



Constraining CKM γ angle at LHCb

Alexis Vallier (LAL, Orsay)
on behalf of the **LHCb collaboration**



2015
Conferences

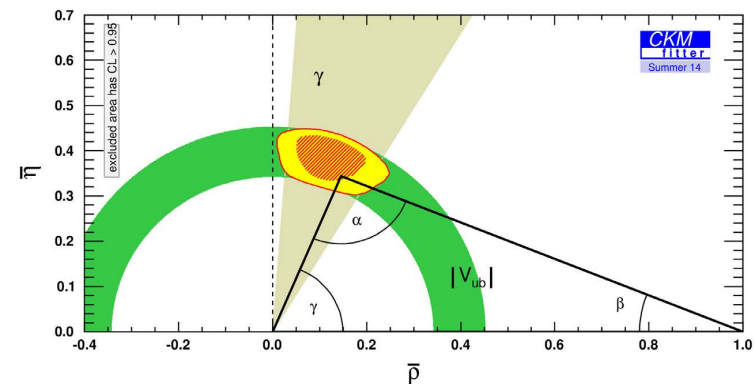
March 14th - 28th
La Thuile, Aosta Valley - Italy

γ a standard candle to probe new physics

- The only angle measurable from **tree only processes**.
- **Theoretically clean** : $\delta\gamma/\gamma \lesssim \mathcal{O}(10^{-7})$
[JHEP 1401(2014)051]
- γ is the **least known CKM angle**.
- **Direct measurements**:
 - BaBar: $(69_{-16}^{+17})^\circ$ [PRD 87(2013)052015]
 - Belle: $(68_{-14}^{+15})^\circ$ [arXiv:1301.2033]
 - LHCb: $(73_{-10}^{+9})^\circ$ [LHCb-CONF-2014-004]

$$\gamma \equiv \arg \left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$

With only “Tree” quantities



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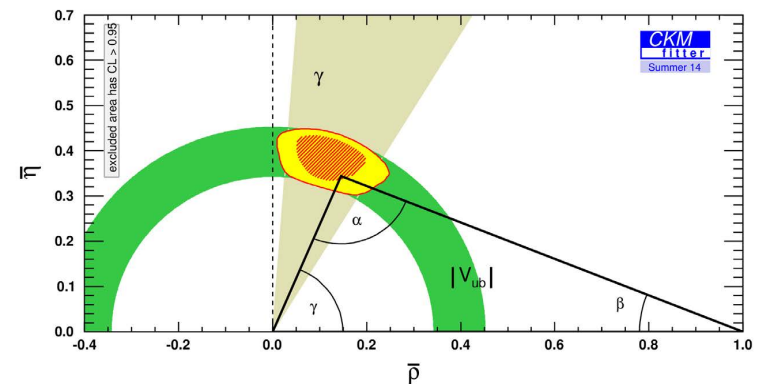
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- **Indirect measurements** (dominated by loops):

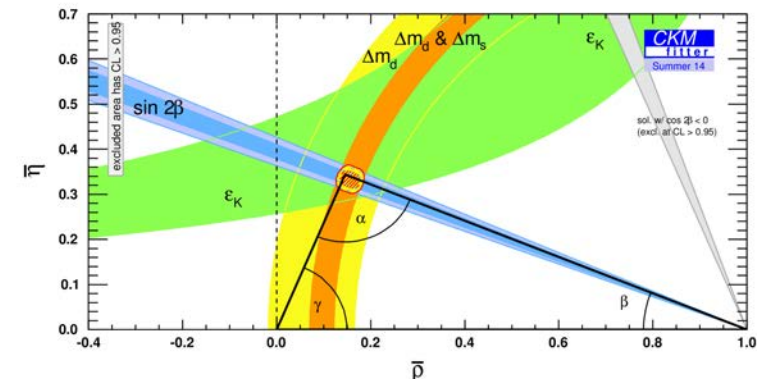
- CKMFitter: $(66.9_{-3.7}^{+1.0})^\circ$ (global fit w/o γ meas.)

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With only “Tree” quantities



With only “Loop” quantities

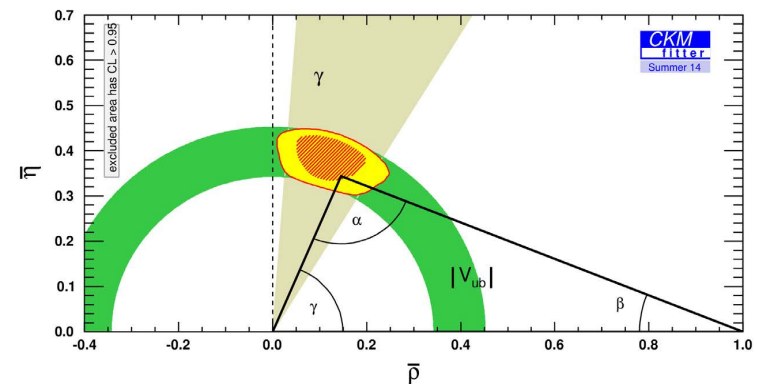


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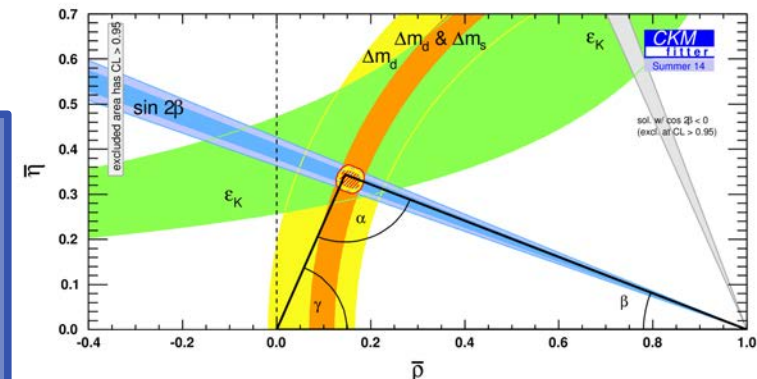
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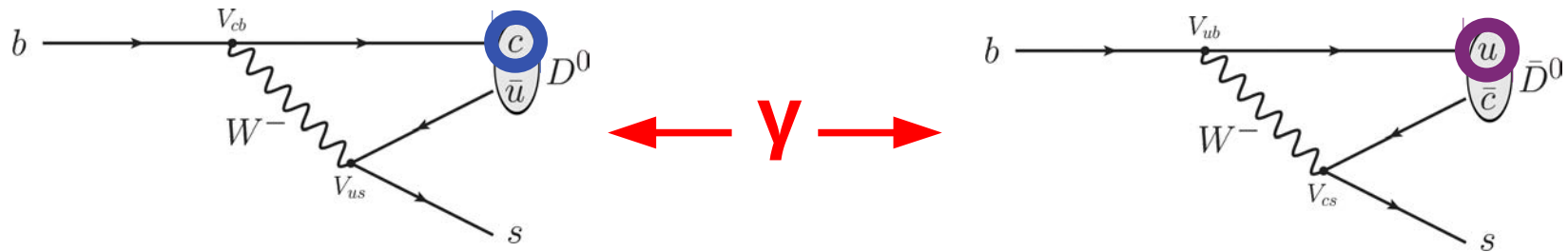
With only “Loop” quantities



Goal: highlight or discard tension between direct and indirect measurements.
Need better precision from direct measurements.

γ from time independent measurement

- Interference between $b \rightarrow \bar{c}u\bar{s}$ and $b \rightarrow u\bar{c}s$: sensitive to weak phase γ .



