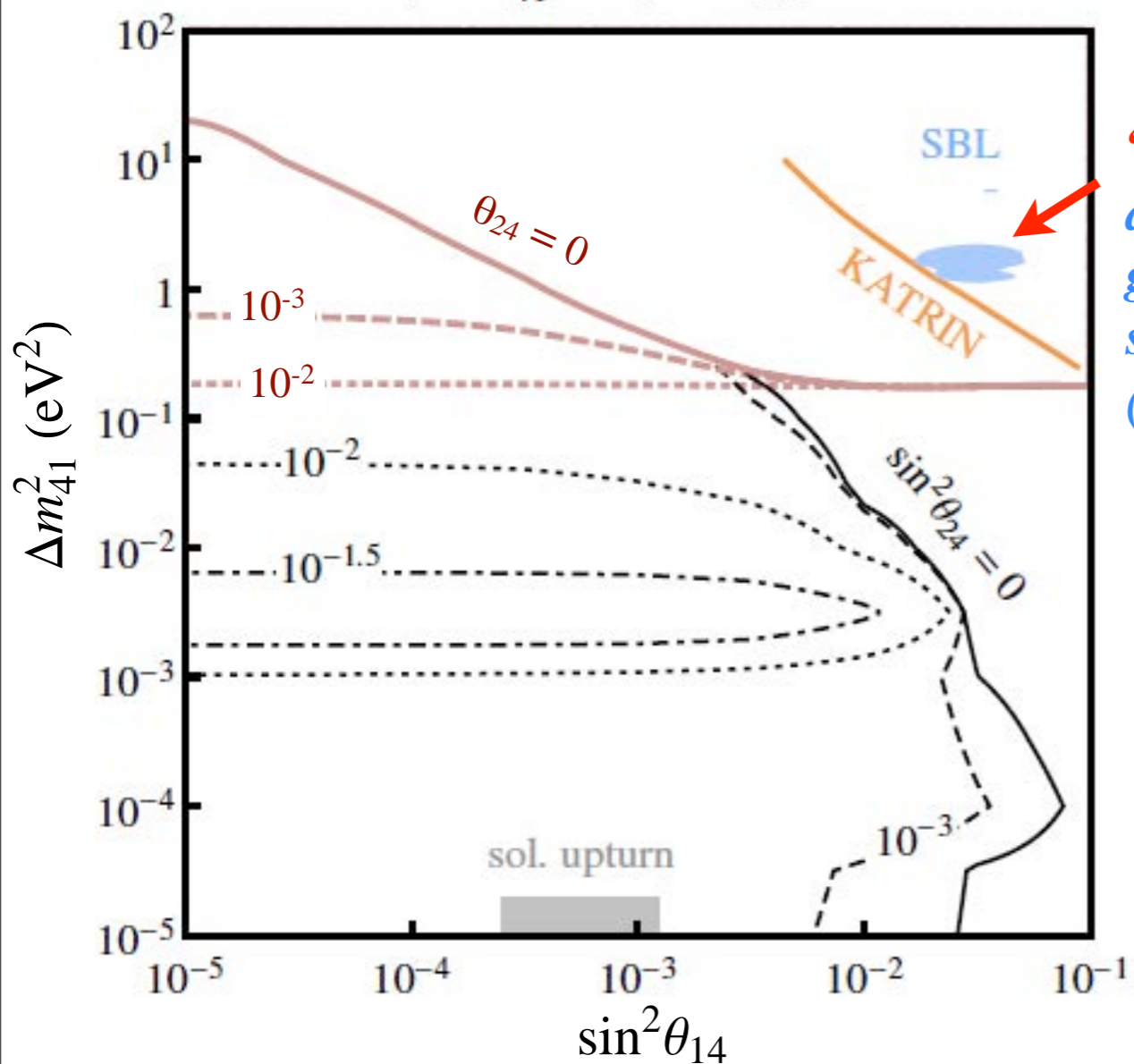
- Red curves imposing the 95% C.L. Planck constraint $m_{\nu_s}^{\text{eff}} < 0.42 \Leftrightarrow \Omega_{\nu} h^2 < 4.5 \cdot 10^{-3}$ on computed

$$\Omega_{\nu} h^2 = \frac{1}{2} \frac{[\sqrt{\Delta m_{41}^2} (\rho_{ss} + \bar{\rho}_{ss})]}{94.1 \text{ eV}}$$

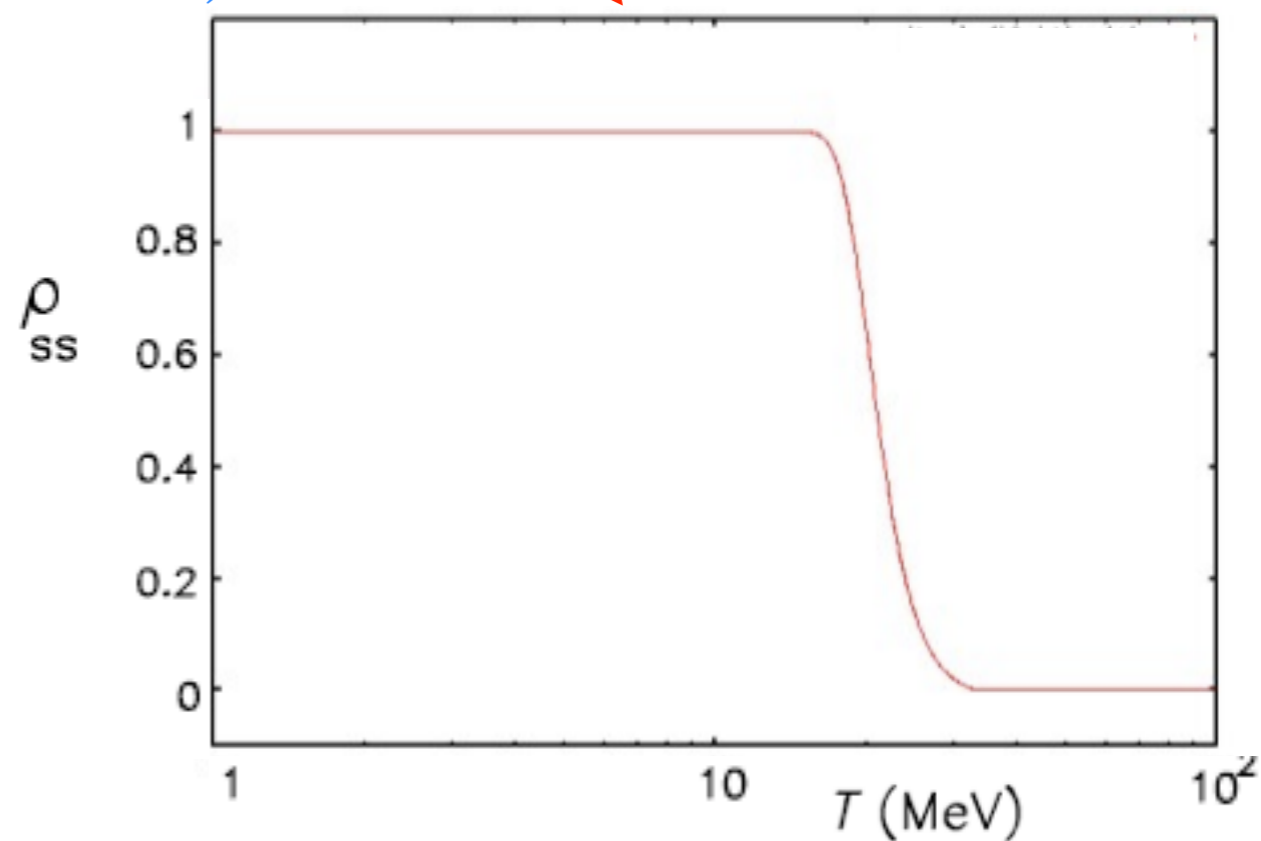
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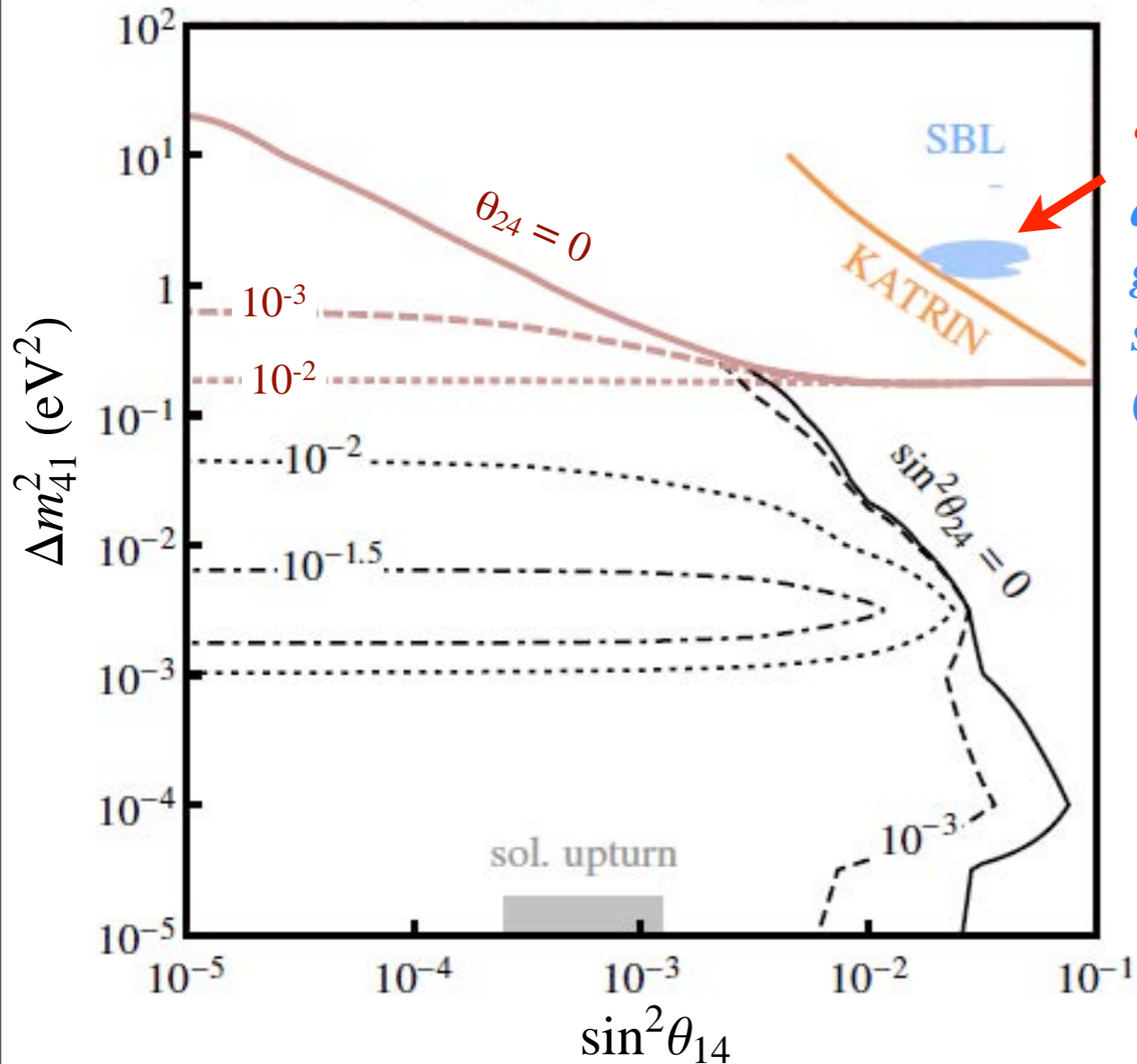


