

# Lepton number violation with *and without* Majorana neutrino masses

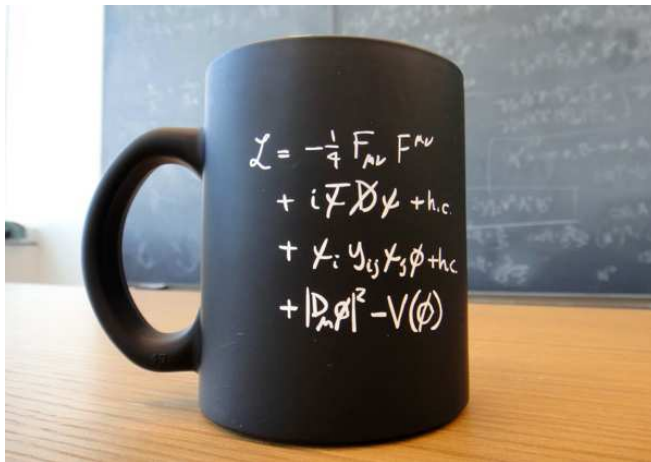
Julian Heeck

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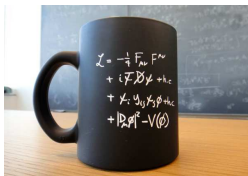
15.03.2015 – Moriond – Electroweak Interactions

# Standard Model of Particle Physics

So simple and beautiful!



# Standard Model of Particle Physics



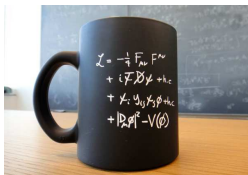
Small print:

- Gauge group  $SU(3)_{\text{color}} \times SU(2)_{\text{isospin}} \times U(1)_{\text{hypercharge}}$ ;  
 $\Rightarrow 8 + 3 + 1$  **spin-1** bosons with field strength  $F_{\mu\nu}$ ,
- Three copies of **spin- $\frac{1}{2}$**  Weyl fields (families/generations) in rep.

$$\Psi_{1,2,3} \sim \underbrace{\left( \mathbf{3}, \mathbf{2}, \frac{1}{6} \right) \oplus \left( \mathbf{3}, \mathbf{1}, -\frac{2}{3} \right) \oplus \left( \mathbf{3}, \mathbf{1}, \frac{1}{3} \right)}_{\text{quarks}} \oplus \underbrace{\left( \mathbf{1}, \mathbf{2}, -\frac{1}{2} \right) \oplus \left( \mathbf{1}, \mathbf{1}, 1 \right)}_{\text{leptons}}$$

- One complex **spin-0** field  $\phi \sim \left( \mathbf{1}, \mathbf{2}, -\frac{1}{2} \right)$  which breaks  $SU(2) \times U(1) \rightarrow U(1)_{\text{EM}}$  via  $\langle \phi \rangle \simeq 250$  GeV.
- About **18 free parameters**, all measured as of 2013 (Brout–Englert–Higgs boson mass).

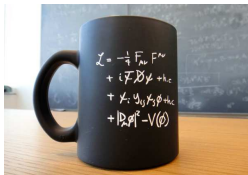
# Standard Model of Particle Physics



even smaller print (shortcomings of the Standard Model):

- Neutrino mass and mixing?
- Dark matter?
- Origin of matter–antimatter asymmetry of our Universe?

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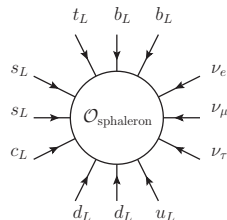
- Neutrino mass and mixing?
- Dark matter?
- Origin of matter–antimatter asymmetry of our Universe?

Actually *easy* to accommodate, but guided by what principle?

# Symmetries of the Standard Model

## A closer look at the mug:

- Baryon ( $B$ ) and lepton number ( $L$ ) classically conserved in the SM.
- $B + L$  theoretically broken non-perturbatively:  $\Delta(B + L) = 6$ .
  - *Instanton*: tunneling at  $T = 0$ , highly suppressed.
  - *Sphaleron*: thermal jump over barrier, fast for  $T \gtrsim 100$  GeV.



- $B - L$  globally conserved in SM at quantum level.

Fate of fundamental  $U(1)_{B-L}$  from **experiments**.

Linked to neutrino nature and matter–antimatter asymmetry.