- Several D decays are used:

- Counting analysis:

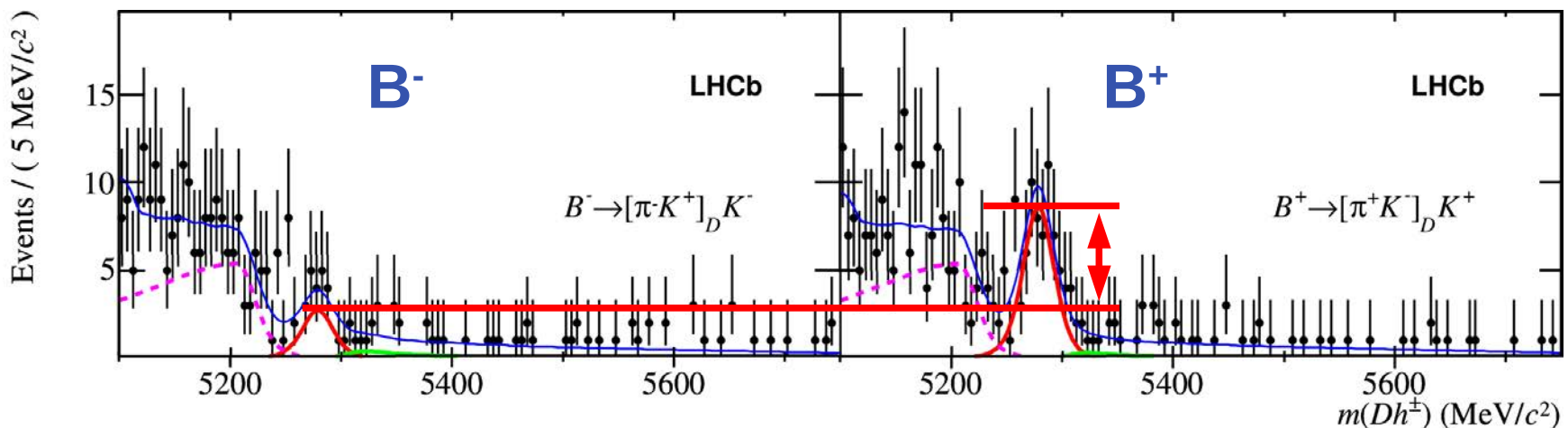
- **GLW**: CP eigenstates (e.g. $D \rightarrow KK$) [1,2]
- **ADS**: flavoured states (e.g. $D \rightarrow K\pi$) [3-5]
- **GLS**: singly Cabibbo suppressed (e.g. $D \rightarrow K_S^0 K\pi$) [6]

} Decay width asymmetries and ratios

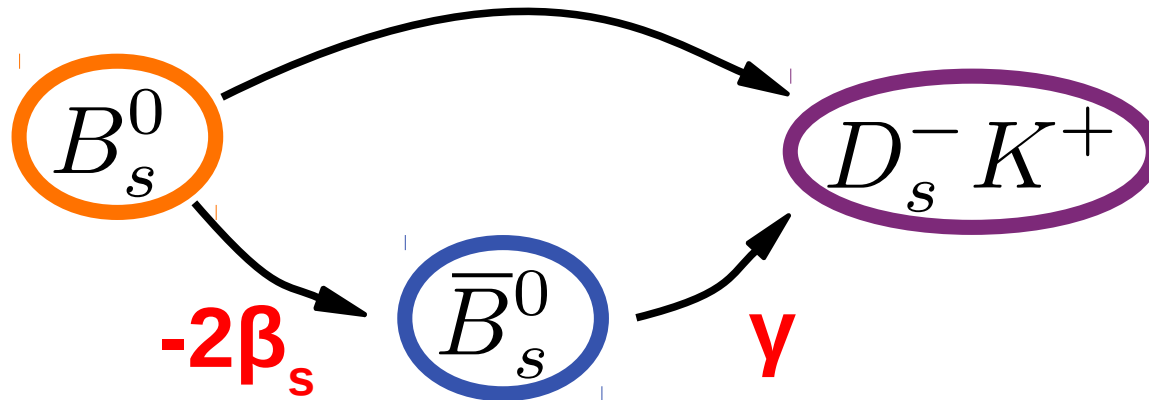
- Amplitude analysis:

- **GGSZ**: 3-body CP conjugate states (e.g. $D \rightarrow K_S^0 \pi\pi$) [7,8]

} Dalitz plot distributions



Time dependent measurement with $B_s^0 \rightarrow D_s^- K^+$



- CP violation in the **mixing and decay**.
- Same tree level process as presented previously.
- **Time dependent** measurement.
- **Measure $(\gamma-2\beta_s)$**
- Assume $\Phi_s = -2\beta_s$ and use as external input the Φ_s measurement from $B_s^0 \rightarrow J/\psi\Phi$ (much better precision).

Inputs for LHCb γ combination

- Two combinations:
 - **Robust:** $B \rightarrow DK$ -like and **Full:** $B \rightarrow DK$ -like and $B \rightarrow D\pi$ [LHCb-CONF-2014-004]
- Measurements included in the combination:
 - $B^+ \rightarrow Dh^+$, $D \rightarrow hh$, GLW/ADS, 1 fb^{-1} [Phys. Lett. B712 (2012) 203]
 - $B^+ \rightarrow Dh^+$, $D \rightarrow K\pi\pi\pi$, ADS, 1 fb^{-1} [Phys. Lett. B723 (2013) 44]
 - $B^+ \rightarrow DK^+$, $D \rightarrow K_s^0 hh$, model independent GGSZ, 3 fb^{-1} [JHEP 10 (2014) 097]
 - $B^+ \rightarrow DK^+$, $D \rightarrow K_s^0 K\pi$, GLS, 3 fb^{-1} [Phys. Lett. B733 (2014) 36]
 - $B^0 \rightarrow DK^{*0}$, $D \rightarrow hh$, GLW/ADS, 3 fb^{-1} [Phys. Rev. D90 (2014) 112002]
 - $B_s^0 \rightarrow D_s^\mp K^\pm$, time-dependent, 1 fb^{-1} [JHEP 11 (2014) 060]
- All these modes have a **limited statistics**:
 - **Branching ratio** $\sim 10^{-7}$, some final states with K_s^0 (hard to reconstruct)