“eV sterile ν ”
 allowed region from
 global analysis of SBL
 $\sin^2 \theta_{24} = 10^{-2}$, 95% C.L.
 (Giunti et al.)

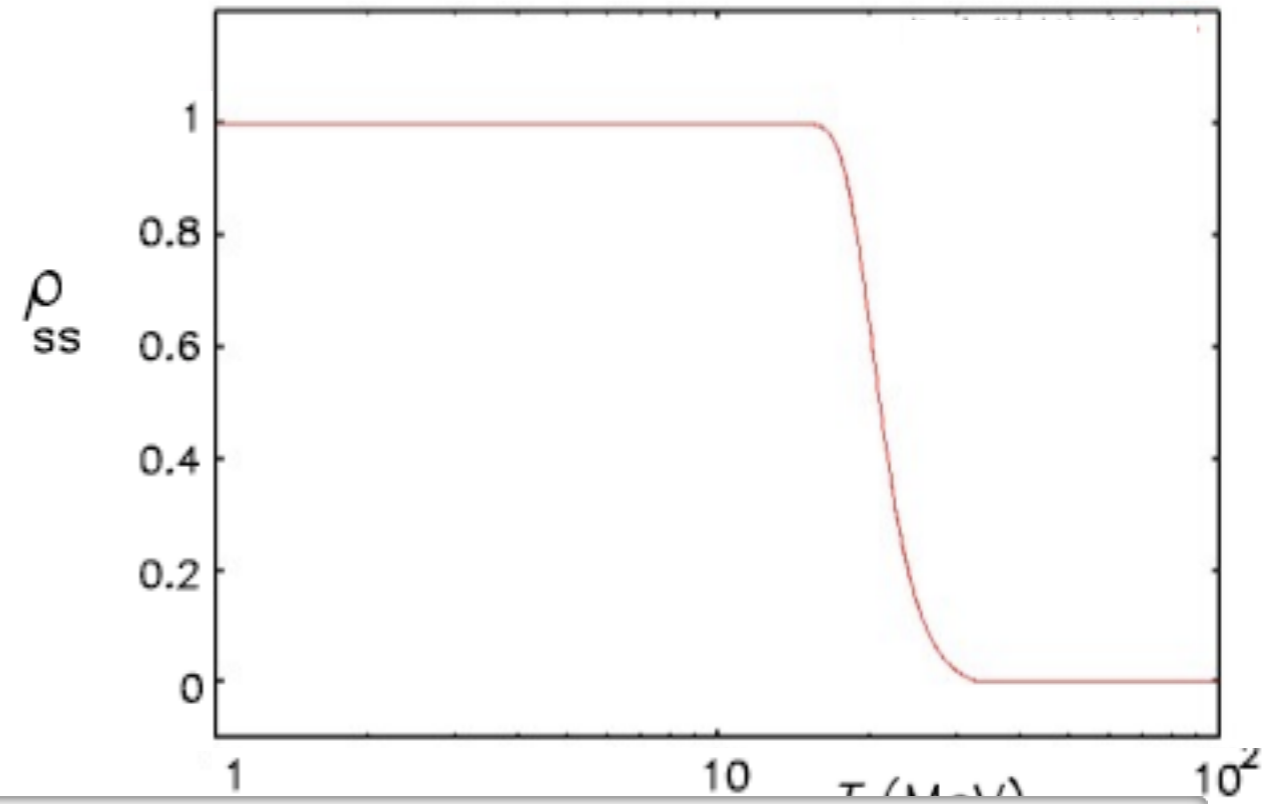


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Thermalized sterile ν with $m \sim \mathcal{O}(1 \text{ eV})$ strongly disfavored by cosmological constraints