# Symmetry of the Standard Model: $B - L$

- $B - L$  globally conserved in SM.

Fate of fundamental  $U(1)_{B-L}$  from **experiments**.

Linked to neutrino nature and matter–antimatter asymmetry.

One more comment from **theory**:

- $B - L$  locally conserved after adding three right-handed neutrinos

$$\nu_R \sim (\mathbf{1}, \mathbf{1}, 0)$$

to cancel anomalies.

- Allows Yukawa coupling

$$\mathcal{L} \supset y_\nu \bar{L} \phi \nu_R + \text{h.c.} \rightarrow \underbrace{y_\nu \langle \phi \rangle}_{m_\nu} \bar{\nu}_L \nu_R + \text{h.c.}$$

⇒ Neutrinos automatically massive if we gauge  $U(1)_{B-L}$ !

## Side Remark

With three  $\nu_R$ , one can actually gauge the much larger non-anomalous<sup>1</sup>

$$U(1)_{B-L} \times U(1)_{L_e - L_\mu} \times U(1)_{L_\mu - L_\tau} \quad \Leftarrow \quad \text{for free!}$$

Flavored  $U(1)$  subgroups can shed light on

- neutrino mixing (e.g. via texture zeros),<sup>1</sup>
- neutrino mass hierarchies,<sup>2</sup>
- flavor violation, e.g.  $h \rightarrow \mu\tau$  in 2HDM,<sup>3</sup> ✓ Talk by Andreas Crivellin.
- lepton-non-universality in  $B$ -meson decays,<sup>4</sup>
- ...

⇒ Very simple gauge symmetry models to study lepton flavor!

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<sup>1</sup>J.H., T. Araki, and J. Kubo, JHEP **1207** (2012) [arXiv:1203.4951].

<sup>2</sup>J.H. and W. Rodejohann, PRD **85**, 113017 (2012) [arXiv:1203.3117].

<sup>3</sup>J.H., M. Holthausen, W. Rodejohann, and Y. Shimizu, arXiv:1412.3671.

<sup>4</sup>J.H., A. Crivellin, and G. D'Ambrosio, PRL (2015) [arXiv:1501.00993],  
J.H., A. Crivellin, and G. D'Ambrosio, arXiv:1503.03477.



# Back to $B - L$

Three possibilities for (local)  $U(1)_{B-L}$ :

1 Majorana  $B - L$

- $\Delta(B - L) = 2$ ,
- Majorana neutrinos, i.e.  $\nu = \bar{\nu}$ ,
- thermal leptogenesis.

2 Unbroken  $B - L$

- Dirac neutrinos, i.e.  $\nu \neq \bar{\nu}$ ,
- neutrino genesis.

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Majorana  $B - L$ 

- New scalar  $\phi_{B-L=2}$  to break  $U(1)_{B-L}$  by two units.

$$\mathcal{L} \supset Y_\nu \bar{\nu}_R H L + \frac{1}{2} Y_R \bar{\nu}_R \nu_R^c \phi_{B-L=2}^* + \text{h.c.}$$

- Spontaneous symmetry breaking gives mass matrix for  $(\nu_L, \nu_R^c)$ :

$$\mathcal{M} = \begin{pmatrix} 0 & Y_\nu^T \langle H \rangle \\ Y_\nu \langle H \rangle & Y_R \langle \phi_{B-L=2} \rangle \end{pmatrix}.$$

- High scale  $Y_R \langle \phi_{B-L=2} \rangle \gg Y_\nu \langle H \rangle$ :  
small seesaw Majorana mass for active neutrinos:

$$\mathcal{M}_\nu \simeq - \frac{\langle H \rangle^2}{\langle \phi_{B-L=2} \rangle} Y_\nu^T Y_R^{-1} Y_\nu \sim 0.5 \text{ eV} \left( \frac{10^{14} \text{ GeV}}{\langle \phi_{B-L=2} \rangle} \right).$$

- Signature of Majorana  $B - L$ : neutrinoless double beta decay

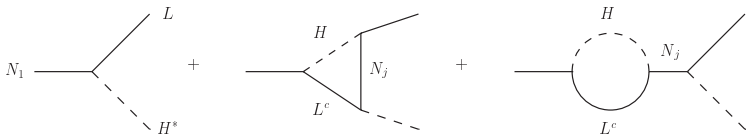
$$(A, Z) \rightarrow (A, Z + 2) + 2e^- \quad \Leftrightarrow \quad \Delta(B - L) = 2.$$

- Low-scale seesaw has more signatures.  $\leftarrow$  J. Lopez-Pavon's talk.