➡ The γ measurement power comes from the **combination**

Inputs for LHCb γ combination

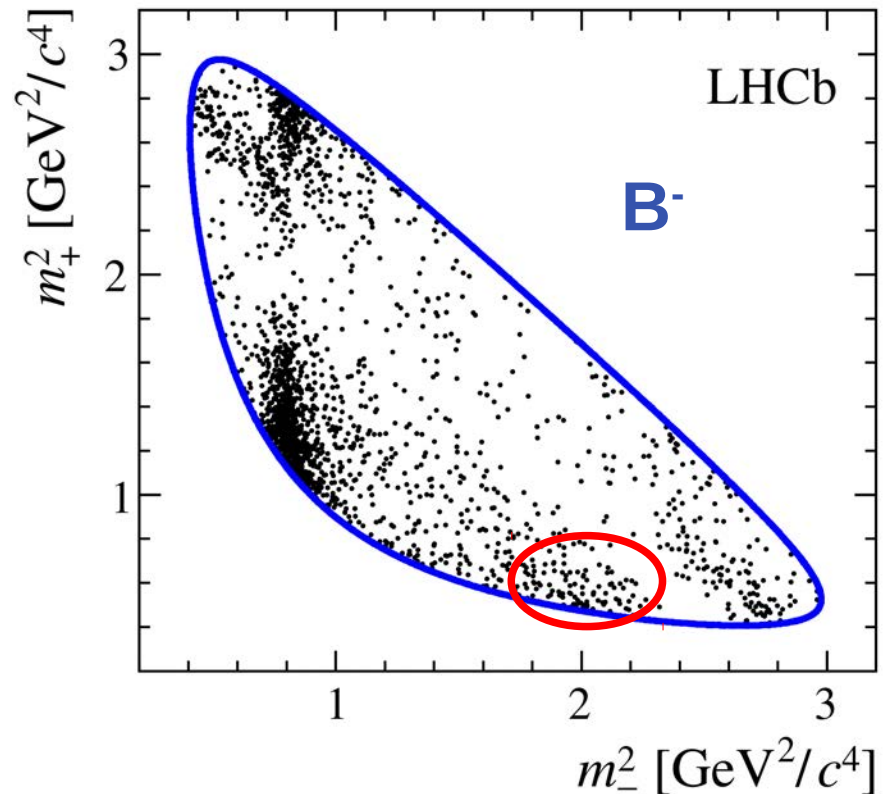
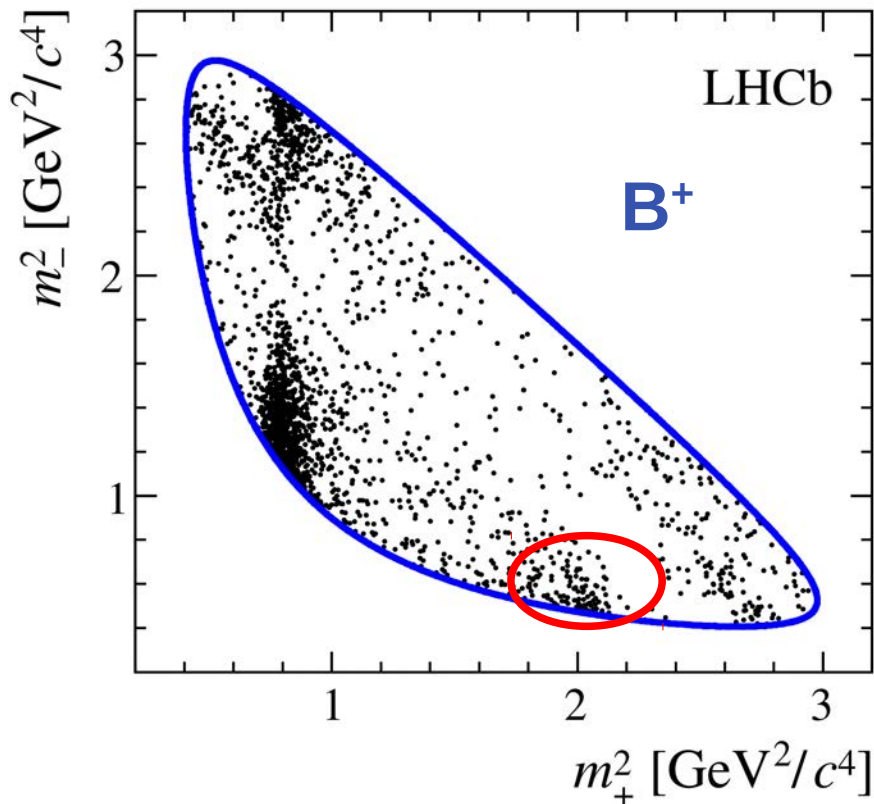
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Briefly present
these two
measurements

➡ The γ measurement power comes from the **combination**

$B^\pm \rightarrow DK^\pm$ GGSZ

[JHEP 10 (2014) 097]



- Use $B \rightarrow DK$ with: $D \rightarrow K_S^0 \pi^+ \pi^-$ and $D \rightarrow K_S^0 K^+ K^-$
- Dalitz plot made with: $m_\pm^2 \equiv m^2(K_S^0 h^\pm)$
- **World most precise single γ measurement:**

$$\gamma = (62_{-14}^{+15})^\circ$$

γ with $B_s^0 \rightarrow D_s K^\pm$

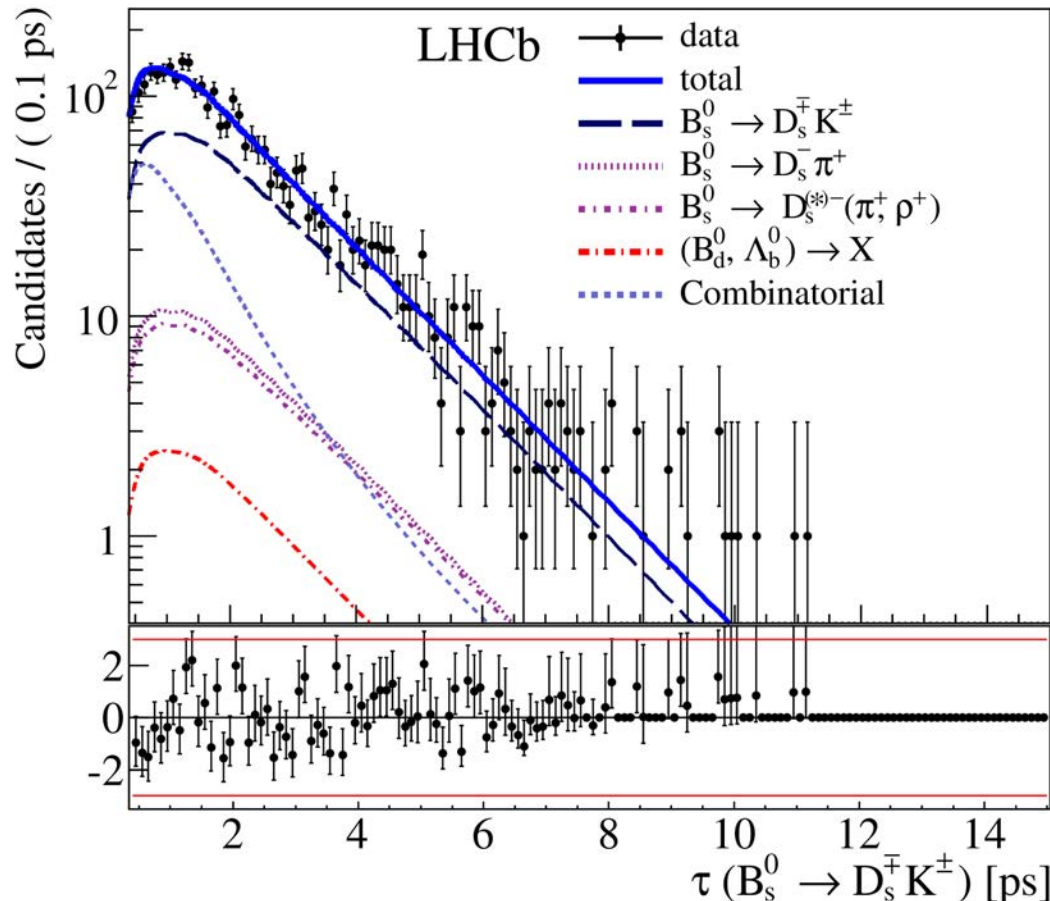
[JHEP 11 (2014) 060]

Time dependent tagged decay rate:

$$\frac{d\Gamma_{B_s^0 \rightarrow f}(t)}{dt e^{-\Gamma_s t}} = \frac{1}{2} |A_f|^2 (1 + |\lambda_f|^2) \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + D_f \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) + C_f \cos(\Delta m_s t) - S_f \sin(\Delta m_s t) \right]$$

$$D_f \propto \cos(\delta - (\gamma - 2\beta_s))$$

$$S_f \propto \sin(\delta - (\gamma - 2\beta_s))$$



- Assumes $-2\beta_s \approx \phi_s$
- Take LHCb Φ_s meas. (1fb^{-1})
[Phys. Rev. D77 (2008) 112010]
- World first measurement with this technique!