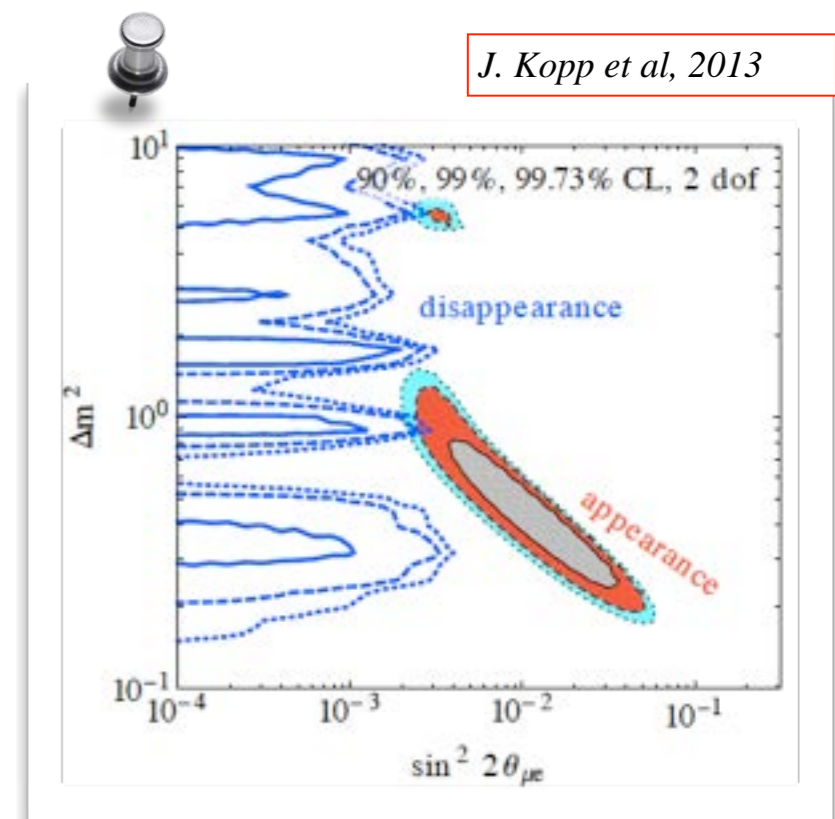
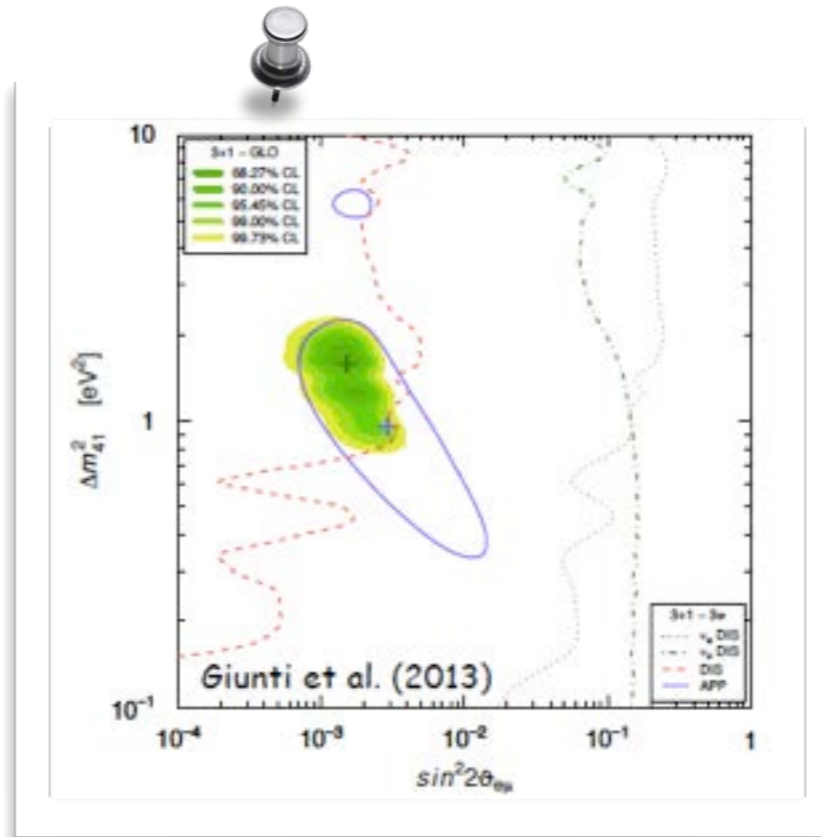
- 3+1: Too *heavy* for **LSS/CMB**
- 3+2: Too *heavy* for **LSS/CMB** and too *many* for **BBN/CMB**

eV Sterile Neutrino

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-  MiniBooNE
-  Gallium
-  Reactor

see
White paper, Abazajian et al., 2012,
Palazzo, 2013



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(...sometimes in tension among themselves....)

eV

Interpretation: **1** (or more) *sterile neutrino* with $\Delta m^2 \sim O(eV^2)$ and $\theta_s \sim O(\theta_{13})$

Are eV ν_s compatible with cosmology? NO

Possible solutions...?

🌐 Different mechanisms to suppress the ν_s abundance:

1. large $\nu-\bar{\nu}$ asymmetries

- ✓ In the presence of large $\nu-\bar{\nu}$ asymmetries ($\sim 10^{-2}$) sterile production strongly suppressed. Mass bound can be evaded

Mirizzi, N.S., Miele, Serpico 2012
Saviano et al., 2013
Hannestad, Tamborra and Tram 2012
Chu & Cirelli, 2006
Di Bari et al, 2001

⚠ **Non trivial implication for BBN**

2. hidden and “secret” interactions for sterile neutrinos

- ✓ Sterile ν feel a new potential that suppresses active-sterile mixing

Hannestad et al., 2013,
Dasgupta and Kopp 2013,
Bringmann et al., 2013
Archidiacono et al., 2014
Saviano et al., 2014
Mirizzi, Mangano, Pisanti, N.S. 2014
Cherry et al, 2014
Tang, 2014

⚠ **Scenario strongly constrained by BBN and neutrino mass bounds**

3. low reheating scenario

- ✓ sterile abundance depends on reheating temperature

Gelmini, Palomarez-Ruiz, Pascoli, 2004
Yaguna 2007

⚠ Simplified scenarios

🌐 Modification of cosmological models

Gariazzo, Giunti Laveder, 2015

Inflationary Freedom

- ✓ Shape of primordial power spectrum of scalar perturbations different from the usual power-law

Conclusions

- neutrino cosmology is entering the precision epoch

$$N_{\text{eff}} < 4 \quad \Sigma_{\text{mv}} < 0.23 \text{ eV} \quad m_{\nu\text{S}}^{\text{eff}} < 0.7 \text{ eV}$$

- Thermalized eV sterile ν *incompatible* with cosmological bounds:
too heavy for structure formation

- New exotics scenarios are required (primordial neutrino asymmetry, hidden interactions, inflationary freedom...) →

→ *however the reconciliation with cosmology is not guaranteed and in some cases disfavoured.*

Conclusions

- neutrino cosmology is entering the precision epoch

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→ *however the reconciliation with cosmology is not guaranteed and in some cases disfavoured.*

Open questions:

- *Will ΔN_{eff} be definitely ruled-out in the future?*
- *Which are the absolute masses of neutrinos?*
- *Will the laboratory anomalies be confirmed?*

