

# Low-spin structure of $^{210}\text{Bi}$ investigated in cold neutron capture reaction on $^{209}\text{Bi}$

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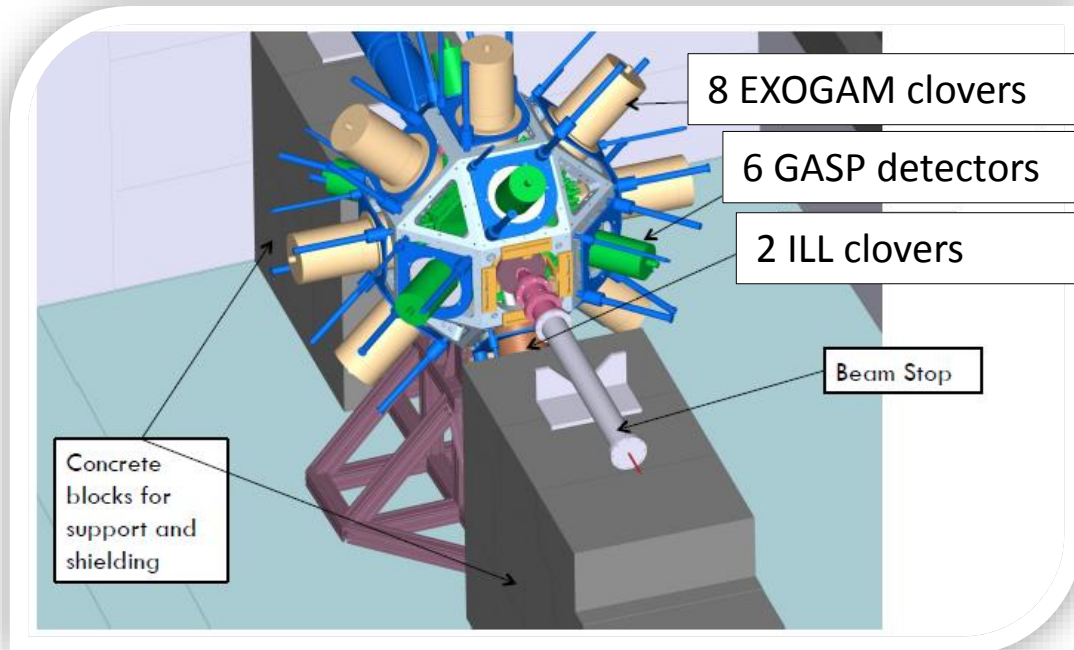
NATALIA CIEPLICKA

# Physics motivation

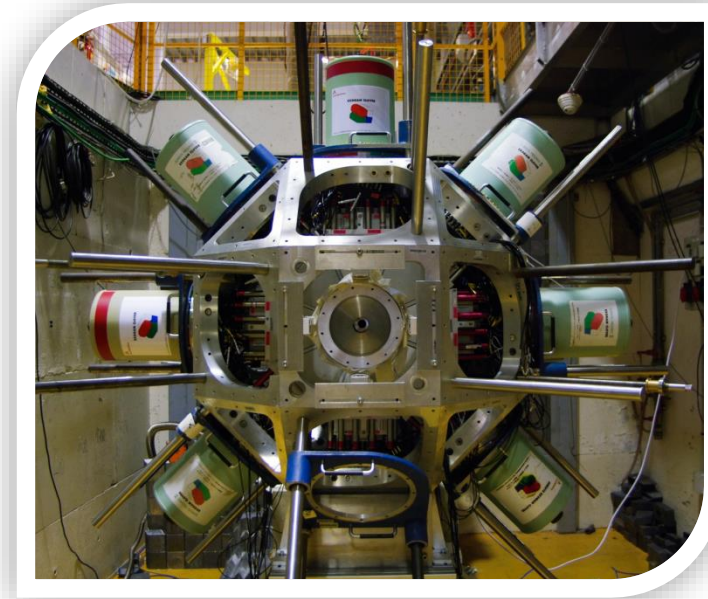
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- Why the  $^{210}\text{Bi}$  nucleus is an **ideal nucleus for testing the shell-model calculations?**
- A rich ground for comparisons with theory, also states arising from **coupling of proton and neutron particles excitations to the  $3^-$  first excited state of octupole character** in doubly-magic  $^{208}\text{Pb}$  are also expected.
- **The unknown multipolarity of the main transition feeding the ground state** introduced rather large uncertainties in measurements of the capture cross section to the ground state in  $^{210}\text{Bi}$ .
- The measured **lifetimes** may be compared to predictions of shell-model calculations.