$$\gamma = (115_{-43}^{+28})^\circ$$

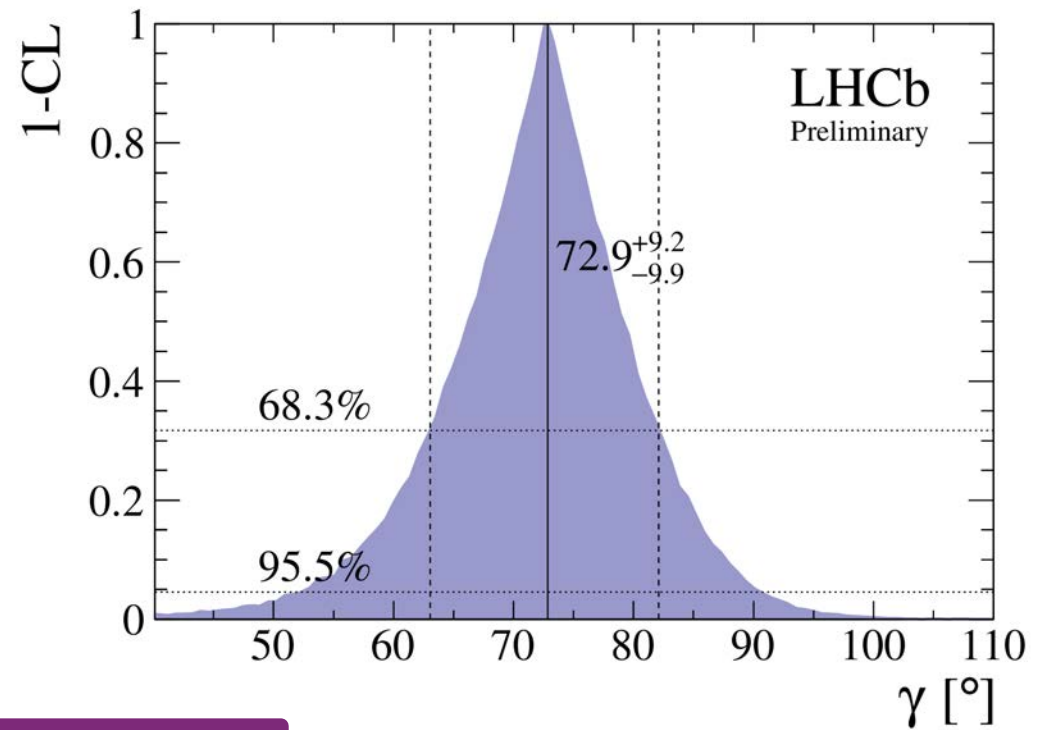
- To be updated with full Run 1 dataset (add 2012 data).

Result of LHCb γ combination

[LHCb-CONF-2014-004]

- Frequentist combination.
- Takes into account D mixing.
- Auxiliary inputs for some hadronic parameters (HFAG, CLEO).
- Bayesian cross-check in good agreement.
- Reaching the 10° precision:

Robust: only $B \rightarrow DK$ like

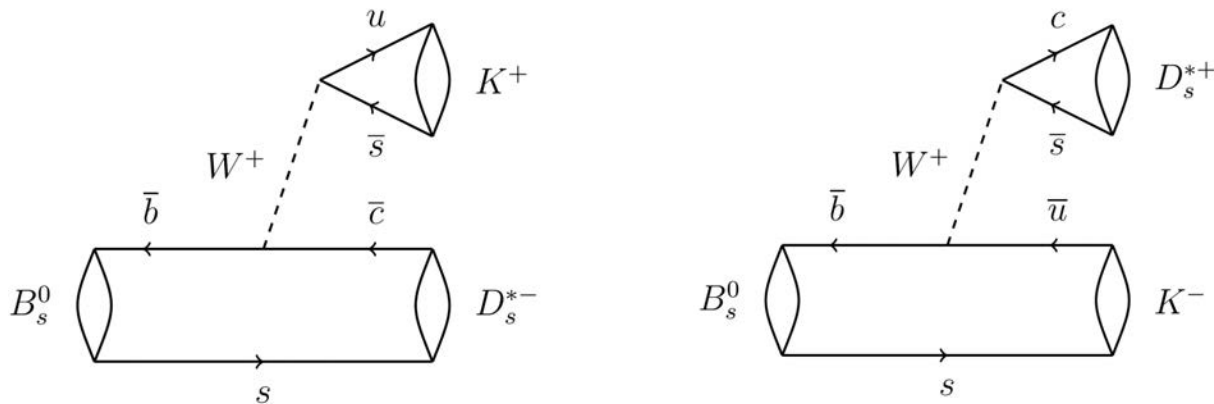


$$\gamma = (73^{+9}_{-10})^\circ$$

First observation of $B_s^0 \rightarrow D_s^* K^\pm$

[LHCb-PAPER-2015-008, to be submitted]

NEW



Channel sensitive to angle γ like $B_s^0 \rightarrow D_s K$

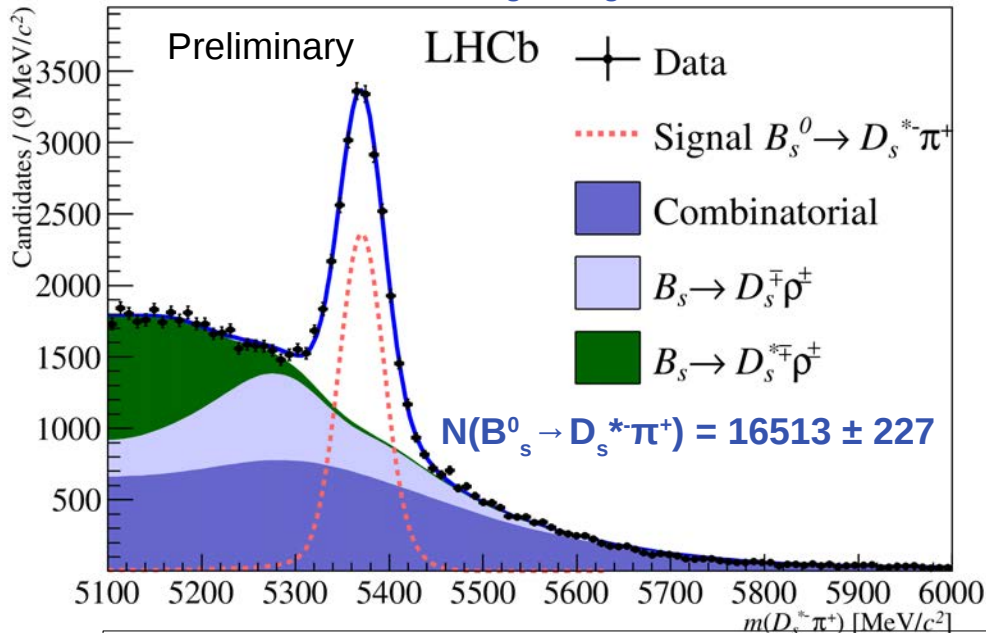
- Has **never been observed** before.
- D_s^* reconstructed with $D_s^* \rightarrow D_s(KK\pi)\gamma$
 - **Soft photon** \rightarrow challenge with LHCb!
- **Branching ratio** as a first step (full Run1 data set) :

$$\mathcal{R}^* \equiv \frac{\mathcal{B}(B_s^0 \rightarrow D_s^{*\mp} K^\pm)}{\mathcal{B}(B_s^0 \rightarrow D_s^{*-} \pi^+)} = \frac{N_{K^\pm} \varepsilon_{\pi^+}}{N_{\pi^+} \varepsilon_{K^\pm}}$$