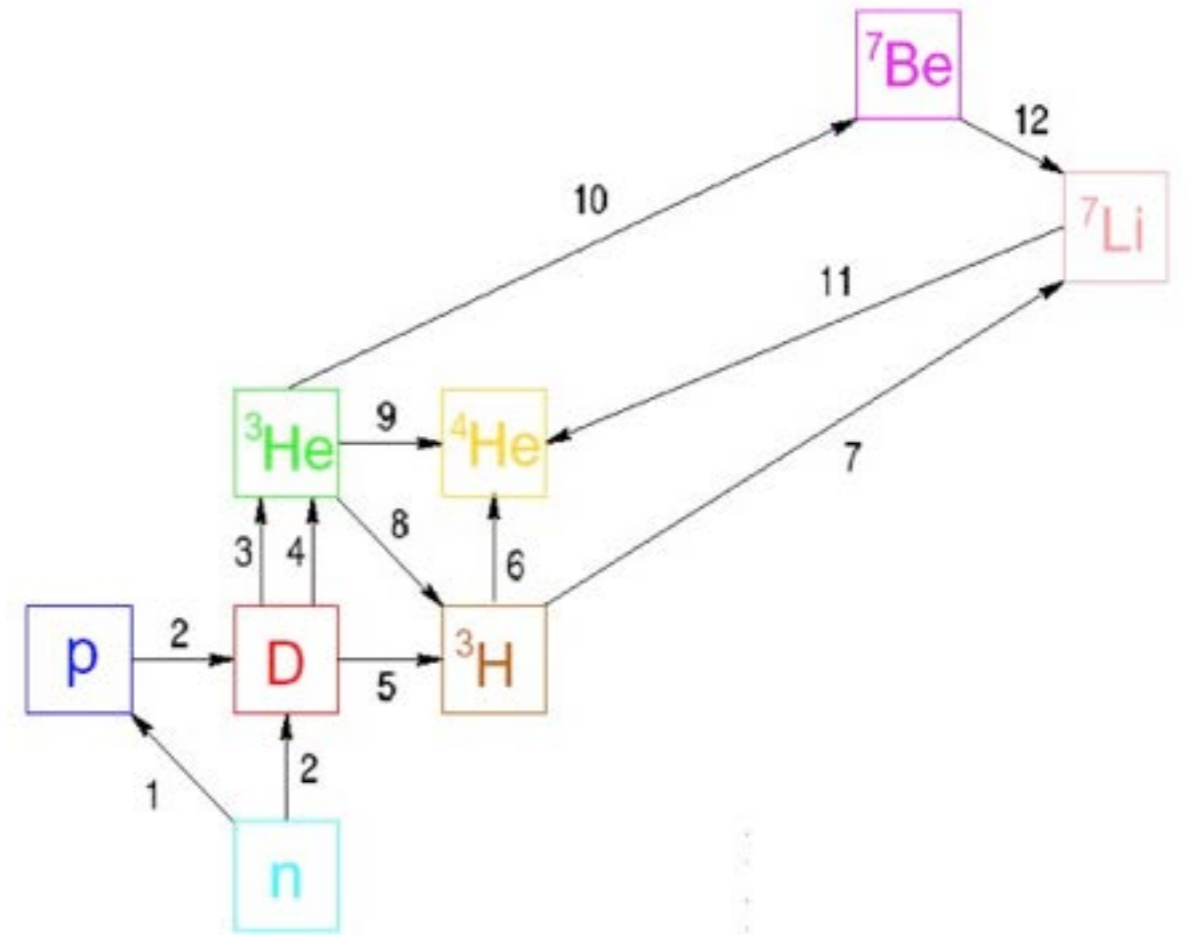
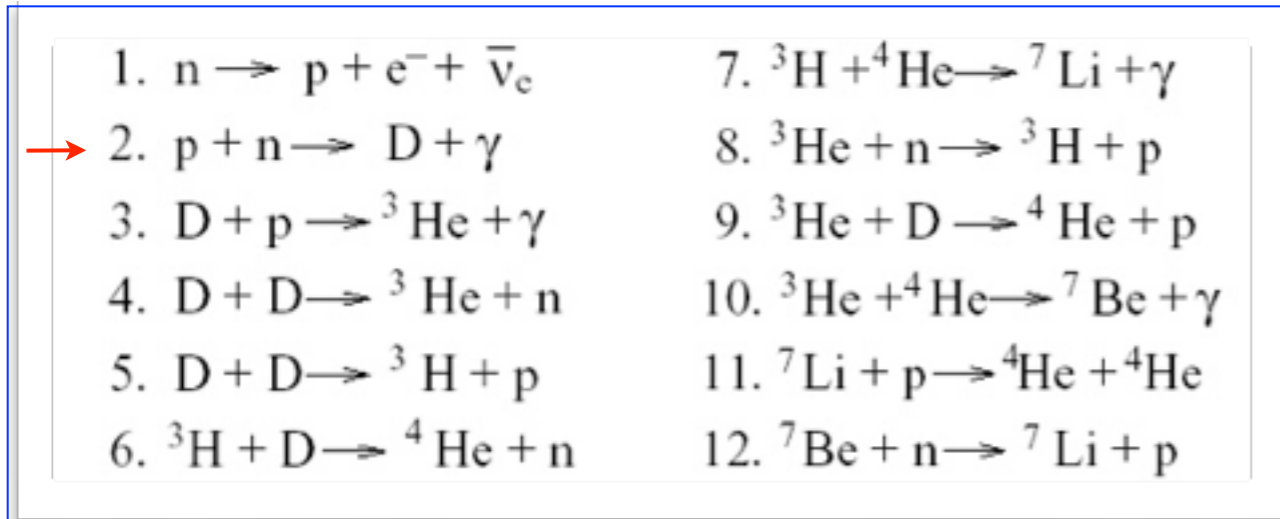


Thank you!

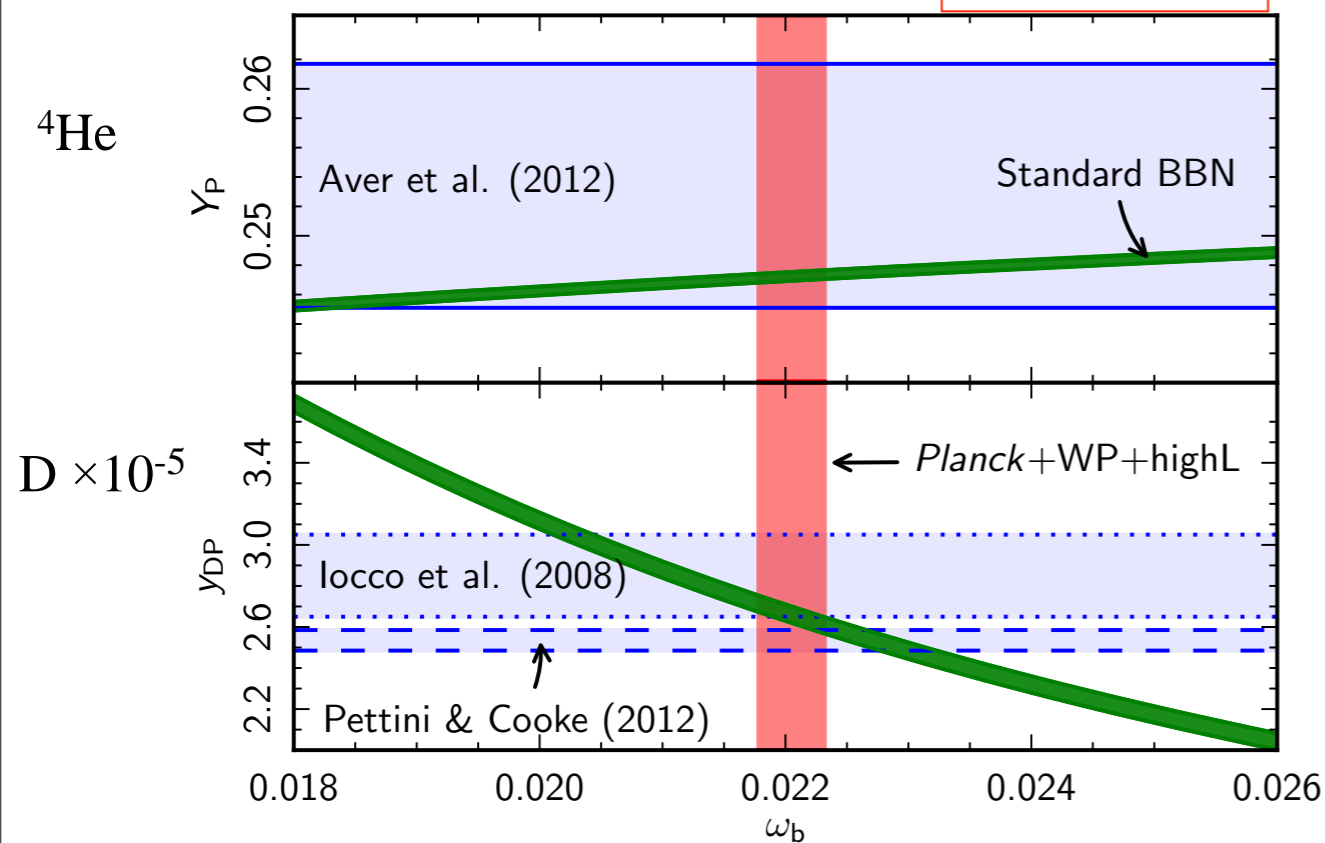
Big Bang Nucleosynthesis (II)