# Majorana $B - L$ : Leptogenesis

$$\mathcal{L} \supset Y_\nu \bar{\nu}_R H L + \frac{1}{2} Y_R \bar{\nu}_R \nu_R^c \phi_{B-L=2}^* + \text{h.c.}$$

- Heavy ( $\mathcal{M}_R \simeq Y_R \langle \phi_{B-L=2} \rangle \gtrsim 10^8 \text{ GeV}$ ) Majorana neutrinos  $N = \nu_R + \nu_R^c$  decay out-of-equilibrium in early Universe.



- If  $CP$  violated in loops:  $\Gamma(N \rightarrow HL) \neq \Gamma(N \rightarrow H^* \bar{L})$   
 $\Rightarrow$  Lepton asymmetry  $\Delta_L!$
- Sphalerons with  $\Delta B = \Delta L = 3$  above  $T \gtrsim 100 \text{ GeV}$  transfer  $\Delta_L$  to baryon asymmetry  $\Delta_B \propto \Delta_L$ .

# Majorana $B - L$ : Summary

$$\mathcal{L} \supset Y_\nu \bar{\nu}_R H L + \frac{1}{2} Y_R \bar{\nu}_R \nu_R^c \phi_{B-L=2}^* + \text{h.c.}$$

Very neat:

- Neutrinos massive, “automatically” small Majorana masses. ✓
- Matter–antimatter asymmetry. ✓
- (Making one of the  $\nu_R$  light (keV) can give warm dark matter.<sup>5</sup> ✓)

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<sup>5</sup>Upcoming white paper by M. Drewes, T. Lasserre, A. Merle, S. Mertens, J.H. et al.

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- What if neutrinos turn out to be Dirac (like all other fermions)?
- Why should  $B - L$  be broken by 2 units?
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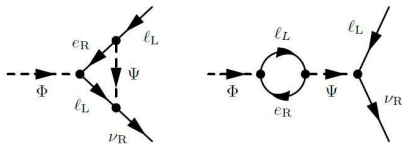
- $\Delta(B - L) = n \neq 2$ ,
- Dirac neutrinos,
- Dirac leptogenesis.



# Unbroken $B - L$

Almost<sup>6</sup> never considered, but very simple:<sup>7</sup>

- Neutrinos are Dirac, with Yukawa couplings  $Y_\nu \sim m_\nu / \langle H \rangle \lesssim 10^{-11}$ .
- Matter–antimatter asymmetry via **neutrino**genesis:<sup>8</sup>
  - New heavy scalar doublets decay so that  $\Delta(B - L) = \Delta L = 0$ , but  $\Delta_L^{\text{left}} = -\Delta_L^{\text{right}} \neq 0$ .



- Right-handed  $\nu_R$  **not thermalized** due to tiny Yukawas.  
 $\Rightarrow$  Sphalerons only see  $\Delta_L^{\text{left}}$ , generate  $\Delta_B \propto \Delta_L^{\text{left}}$  via  $\Delta(B + L) = 6!$

<sup>6</sup>D. Feldman, P. Fileviez Perez, and P. Nath, arXiv:1109.2901.

<sup>7</sup>J.H., PLB **739**, 256 (2014) [arXiv:1408.6845].

<sup>8</sup>K. Dick, M. Lindner, M. Ratz, and D. Wright, arXiv:hep-ph/9907562.