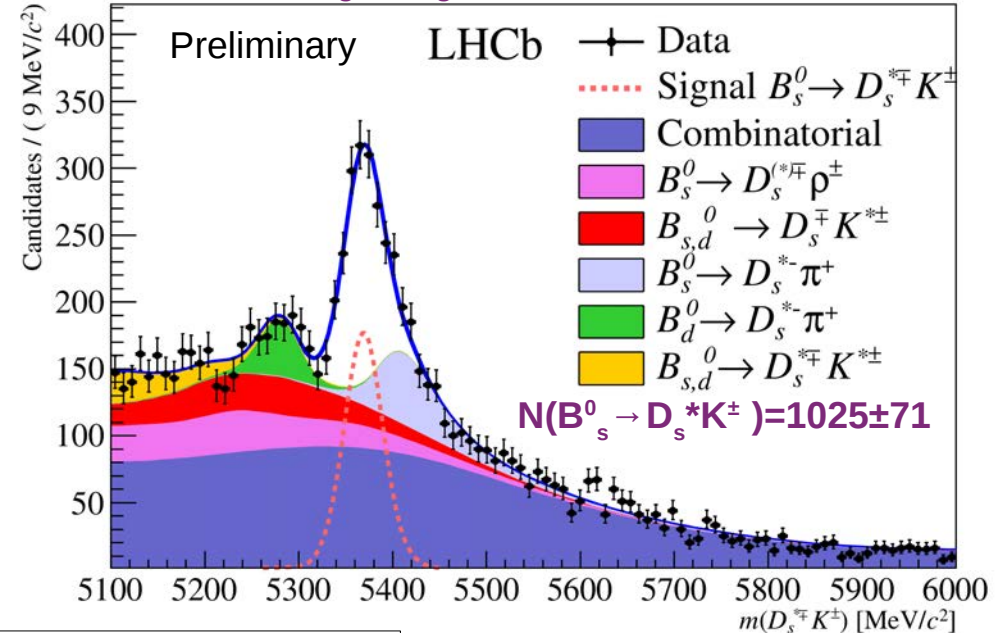
First observation of $B_s^0 \rightarrow D_s^* K^\pm$

[LHCb-PAPER-2015-008]

Normalisation: $B_s^0 \rightarrow D_s^* \pi^\pm$



Signal: $B_s^0 \rightarrow D_s^* K^\pm$



On the same dataset: $N(B_s^0 \rightarrow D_s^* K^\pm) = 5101 \pm 100$ [arXiv:1412.7653]

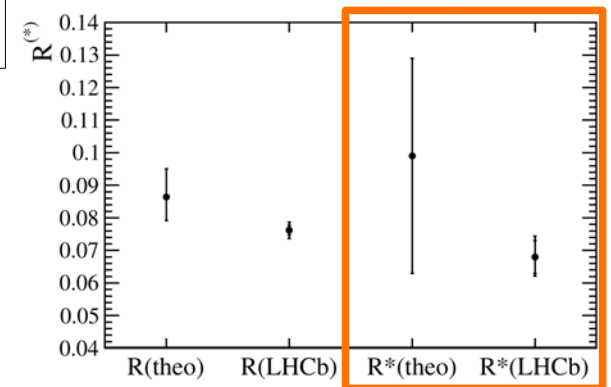
- Branching fraction ratio:

$$\mathcal{R}^* = 0.068 \pm 0.005 \text{ (stat.) } \begin{matrix} +0.004 \\ -0.003 \end{matrix} \text{ (sys.)} \quad \text{Preliminary}$$

mainly combi. Background uncert.

- With $B(B_s^0 \rightarrow D_s^* \pi^\pm)$ from Belle:

$$\mathcal{B}(B_s^0 \rightarrow D_s^* K^\pm) = 16.3 \pm 1.2 \text{ (stat.) } \begin{matrix} +1.0 \\ -0.7 \end{matrix} \text{ (sys.) } \pm 4.8 \text{ (bf)} \times 10^{-5}$$



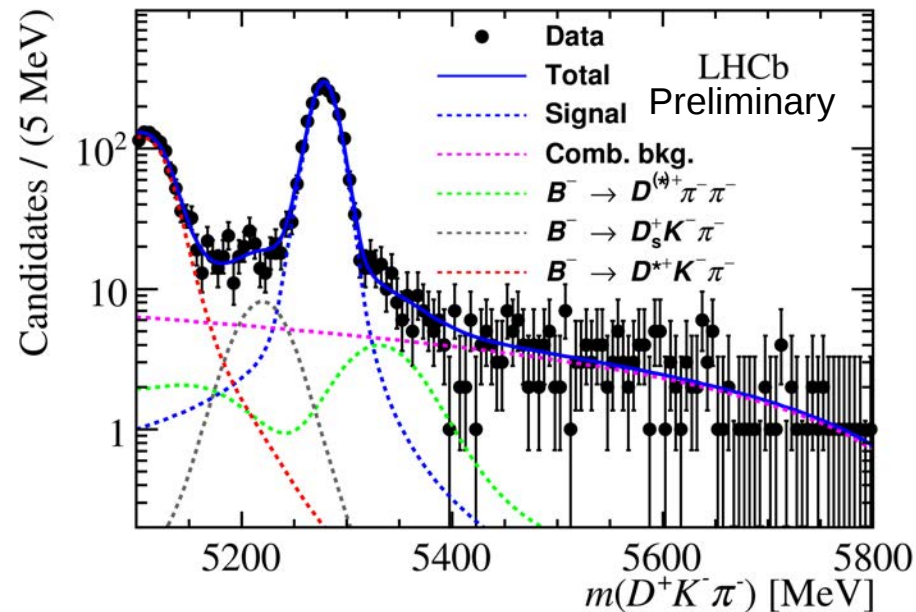
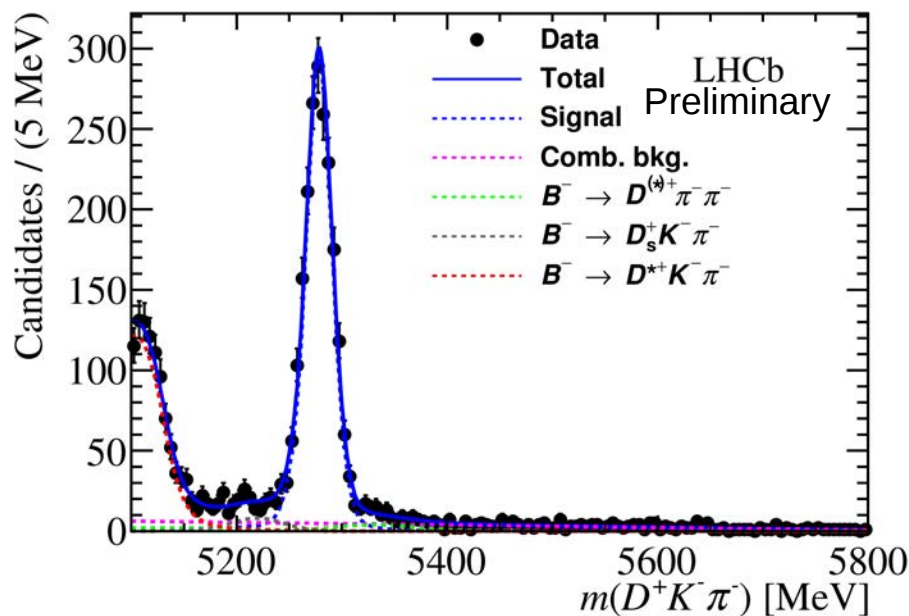
Preliminary

First observation of $B^- \rightarrow D^+ K^- \pi^-$

[LHCb-PAPER-2015-007, arXiv:1503.02995, submitted to PRD]

Subm.
Last week

- $B^- \rightarrow D^+ K^- \pi^-$ interesting for:
 - **Properties of neutral D^{**} states** measurement (spin-parity).
 - Determine **potential for γ** measurement with $B^- \rightarrow D^{**} K^-$ (measure interf. magnitude r_B).
- **First observation of the decay:** ~ 2000 signal candidates (60σ)



