

# SO(10) unification at next-to-leading order

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# Proton decay: theoretical uncertainties vs experiment

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- grand unified theories (GUTs) predict baryon number violation
- non-SUSY GUTs: “golden” channel for proton decay:  
 $p \rightarrow \pi^0 e^+$
- recent experimental limit  
[Super-Kamiokande, S.Mine talk]  
 $\tau(p \rightarrow \pi^0 e^+) \geq 1.4 \times 10^{34} \text{ y}$
- new experiments planned to reach up to  $\tau(p \rightarrow \pi^0 e^+) \geq 1 \times 10^{35} \text{ y}$   
[Hyper-Kamiokande, S.Mine talk]

**What about the theory side?**

$\text{Log}_{10} \tau(p \rightarrow \pi^0 e^+) [\text{y}]$

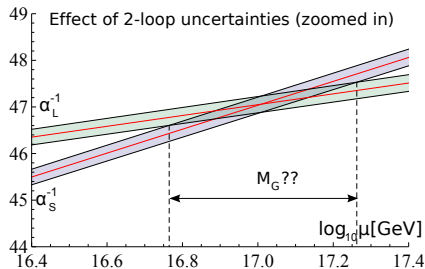
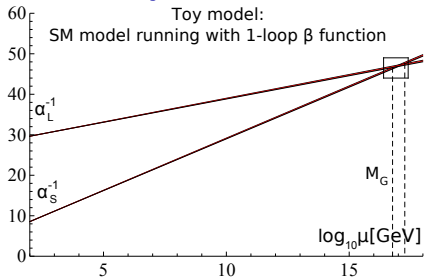
39  
38  
37  
36  
35  
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HK (10 years):  $\tau_p > 1 \times 10^{35} \text{ y}$

Recent SK limit:  $\tau_p > 1.4 \times 10^{34} \text{ y}$

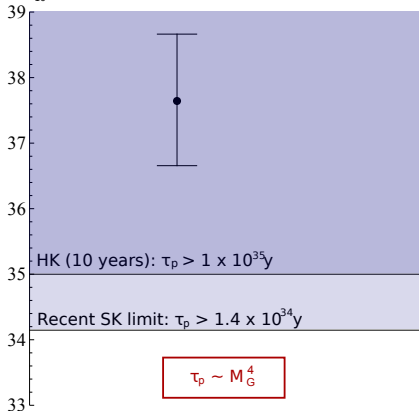


# Proton decay: theoretical uncertainties vs experiment

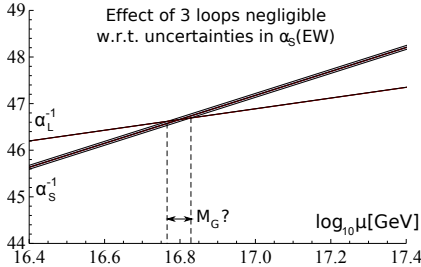
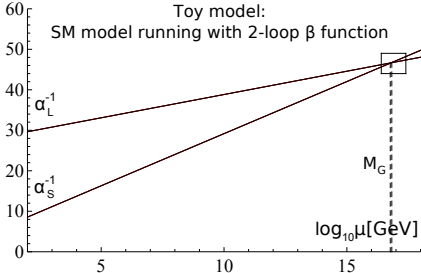


One-loop  
result with  
"typical"  
errors due to  
neglecting  
2-loop  
effects

$\log_{10} \tau(p \rightarrow \pi^0 e^+) [y]$

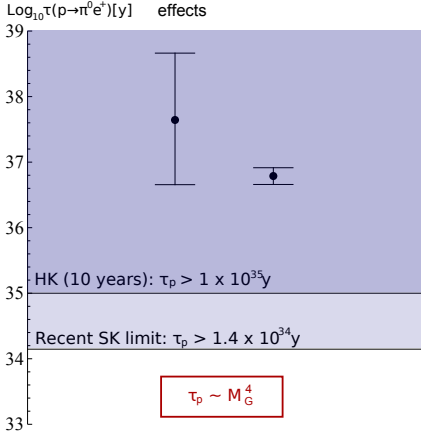


# Proton decay: theoretical uncertainties vs experiment



One-loop result with "typical" errors due to neglecting 2-loop effects

Two-loop result with error due to uncertainty in  $\alpha_S$



# Proton decay: theoretical uncertainties vs experiment

## Still other sources of uncertainties!

- threshold effects ( $\sim$  size of 2-loop corrections)  $\Rightarrow$  knowledge of the heavy spectrum needed
- SUSY GUTs:  $m_{\text{SUSY}}$  uncertainty
- Planck induced effective operators  
[Calmet, Hsu, Reeb, 2008, arXiv: 0805.0145]