# Signatures of Unbroken $B - L$

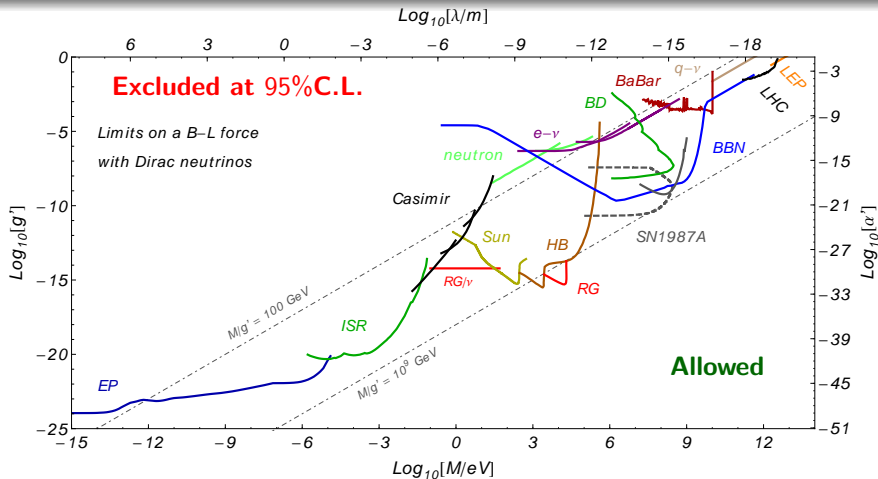
- No  $0\nu 2\beta$  or other  $\Delta(B - L) \neq 0$  processes. . .
- Massless  $Z'$  with tiny coupling  $\alpha' \lesssim 10^{-50}$ ,
- or  $M_{Z'} > 0$  with Stückelberg mass.
- $M_{Z'}/g'$  not connected to  $m_\nu$  or leptogenesis  $\Rightarrow$  no preferred scale!
- Limits from modified gravity, stellar energy losses, scattering/collider experiments, and Big Bang nucleosynthesis ( $\bar{\nu}_R \gamma^\mu \nu_R Z'_\mu$ ).

$\Rightarrow$  Unbroken (local)  $B - L$  perfectly valid!<sup>9</sup>

- (For  $\tau_{Z'} > \tau_{\text{Universe}}$ ,  $Z'$  could form dark matter via misalignment.)

<sup>9</sup>J.H., PLB **739**, 256 (2014) [arXiv:1408.6845].

# The Money Shot



Applicable to any  $Z'_{B-L}$  (BBN,  $RG/\nu$ , solid SN1987 depend on number of light  $\nu_R$ ).<sup>10</sup>

<sup>10</sup>J.H., PLB 739, 256 (2014) [arXiv:1408.6845].

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- $\Delta(B - L) = n \neq 2$ ,
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Dirac  $B - L$ 

Break  $B - L$ , but by  $n \neq 2$  units.<sup>11</sup>

⇒ Lepton number violating Dirac neutrinos.

- All fermions in  $SM + \nu_R$  are odd under  $B - L$   
 ⇒ only **even**  $\Delta(B - L)$  possible.  
 ⇒ Lowest order new processes:  $\Delta(B - L) = 4$ :

$$\mathcal{O}_{d=6} : \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=8} : |H|^2 \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R, \quad (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \nu_R, \quad F_Y^{\mu\nu} \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=10} : (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L), \quad (\bar{u}_R d_R^c)(\bar{d}_R \tilde{H}^\dagger L)(\bar{\nu}_R^c \nu_R), \\ F_Y^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, \quad W_a^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger \tau^a L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, \dots$$

$$\mathcal{O}_{d=18} : (\bar{d}_R d_R^c \bar{u}_R^c u_R \bar{e}_R^c e_R)(\bar{d}_R d_R^c \bar{u}_R^c u_R \bar{e}_R^c e_R), \dots$$

$$\mathcal{O}_{d=20} : \left[ (\overline{(D_\mu L)^c} \tilde{H})(H^\dagger D_\nu L) \right]^2 \supset (\bar{e}_L^c W_\mu^+ W_\nu^+ e_L)(\bar{e}_L^c W^{+\mu} W^{+\nu} e_L), \dots$$

- $(U(1)_{B-L} \rightarrow \mathbb{Z}_4$  breakdown could stabilize dark matter.)

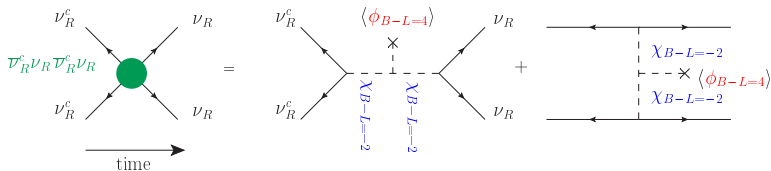
<sup>11</sup>  $\Delta L = 0 \pmod n$  old idea, e.g. E. Witten, hep-ph/0006332.