- Normalised to $B^- \rightarrow D^+ \pi^- \pi^-$ (PDG value) :

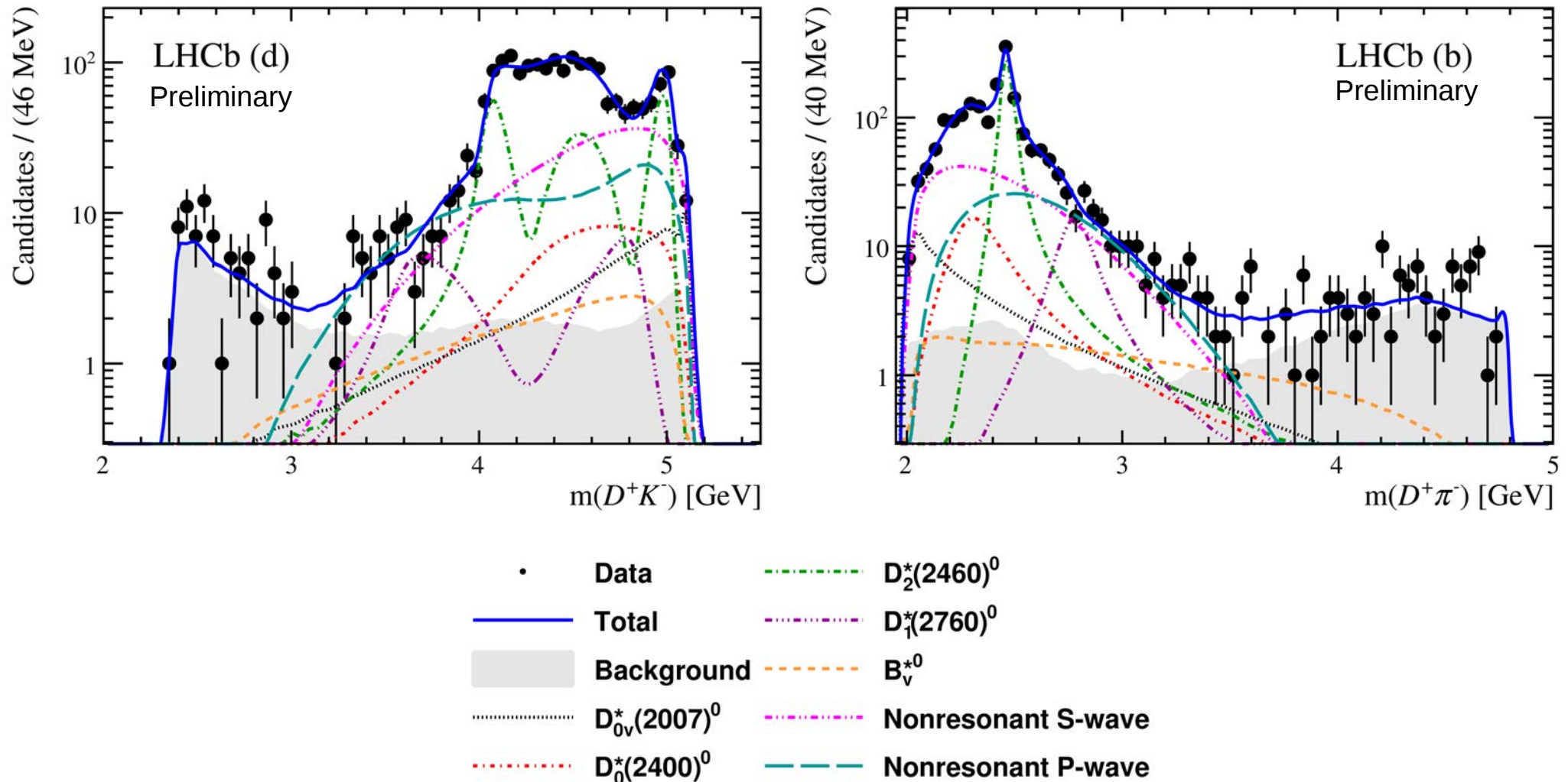
$$\mathcal{B}(B^- \rightarrow D^+ K^- \pi^-) = (7.92 \pm 0.23 \pm 0.24 \pm 0.42) \times 10^{-5} \quad \text{Preliminary}$$

stat. syst. normalisation

Dalitz Plot of $B^- \rightarrow D^+ K^- \pi^-$

[LHCb-PAPER-2015-007, arXiv:1503.02995]

- A Dalitz plot model is determined with an isobar approach (coherent sum of resonant and non-resonant amplitudes)



Results of $B^- \rightarrow D^+ K^- \pi^-$ Amplitude Analysis

[LHCb-PAPER-2015-007, arXiv:1503.02995]

- $D_J^*(2760)^0$ determined to have **spin 1**: $D_1^*(2760)^0$
- Masses and widths of $D_2^*(2460)^0$ and $D_1^*(2760)^0$ reported:

$m(D_2^*(2460)^0)$	$=$	$(2464.0 \pm 1.4 \pm 0.5 \pm 0.2)$ MeV	} Good agreement with PDG
$\Gamma(D_2^*(2460)^0)$	$=$	$(43.8 \pm 2.9 \pm 1.7 \pm 0.6)$ MeV	
$m(D_1^*(2760)^0)$	$=$	$(2781 \pm 18 \pm 11 \pm 6)$ MeV	} Good agreement with prev. meas.*
$\Gamma(D_1^*(2760)^0)$	$=$	$(177 \pm 32 \pm 20 \pm 7)$ MeV	
Preliminary		stat. syst. Dalitz model	} Larger than prev. meas.* by $\sim 3\sigma$

- **Can be used in the future for γ measurement.**
- **Improved knowledge of D^{**} states useful for other Dalitz analyses.**
 - For instance $B^0 \rightarrow D^0 K^+ \pi^-$ is promising for a γ measurement.

[PRD 80 (2009) 092002, arXiv:0909.1495]

* BaBar PRD 82 (2010) 111101 and LHCb JHEP 09 (2013) 145.

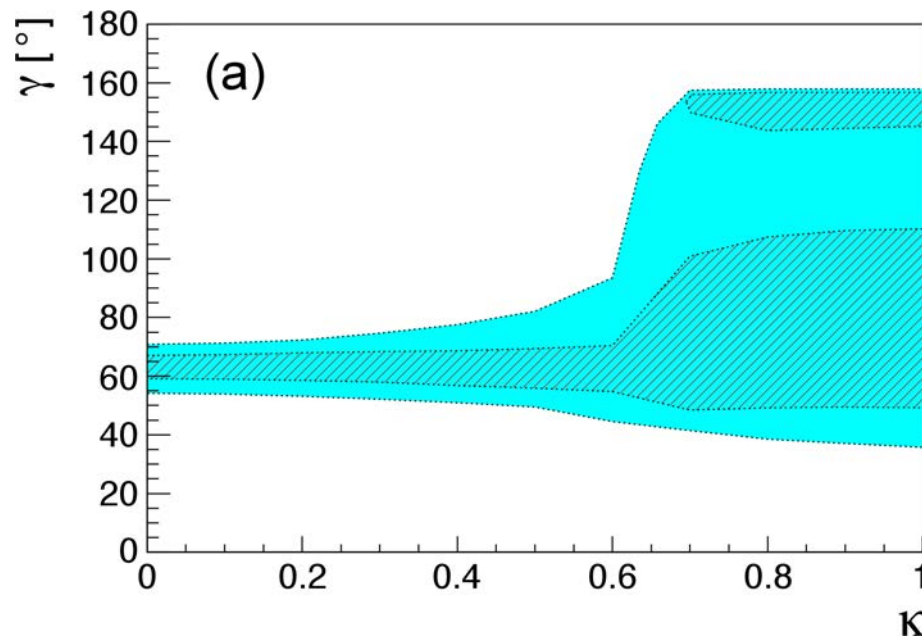
γ from charmless B decays

[Phys. Lett. B 741 (2015) 1-11]

- Combine CP violation time dependent measurements of :

$B^0 \rightarrow \pi^+\pi^-$, $B^0_s \rightarrow K^+K^-$, $B^0 \rightarrow \pi^0\pi^0$ and $B^+ \rightarrow \pi^+\pi^0$. Suggested by [9-13]

- Sensitive to penguin diagrams contributions.
- Exploits isospin and U-spin ($d \leftrightarrow s$) symmetries.
- Bayesian analysis with floating maximal magnitude of U-spin breaking (κ).