$$\frac{c}{M_{\text{pl}}} \text{Tr}(G_{\mu\nu} G^{\mu\nu} H)$$

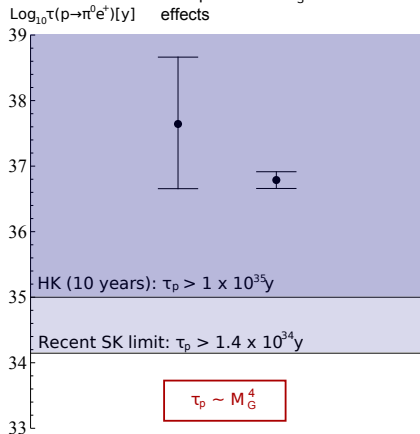
$\langle H \rangle = M_G \Rightarrow$  redefinition of gauge couplings  $\Rightarrow \alpha_i$  measured  
 $\times$  unification condition:

$$(1 + k_i \varepsilon) \alpha_i(M_G) = (1 + k_j \varepsilon) \alpha_j(M_G)$$

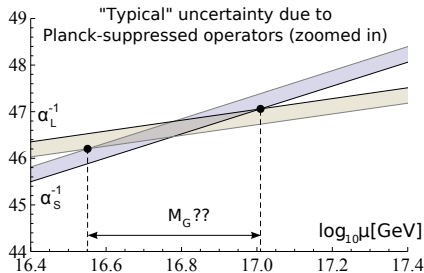
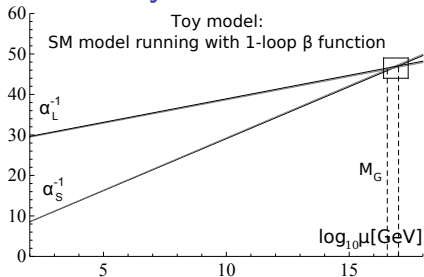
$$\varepsilon \sim M_G/M_{\text{pl}}, k_i \sim \mathcal{O}(1)$$

One-loop result with "typical" errors due to neglecting 2-loop effects

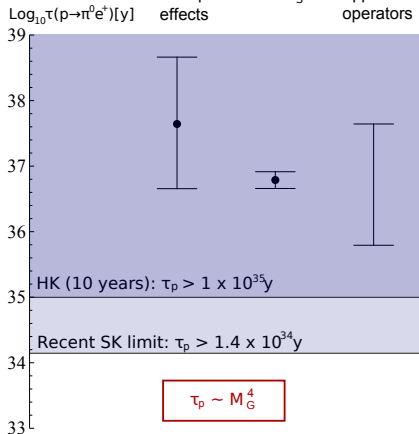
Two-loop result with error due to uncertainty in  $\alpha_5$



# Proton decay: theoretical uncertainties vs experiment



One-loop result with "typical" errors due to neglecting 2-loop effects	Two-loop result with uncertainty in $\alpha_S$	One-loop result with "typical" error due to Planck-suppressed operators
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# Non-SUSY SO(10) broken by $\langle 45_H \rangle$

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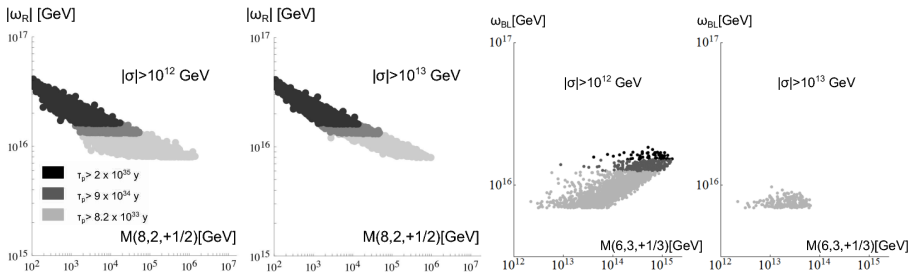
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- Exact unification and correct seesaw scale ( $\langle 126_H \rangle \equiv \sigma \sim 10^{13}$  GeV) ensured by making either  $(8, 2, +1/2)$  or  $(6, 3, 1/3)$  scalar field light [Bertolini, Di Luzio, Malinsky, 2010, arXiv: 1302.3401], [HK, Malinsky, 2014, arXiv: 1409.4961]
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