# UV Completion

- One scalar  $\phi_{B-L=4}$  to break  $B - L$ , one scalar  $\chi_{B-L=-2}$  as mediator.

$$\mathcal{L} \supset y \bar{L} H \nu_R + \kappa \chi_{B-L=-2} \bar{\nu}_R \nu_R^c + \text{h.c.}$$

- Neutrinos are Dirac (and  $\Delta L = 2$  forbidden) if  $\langle \chi_{B-L=-2} \rangle = 0$ .
- Scalar potential  $V \supset \mu \phi_{B-L=4} (\chi_{B-L=-2})^2 + \text{h.c.}$
- Lepton number violation  $\Delta L = 4$  still possible!<sup>12</sup>



- Extension to left–right model can enhance rates.

<sup>12</sup>J.H. and W. Rodejohann, EPL **103**, 32001 (2013) [arXiv:1306.0580].

# Extension to Left-Right Model

- $U(1)_{B-L}$  easily embeddable into left-right symmetric models:  
 $SU(2)_L \times U(1)_Y \rightarrow SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ .
- $\nu_R$  now part of a doublet:

$$\Psi_L = (\nu_L, e_L)^T \sim (\mathbf{2}, \mathbf{1}, -1),$$

$$\Psi_R = (\nu_R, e_R)^T \sim (\mathbf{1}, \mathbf{2}, -1),$$

$$q_L = (u_L, d_L)^T \sim (\mathbf{2}, \mathbf{1}, 1/3),$$

$$q_R = (u_R, d_R)^T \sim (\mathbf{1}, \mathbf{2}, 1/3),$$

$$H = \begin{pmatrix} h_1^0 & h_1^+ \\ h_2^- & h_2^0 \end{pmatrix} \sim (\mathbf{2}, \bar{\mathbf{2}}, 0).$$

- Typically introduce triplet  $\delta \sim (\mathbf{1}, \mathbf{3}, -2)$  to break

$$SU(2)_R \times U(1)_{B-L} \xrightarrow{\langle \delta \rangle} U(1)_Y$$

at high scale and give mass to gauge bosons  $Z_R$  and  $W_R^\pm$ .

$\Rightarrow$  Left-right extension of Majorana  $B - L \dots$

# Left-Right Extension of Dirac $B - L$

- Important part of simple model:

$$\mathcal{L} \supset y \bar{L} H \nu_R + \kappa \chi_{B-L=-2} \bar{\nu}_R \nu_R^c + \mu \phi_{B-L=4} (\chi_{B-L=-2})^2 + \text{h.c.}$$

- Extension to left-right straightforward:<sup>13</sup>

$$\chi_R = \frac{1}{\sqrt{2}} \begin{pmatrix} \chi_R^- & \chi_R^0 & 0 \\ \chi_R^{--} & 0 & \chi_R^0 \\ 0 & \chi_R^{--} & -\chi_R^- \end{pmatrix} \sim (\mathbf{1}, \mathbf{3}, -2),$$

$$\phi_R = \frac{1}{\sqrt{6}} \begin{pmatrix} \phi_R^{++} & \sqrt{3}\phi_R^{+++} & \sqrt{6}\phi_R^{++++} \\ \sqrt{3}\phi_R^+ & -2\phi_R^{++} & -\sqrt{3}\phi_R^{+++} \\ \sqrt{6}\phi_R^0 & -\sqrt{3}\phi_R^+ & \phi_R^{++} \end{pmatrix} \sim (\mathbf{1}, \mathbf{5}, 4).$$

- Couplings perfect (add  $\chi_L$  and  $\phi_L$  for LR parity):

$$\mathcal{L} \supset y \bar{\Psi}_L H \Psi_R + \kappa \bar{\Psi}_R \chi_R \Psi_R^c + \mu \text{tr} [\chi_R \phi_R \chi_R] + \text{h.c.}$$

- Triplet *without* VEV,  $SU(2)_R$  breaking via  $\langle \phi_R \rangle$ :

$$M_{W_R^\pm}^2 = 2g_R^2 \langle \phi_R^0 \rangle^2, \quad M_{Z_R}^2 = 8 \langle \phi_R^0 \rangle^2 (g_R^2 + 4g_{B-L}^2).$$

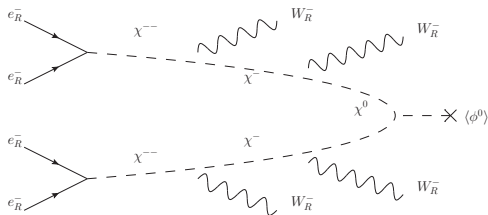
<sup>13</sup>J.H., work in progress.