- Assuming up to 50% of U-spin symmetry breaking:

$$\gamma = \left(63.5^{+7.2}_{-6.7}\right)^\circ$$

- Measurement **compatible** and **competitive** with the one obtained from **tree decays**.
- However need better theoretical understanding of U-spin breaking.**

Conclusion and Outlook

- The LHCb experiment has reached the **10° precision** on the CKM angle γ :

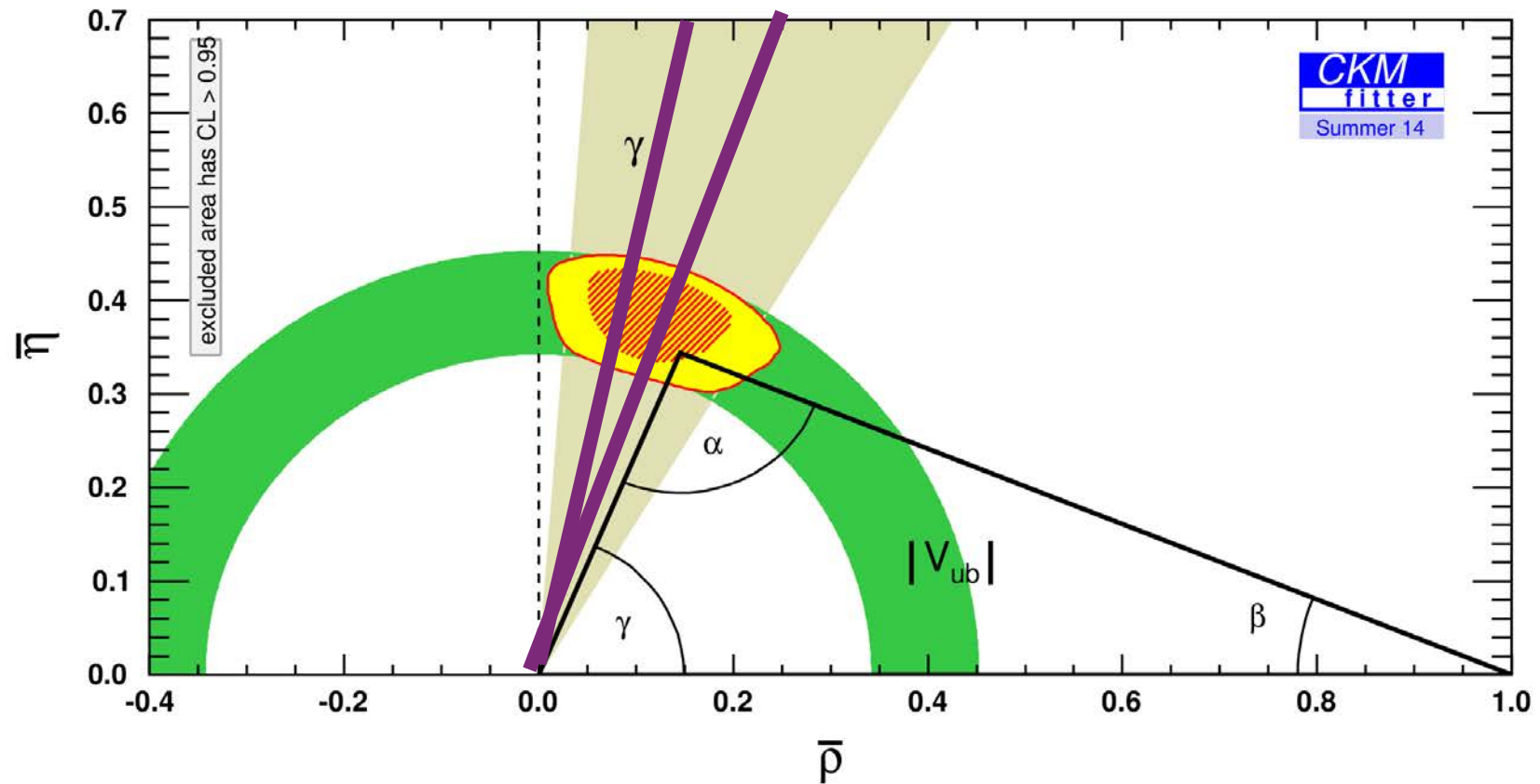
$$\gamma = (73_{-10}^{+9})^\circ$$

[LHCb-CONF-2014-004]



- **Large room for improvement:**
 - The current combination still includes some measurement with only 2011 Data.
 - We will add extra decay channels (with B^0 , new Dalitz analyses, and photon and π^0 in final states).
- **On the track to reach the 4° precision by 2018!**

Conclusion and Outlook



- On the track to reach the 4° precision by 2018!

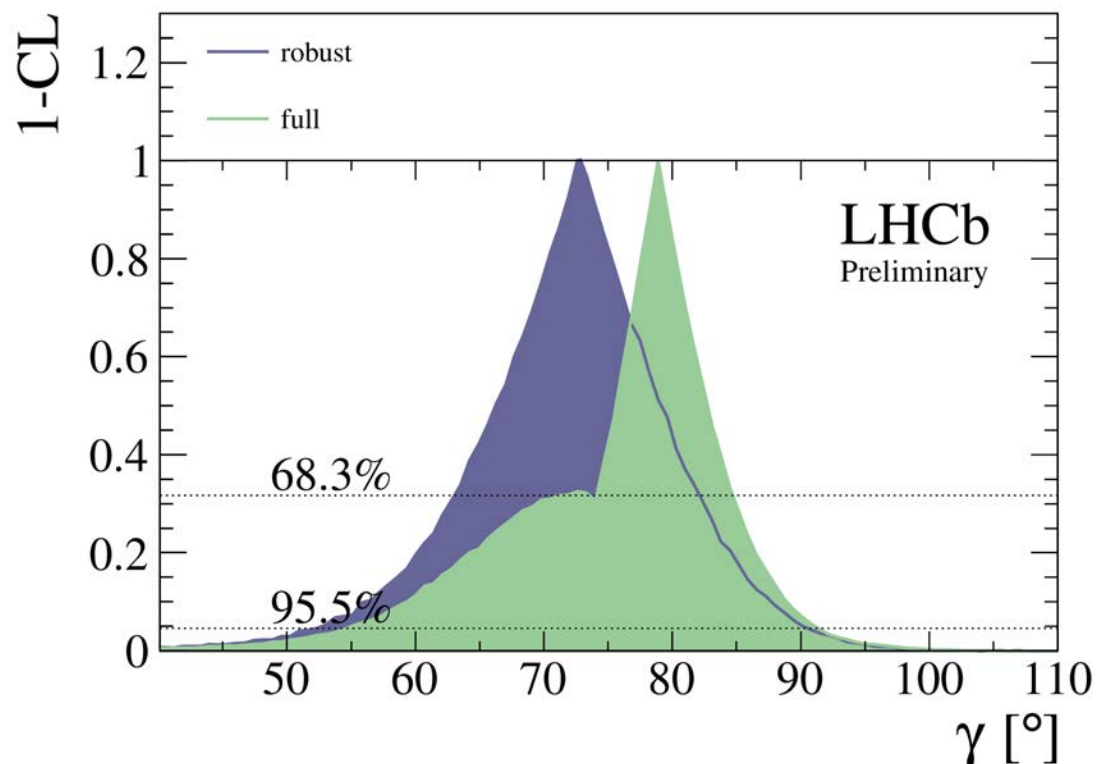
BACKUP

LHCb γ combination – Adding $B \rightarrow D\pi$

- **$B \rightarrow D\pi$ less sensitive to γ .**
 - Interference much smaller.
 - $r_B^{D\pi} \sim r_B^{DK}/15$.
- **$B \rightarrow D\pi$ data sample 10x larger.**
- Full combination:
 - Sharp max at $\gamma = 78.9^\circ$
 - Secondary max \sim Robust max
 - Unexpected large value of $r_B^{D\pi}$ (0.027 instead of ~ 0.006)
- 95% Confidence level intervals agree between both combination:

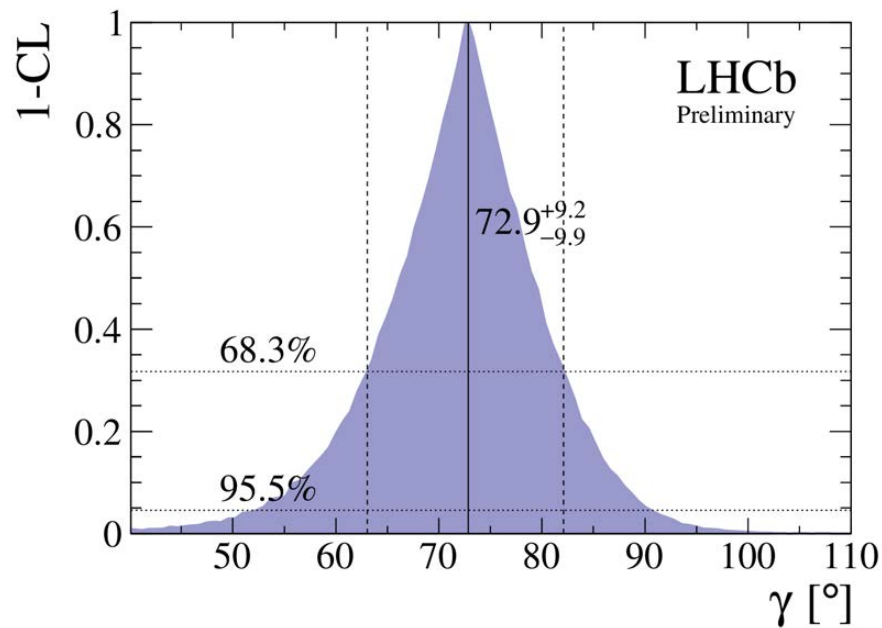
robust	$\gamma \in [52.0, 90.5](^\circ)$
full	$\gamma \in [54.6, 91.4](^\circ)$

Robust: only $B \rightarrow DK$ like
Full: add $B \rightarrow D\pi$

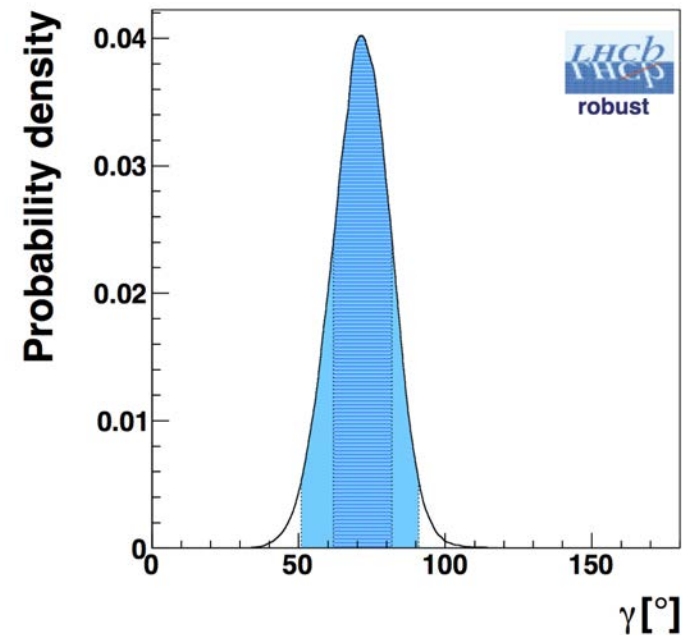


LHCb γ combination – Bayesian interpretation

Frequentist combination



Bayesian combination



	Central value	68% Interval
Frequentist γ combination ($^\circ$)	72.9	[63.0, 82.1]
Bayesian γ combination ($^\circ$)	71.9	[61.9, 81.8]

γ from time independent measurement- References

- [1] M. Gronau and D. London, PLB 253 (1991) 483
- [2] M. Gronau and D. Wyler PLB 265 (1991) 172
- [3] D. Atwood and I. Dunietz and A. Soni, PRL 78 (1997) 3257
- [4] D. Atwood, I. Dunietz and A. Soni, PRD 63 (2001) 036005
- [5] D. Atwood and A. Soni, PRD 68 (2003) 033003
- [6] Y. Grossman, Z. Ligeti and A. Soffer, PRD 67 (2003) 071301
- [7] A. Giri, Y. Grossman, A. Soffer and J. Zupan, PRD 68 (2003) 054018
- [8] A. Bondar, Proceedings of BINP special analysis meeting on Dalitz analysis, 2002, unpublished

γ from charmless B decays - Parametrisation

- Express CP asymmetries and BR as a function of weak and hadronic param. :

Observable:
Asymmetry
Branching Ratio

$$O = f \left(\beta, \gamma, \underbrace{|D|, d, \vartheta, q, \vartheta_q}_{B^0 \rightarrow \pi^+ \pi^-, B^0 \rightarrow \pi^0 \pi^0, B^+ \rightarrow \pi^+ \pi^0}, \underbrace{|D'|, d', \vartheta'}_{B_s^0 \rightarrow K^+ K^-} \right)$$

$\sin(2\beta) = 0.682 \pm 0.019$ (HFAG)

- Take into account non factorizable U-spin breaking correction:

$$|D'| = \underbrace{\left| \frac{D'}{D} \right|_{\text{fact}}}_{1.41^{+0.20}_{-0.11}} |D| |1 + r_D e^{i\vartheta_{r_D}}|$$

(QCD sum rules*)

$$d' e^{i\vartheta'} = d e^{i\vartheta} \frac{1 + r_G e^{i\vartheta_{r_G}}}{1 + r_D e^{i\vartheta_{r_D}}}$$

- Use flat priors:

Quantity	Prior range
d	[0, 20]
ϑ	[-180°, 180°]
q	[0, 20]
ϑ_q	[-180°, 180°]
r_D	[0, κ]
ϑ_{r_D}	[-180°, 180°]
r_G	[0, κ]
ϑ_{r_G}	[-180°, 180°]
γ (analysis C only)	[-180°, 180°]

* [PRD78 (2008) 054015]

γ from charmless B decays - References

[9] R. Fleischer, Phys. Lett. B 459 (1999) 306, arXiv:hep-ph/9903456

[10] R. Fleischer, Eur. Phys. J. C 52 (2007) 267, arXiv:0705.1121

[11] R. Fleischer, R. Knegjens, Eur. Phys. J. C 71 (2011) 1532, arXiv:1011.1096

[12] M. Ciuchini, E. Franco, S. Mishima, L. Silvestrini, JHEP 1210 (2012) 029, arXiv:1205.4948

[13] M. Gronau, D. London, Phys. Rev. Lett. 65 (1990) 3381