* 0.1-0.01 MeV

Formation of light nuclei starting from D



Planck XVI, 2013



Prediction for ${}^4\text{He}$ and D in a **standard** BBN obtained by Planck collaboration using **PARthENoPE**

Blue regions: primordial yields from measurements performed in different astrophysical environments

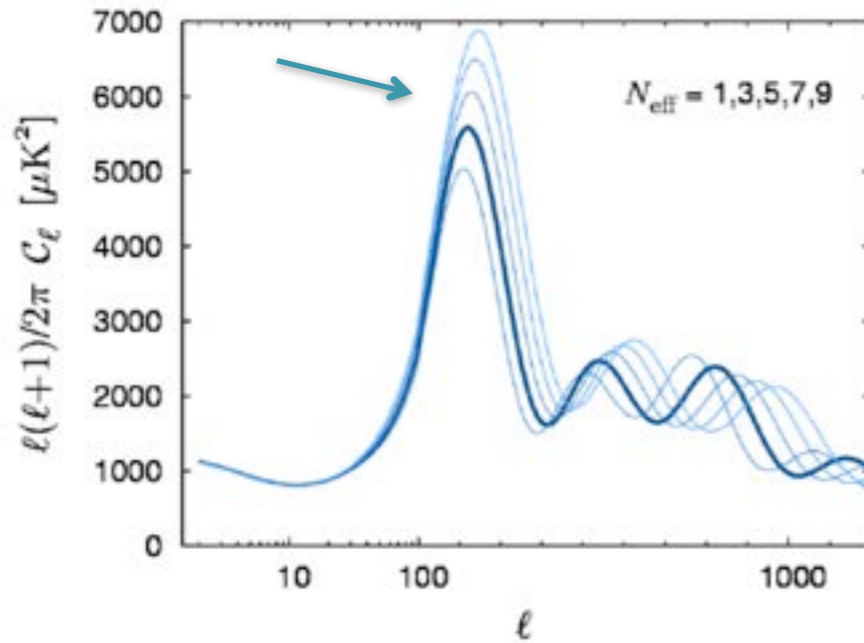
$$\omega_b = 0.02207 \pm 0.00027$$

Extra radiation impact on CMB...

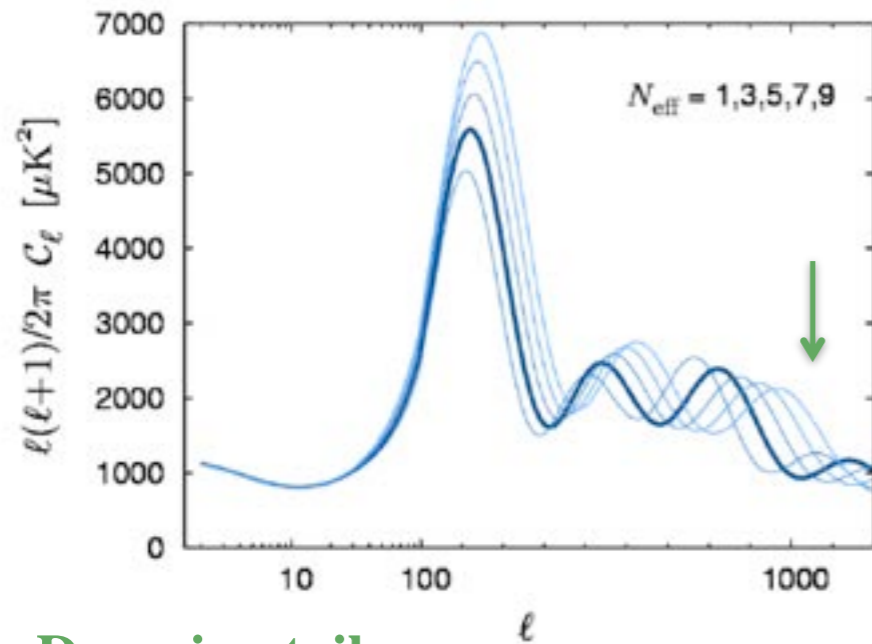
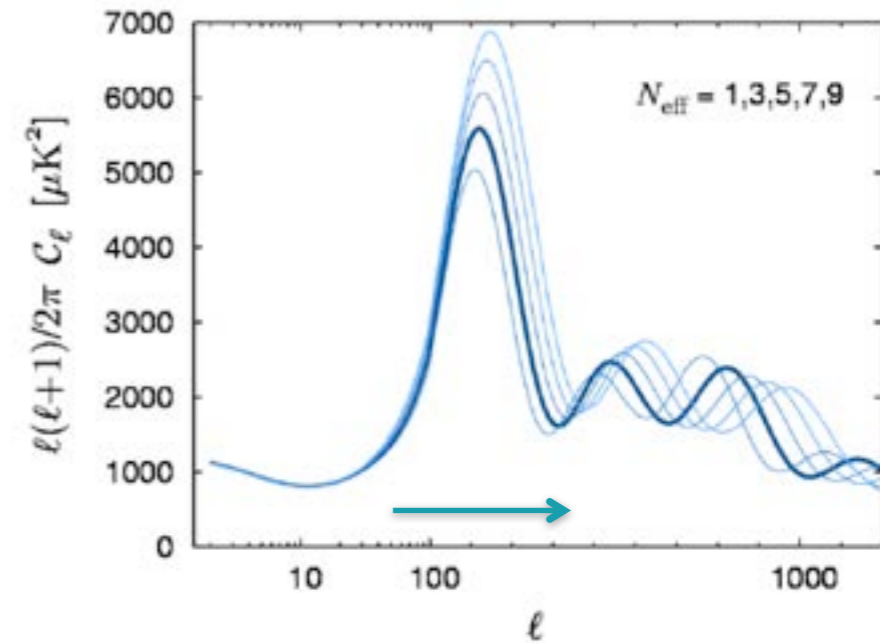
... and degeneracies

Matter-radiation equality

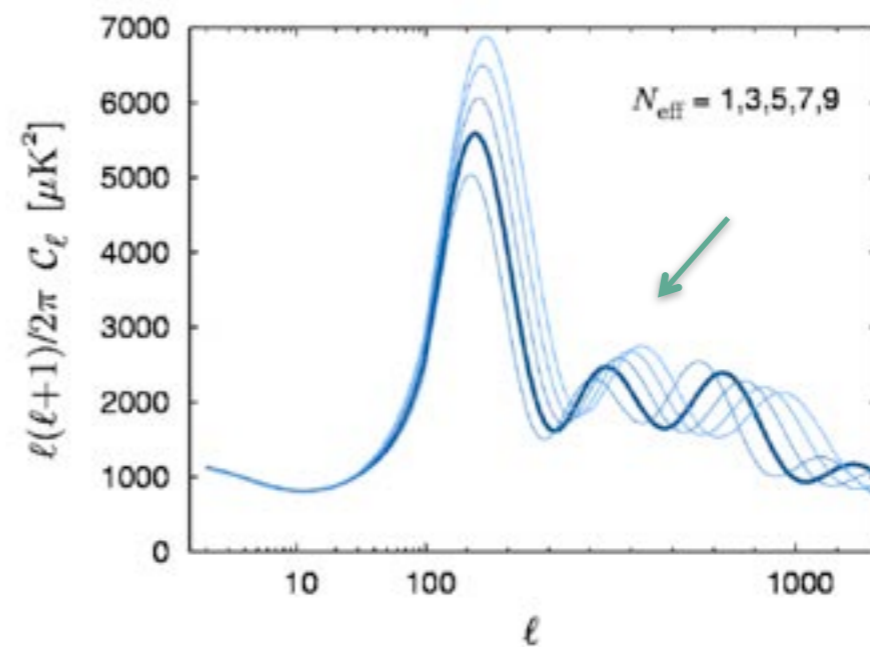
degenerate with Ω_m



Sound horizon/angular positions of the peaks degenerate with H_0 and Ω_m



Damping tail degenerate with Y_p



Anisotropic stress (partially) degenerate with A_s and n_s

1. Matter-radiation equality

$$z_{eq} \propto \frac{\omega_m}{\omega_R} \propto \frac{\omega_m}{\omega_\gamma [1 + 0.2271 N_{\text{eff}}]}$$

The equality redshift is one of the direct observables from the temperature power spectrum. The CMB data constrain z_{eq} mainly from the ratio of the first peak to the third peak.