# Phenomenology of LNV Dirac Neutrinos

How to check for  $\Delta L = 4$ ?

- Collider processes:
  - LHC:  $pp \rightarrow W^- W^- W^- W^- \ell^+ \ell^+ \ell^+ \ell^+ + X$ ,
  - Like-sign lepton collider:  $e^- e^- \rightarrow W^- W^- W^- W^- \ell^+ \ell^+$ .
- Nuclear decays ( $0\nu 4\beta?$ ).<sup>14</sup>
- Rare meson decays etc.?



All tough, many particles in final state and tiny rates!<sup>14</sup>  
 (Even harder for  $\Delta L > 4$ ...)

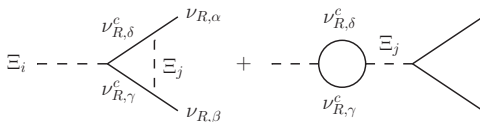
$\Delta L = 4$  can however easily be relevant in the early Universe  
 $\Rightarrow$  new *Dirac leptogenesis* mechanism!<sup>15</sup>

<sup>14</sup>J.H. and W. Rodejohann, EPL **103**, 32001 (2013) [arXiv:1306.0580].

<sup>15</sup>J.H., PRD **88**, 076004 (2013) [arXiv:1307.2241].

# Dirac $B - L$ : Leptogenesis

- Two heavy mediator scalars  $\chi_{B-L=-2}^j = (\Xi_j + i\Xi_j)/\sqrt{2}$  decay to  $\nu_R\nu_R$  or  $\bar{\nu}_R\bar{\nu}_R$  out-of-equilibrium in early Universe.



$\Rightarrow$  Asymmetry in  $\nu_R$ :

$$\Delta_{\nu_R} \propto \frac{\Gamma(\Xi_i \rightarrow \nu_R\nu_R) - \Gamma(\Xi_i \rightarrow \nu_R^c\nu_R^c)}{\Gamma(\Xi_i \rightarrow \nu_R\nu_R) + \Gamma(\Xi_i \rightarrow \nu_R^c\nu_R^c)}.$$

Asymmetry in  $\nu_R$ . ✓ How to translate to baryon asymmetry?

- Dirac-Yukawa coupling  $Y_\nu = m_\nu/\langle H \rangle$  too small to equilibrate  $\nu_R$ ...

# Baryon Asymmetry

Add second scalar doublet  $H_2$  with large Yukawa  $\bar{L}H_2\nu_R$ :

- Neutrinophilic  $H_2$  with small VEV  $\langle H_2 \rangle \sim 1 \text{ eV}$ .<sup>16</sup>  
 $\Rightarrow$  Dirac neutrinos light with large Yukawas.

$$\Delta_{\nu_R} \xrightarrow{H_2} \Delta_L \xrightarrow{\text{sphalerons}} \Delta_B.$$

$\Rightarrow$  Different from **neutrinogenesis!**

- Necessary thermalization of  $\nu_R \Rightarrow N_{\text{eff}} > 3!$
- $3.14 \lesssim N_{\text{eff}} \lesssim 3.29$  depending on  $H_2^+$  mass and Yukawa coupling.
- Planck 2015:  $N_{\text{eff}} = 3.15 \pm 0.23$  at 68% C.L.
- Specific collider signatures of neutrinophilic  $H_2$ .<sup>17</sup>

<sup>16</sup>Ma, PRL (2001), Wang, Wang, Yang, EPL (2006), Gabriel, Nandi, PLB (2007).

<sup>17</sup>Davidson and Logan, PRD **80** (2009) [arXiv:0906.3335].

# Summary

	$\Delta(B - L)$	neutrino	$B$ asymmetry	signatures
Unbroken $B - L$	0	Dirac	neutrino genesis	$Z'$
Majorana $B - L$	2	Majorana	leptogenesis	$0\nu 2\beta$
Dirac $B - L$	$> 2$ , e.g. 4	Dirac	Dirac leptogenesis	$0\nu 4\beta$ , $N_{\text{eff}} \gtrsim 3.14$

- $B - L$  mystery: global, local, unbroken, broken by 2, 4, ... units?
- Currently testing:  $\Delta L = 2$  via  $0\nu 2\beta$ .
- $\Delta L \geq 4$  way more challenging (experimentally and theoretically),
- but easily relevant in the early Universe.

# Backup

# Stückelberg Mass

Mass for a  $U(1)$  gauge boson without symmetry breaking:

- Introduce *real* scalar  $\sigma$  with gauge trafo  $\sigma \rightarrow \sigma + M_{Z'}\theta(x)$ .

$$\Delta\mathcal{L} = \frac{1}{2} (M_{Z'} Z'^{\mu} + \partial^{\mu}\sigma) (M_{Z'} Z'_{\mu} + \partial_{\mu}\sigma)$$

is gauge invariant ( $Z'_{\mu} \rightarrow Z'_{\mu} - \partial_{\mu}\theta$ ).

- Use gauge to set  $\sigma(x) = 0$ .
- Mass term  $\frac{1}{2} M_{Z'}^2 Z'_{\mu} Z'^{\mu}$  is just gauge **fixing**, not **breaking**.

*Abelian* gauge bosons can have a mass without symmetry breaking.

- Connection to Higgs mechanism in formal limit

$$v_{\Phi} \rightarrow \infty, \quad q_{\Phi} \rightarrow 0, \quad M_{Z'} \propto q_{\Phi} v_{\Phi} = \text{const.}$$

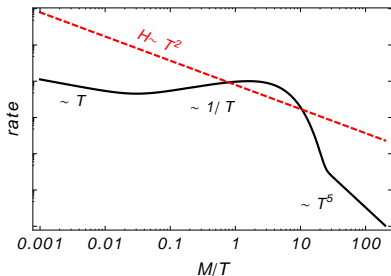
# Big Bang Nucleosynthesis

Unbroken  $B - L$ :

- $\nu_R$  are light (**Dirac neutrinos**)  $\rightarrow N_{\text{eff}} \simeq 6$  for strong  $Z'$  interactions.
- Light  $Z'$  also contributes to  $N_{\text{eff}}$ .
- BBN ( $T \sim 1 \text{ MeV}$ ) limit:  $N_{\text{eff}} < 4$  at 95% C.L.<sup>18</sup>

Thermally averaged rate via  $Z'$ :

$$\langle \Gamma(\bar{f}f \leftrightarrow \bar{\nu}_R \nu_R) \rangle \propto \begin{cases} g'^4 T, & M_{Z'} \ll T, \\ g'^2 \frac{M_{Z'}^2}{T}, & M_{Z'} \lesssim T, \\ \frac{g'^4}{M_{Z'}^4} T^5, & M_{Z'} \gg T. \end{cases}$$

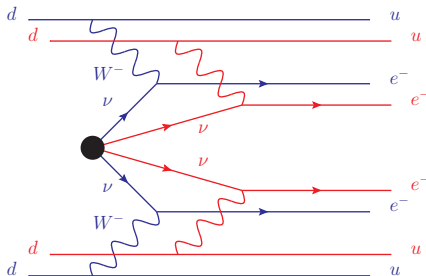


- Demand  $\langle \Gamma(\bar{f}f \leftrightarrow \bar{\nu}_R \nu_R) \rangle < H(T) \sim T^2/M_{\text{Pl}}$  “at” BBN.

<sup>18</sup>Mangano, Serpico, PLB (2011) [arXiv:1103.1261].

# How to check for $\Delta L = 4$ ?

- Neutrinoless quadruple beta decay<sup>19</sup>  $(A, Z) \rightarrow (A, Z + 4) + 4 e^-$   
e.g. via  $\mathcal{O}_{\Delta L=4} = (\bar{\nu}_L^c \nu_L)^2 / \Lambda^2$ :



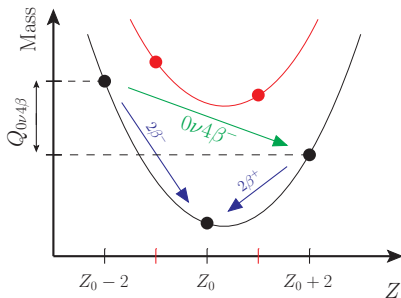
- Collider process  $e^- e^- \rightarrow W^- W^- W^- W^- \ell^+ \ell^+$ .
- Rare meson decays etc.?

<sup>19</sup>J.H. and W. Rodejohann, EPL **103**, 32001 (2013) [arXiv:1306.0580].