Measuring z_{eq} essentially fixes the ratio of the energy density in matter to the energy density in radiation.

2. Sound horizon and location peaks

The sound horizon affects the angular position of the acoustic peaks via

$$\theta_s = \frac{r_s}{D_A}$$

$$r_s = \int_0^{\tau_*} d\tau' c_s(\tau')$$
 depends on the expansion and on sound speed

$$c_s \propto \frac{\bar{\epsilon}_\gamma}{\bar{\epsilon}_B}$$

D_A is the angular diameter distance to the Last SS

$$\theta_s \propto \frac{\Omega_m^{-1/2}}{\int_{a_*}^1 \frac{da}{a^2 \sqrt{\Omega_m a^{-3} + (1 - \Omega_m)}}}$$

This relation implies that while θ_s constrains the parameter combination $\Omega_m = \omega_m / h^2$ it does not constrain ω_m and h individually

4. Damping tail

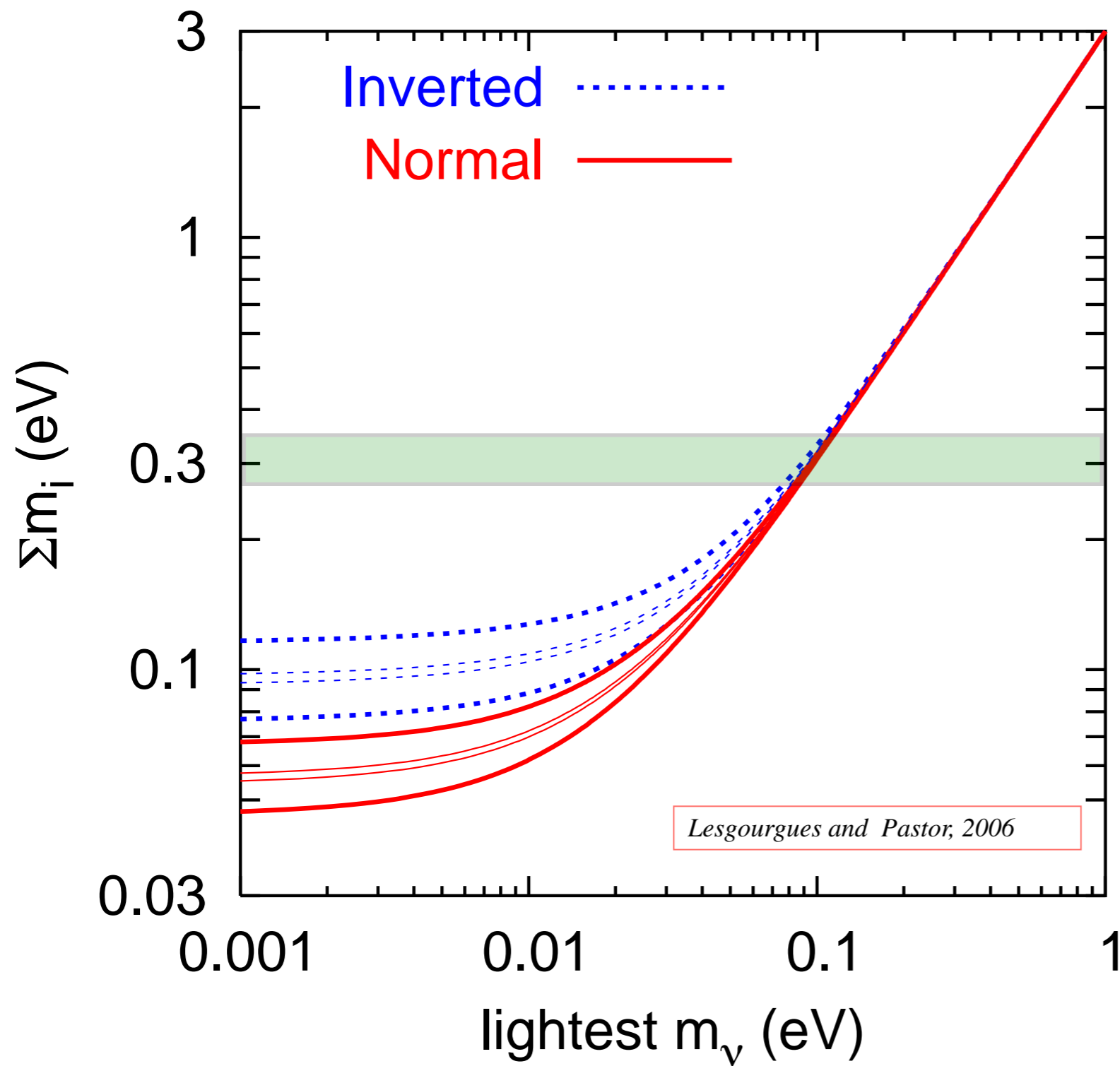
Close to recombination, the tight-coupling approximation breaks down.
Random scattering processes tend to erase perturbations below the photon diffusion length.

The envelope of the secondary peaks at large l depends on the angle $\theta_d = \lambda_d/DA$
where λ_d is the diffusion length .
Increasing the expansion rate will increase λ_d

λ_d which is controlled by the expansion history and recombination history before the decoupling. It depends essentially by free electron n_e ($\propto 1/n_e$).

An enhancing of n_e can compensate the increased expansion rate less ^4He (less recombination)
→

$$n_e = (1 - Y_p)n_B$$



Equation for the flavour evolution

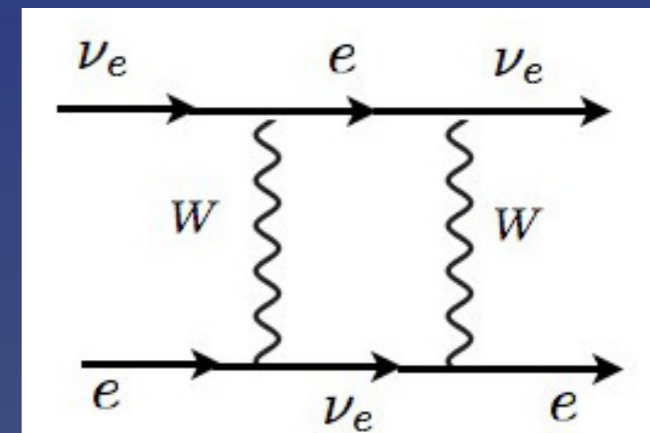
Evolution equation:

$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

$$\Omega = \Omega_{\text{vac}} + \Omega_{\text{mat}} + \Omega_{\nu-\nu}$$

MSW effect with background medium
(refractive effect) $\propto G_F$

→ 2th order term: “symmetric” matter effect
(charged lepton asymmetry subleading ($O(10^{-9})$))



Equation for the flavour evolution

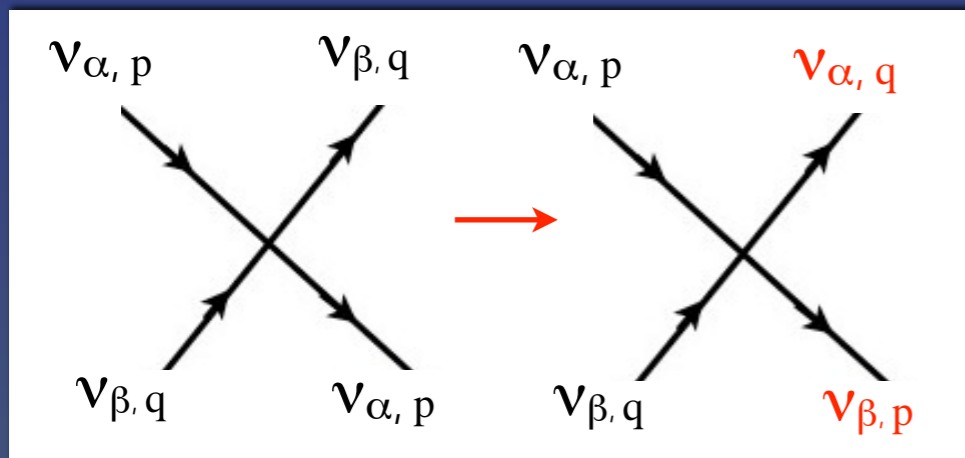
Evolution equation:

$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

$$\Omega = \Omega_{\text{vac}} + \Omega_{\text{mat}} + \underbrace{\Omega_{\nu-\nu}}_{\substack{\text{refractive } \nu-\nu \text{ term } \propto G_F \\ \text{symmetric term } \propto (\rho + \bar{\rho}) \\ \text{asymmetric term } \propto (\rho - \bar{\rho}) \\ = L}}$$

self-interactions of ν with the ν background:

off-diagonal potentials \Rightarrow non-linear EoM



The importance of multi-flavour system

Mirizzi et al 2013, arXiv1303.5368

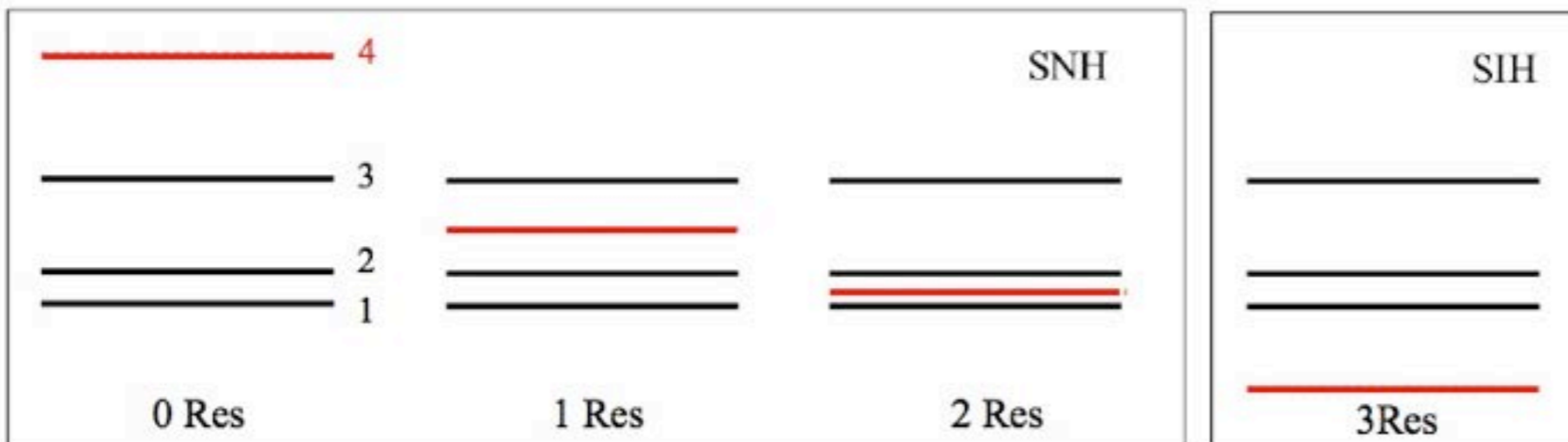
- **More mixing angles:**

- oscillation mechanism shared between different flavours → effects not possible in the simple “1+1” scenario

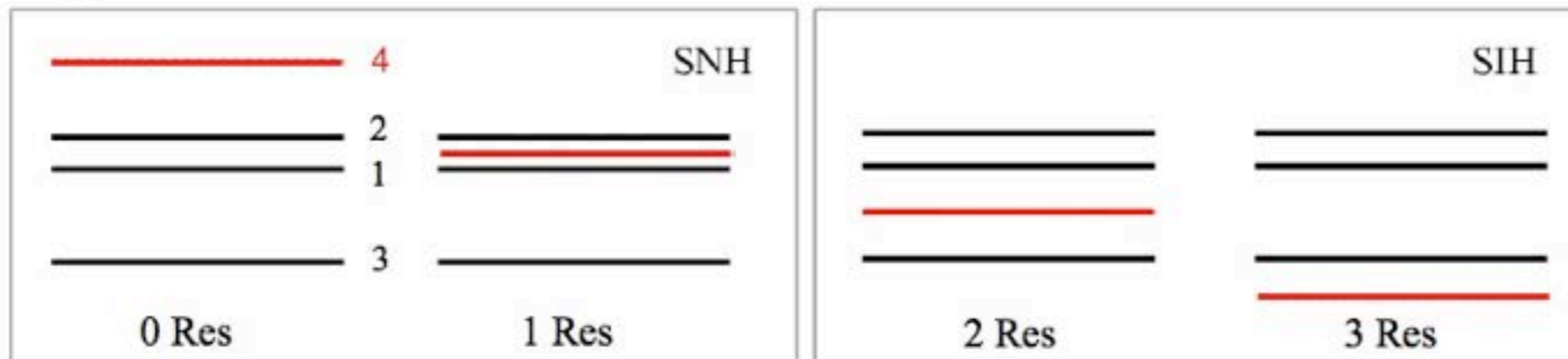
- **More resonances with the matter term, affecting the sterile neutrino production**

- When the matter term becomes of the same order of the neutrino mass-squared splitting, induce MSW-like resonances between the active and sterile states

NH

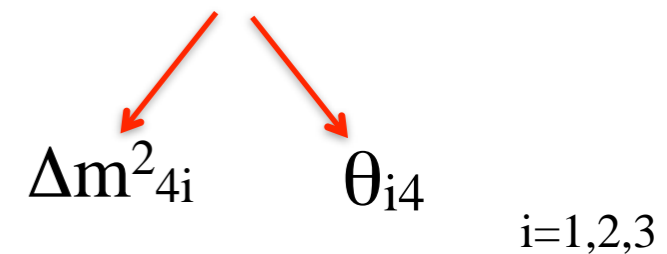


IH



In the sterile sector:

resonances associated with



Active
 NH, $\Delta m^2_{31} > 0$
 IH, $\Delta m^2_{31} < 0$

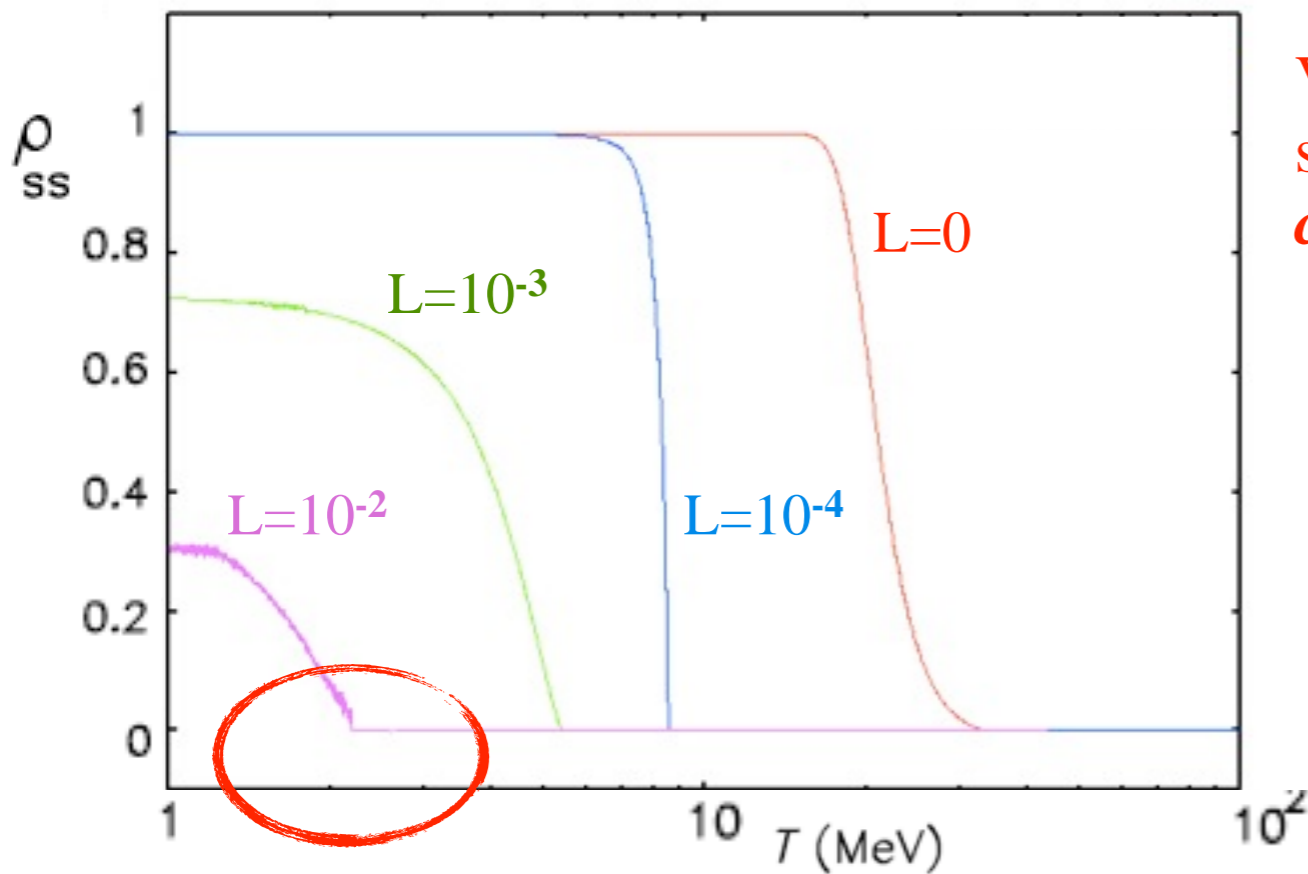
Sterile
 SNH, $\Delta m^2_{41} > 0$
 SIH, $\Delta m^2_{41} < 0$

Sterile production by neutrino asymmetry

- ✓ ρ_{ss} and distortions of ν_e spectra as function of the ν *asymmetry parameter*
 - evaluation of the cosmological consequences

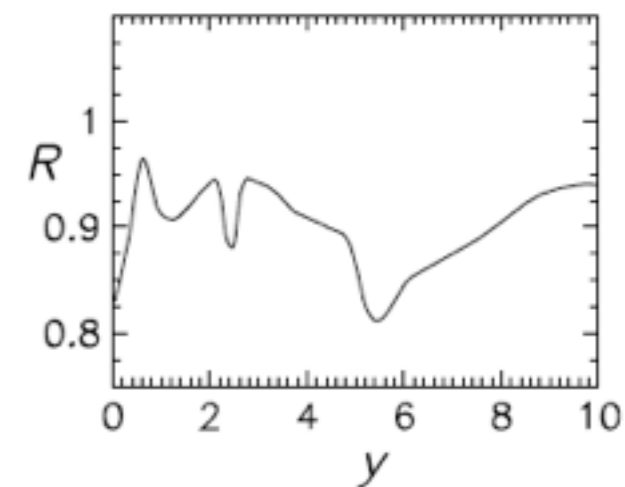
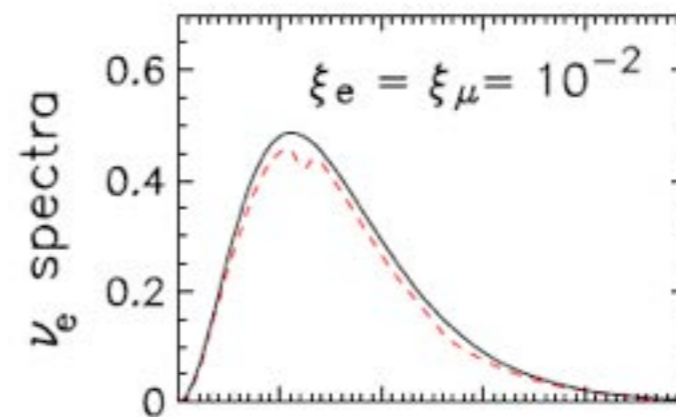
- ✗ Very challenging task, involving time consuming numerical calculations
 - few representative cases

$$L_\alpha \simeq 0.68 \xi_\alpha \left(\frac{T_\nu}{T_\gamma} \right)^3$$



Very large asymmetries are necessary to suppress the sterile neutrino abundances leading to *non trivial consequences on BBN*

→ conversions occur at $T \sim T_\nu$ decoupling
 \Rightarrow active not repopulated anymore by collisions ($\rho_{ee} < 1$)



Active-Sterile flavour evolution

$\nu_s - \nu_s$ interaction strength $G_X = \frac{\sqrt{2}}{8} \frac{g_X^2}{M_X^2}$ for $T \ll M_X$

Evolution equation:

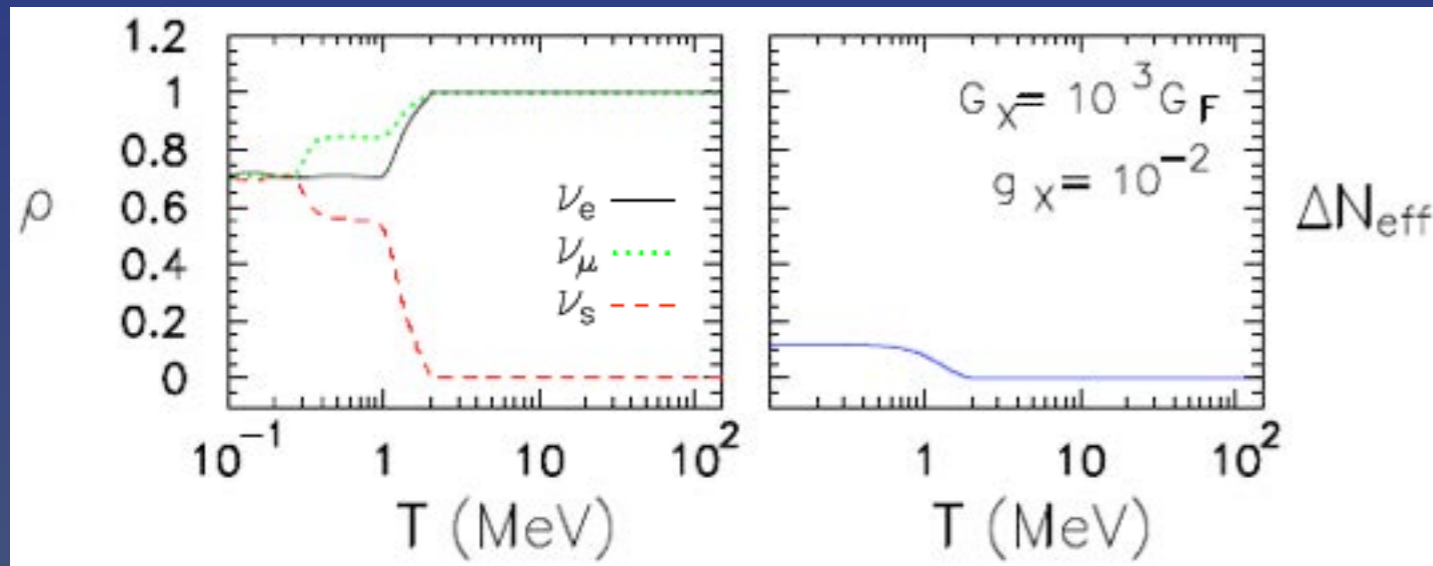
$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

$$\Omega = \Omega_{\text{vac}} + \Omega_{\text{mat}} + \Omega_{\nu-\nu} + \Omega_{\nu_s-\nu_s}^{\text{secr}}$$

$\swarrow \propto G_F$ $\swarrow \propto G_X$

$$C = C_{\text{SM}} + C_{\text{secr}}$$

$\swarrow \propto G_F^2$ $\swarrow \propto G_X^2$



primordial ^2H yield