Candidate Nuclei for  $0\nu 4\beta$ 

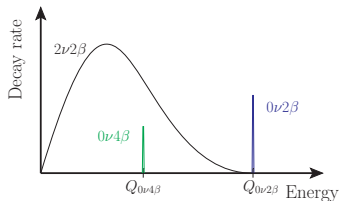
	$Q_{0\nu 4\beta}$	competing decays	NA/%
${}^{96}_{40}\text{Zr} \rightarrow {}^{96}_{44}\text{Ru}$	0.629 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{19} \text{ y}$	2.8
${}^{136}_{54}\text{Xe} \rightarrow {}^{136}_{58}\text{Ce}$	0.044 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 2 \times 10^{21} \text{ y}$	8.9
${}^{150}_{60}\text{Nd} \rightarrow {}^{150}_{64}\text{Gd}$	2.079 MeV	$\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18} \text{ y}$	5.6



# Best Candidate: Neodymium $^{150}\text{Nd}$

Decay channels:

- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{62}\text{Sm}$  via  $2\nu 2\beta$  ( $\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18}$  y): the two electrons have a continuous energy spectrum and total energy  $E_{e,1} + E_{e,2} < 3.371$  MeV.
- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{64}\text{Gd}$  via  $0\nu 4\beta$ . Four electrons with continuous energy spectrum and summed energy  $Q_{0\nu 4\beta} = 2.079$  MeV are emitted. In this special case, the daughter nucleus is  $\alpha$ -unstable with half-life  $\tau_{1/2}^{\alpha}(^{150}_{64}\text{Gd} \rightarrow ^{146}_{62}\text{Sm}) \simeq 2 \times 10^6$  y.



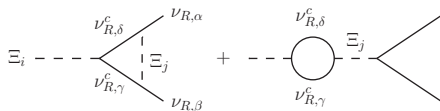
$0\nu 4\beta$  kinematically allowed, but expected rates **unobservable**.

# Dirac $B - L$ : Leptogenesis

- Scalar potential  $V(H, \phi, \chi) \supset -\mu \phi_{B-L=4} (\chi_{B-L=-2})^2$  breaks complex  $\chi_{B-L=-2} = (\Xi_1 + i\Xi_2)/\sqrt{2}$  into two real scalars with mass

$$m_1^2 = m_c^2 - 2\mu \langle \phi_{B-L=4} \rangle, \quad m_2^2 = m_c^2 + 2\mu \langle \phi_{B-L=4} \rangle.$$

- Heavy mediator scalar  $\Xi_j$  decays to  $\nu_R \nu_R$  or  $\bar{\nu}_R \bar{\nu}_R$  out-of-equilibrium in early Universe.



- $CP$  violation requires *second* scalar  $\chi_{B-L=-2}$ .

$$Y_{\nu_R} \equiv \frac{n_{\nu_R}}{s} \sim \frac{1}{g_*} \frac{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) - \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) + \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}.$$

Asymmetry in  $\nu_R$ . ✓ How to translate to baryon asymmetry?

# Baryon Asymmetry

- Dirac-Yukawa coupling  $Y_\nu = m_\nu / \langle H \rangle$  too small to equilibrate  $\nu_R$ ...

Add second scalar doublet  $H_2$  with large Yukawa  $\bar{L}H_2\nu_R$ :

- Neutrinophilic  $H_2$  with small VEV  $\langle H_2 \rangle \sim 1 \text{ eV}$ .<sup>20</sup>  
 $\Rightarrow$  Dirac neutrinos light with large Yukawas.
- $H_2$  moves  $Y_{\nu_R}$  to  $Y_{\nu_L}$ .
- Sphalerons move  $Y_{\nu_L}$  to  $Y_B$ .

$\Rightarrow$  Different from **neutrinogenesis!**

- Necessary thermalization of  $\nu_R \Rightarrow N_{\text{eff}} > 3!$
- $3.14 \lesssim N_{\text{eff}} \lesssim 3.29$  depending on  $H_2^+$  mass and Yukawa coupling.
- Specific collider signatures of neutrinophilic  $H_2$ .<sup>21</sup>

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<sup>20</sup>E. Ma, PRL **86** (2001), F. Wang, W. Wang, J. M. Yang, EPL **76** (2006), S. Gabriel and S. Nandi, PLB **655** (2007).

<sup>21</sup>Davidson and Logan, PRD **80** (2009) [arXiv:0906.3335].