# Experiment – ILL Grenoble (PF1B line)



16 Ge detectors of EXILL array: 8 of EXOGAM, 6 of GASP, and 2 from ILL collaboration – coincidence measurements of gamma rays



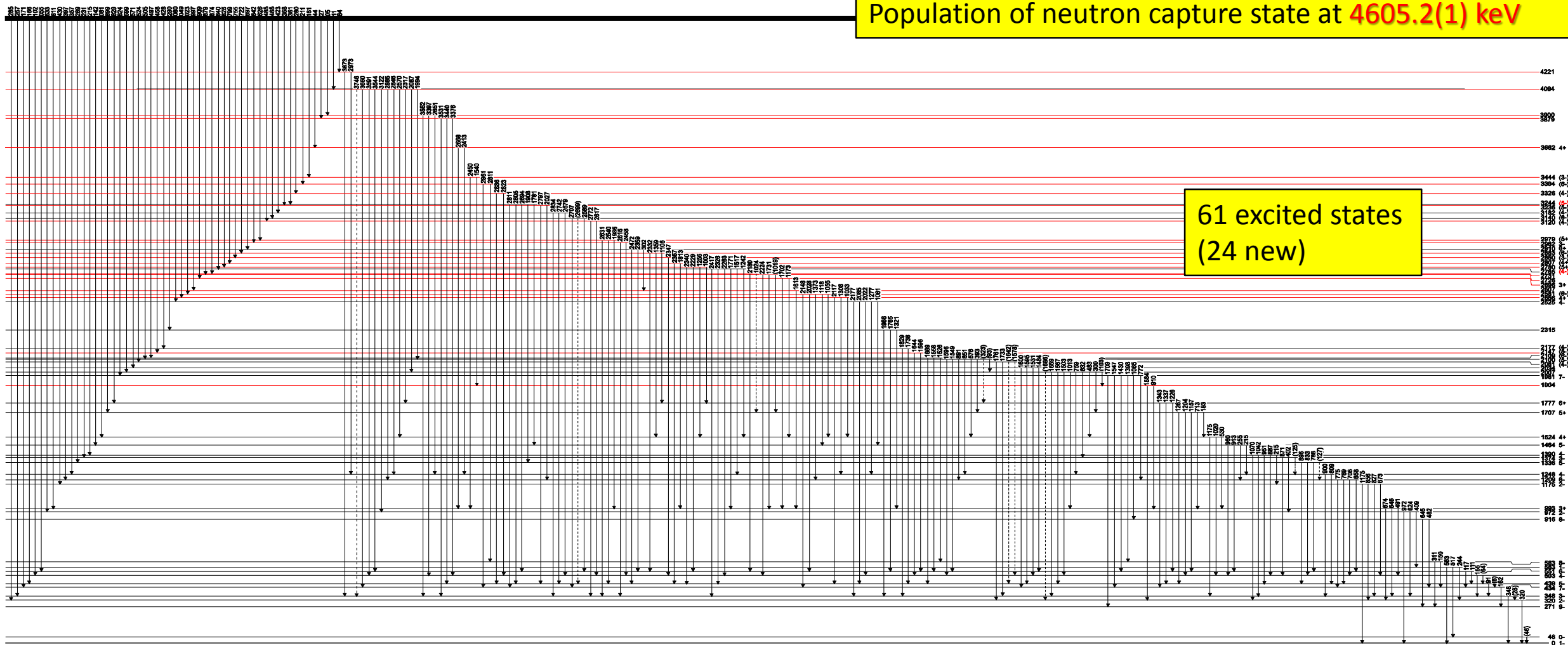
- 8 detectors of EXOGAM arranged into ring around the target at every  $45^\circ$  so angular correlation measurements could be performed
- Additional 4<sup>th</sup> angle ( $60^\circ$ ) from GASP detectors (correction factor of 0.115261)
- Measurements of the lifetimes with FATIMA detectors

55 primary transitions  
(31 new)

# Experimental results: level scheme

Population of neutron capture state at **4605.2(1) keV**

61 excited states  
(24 new)



$^{210}\text{Bi}$

# Angular correlations of $\gamma$ rays from $^{210}\text{Bi}$

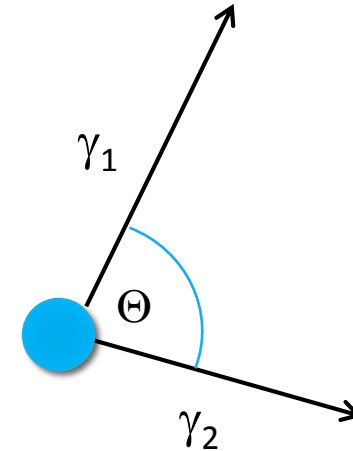
The angular correlation function for a pair of coincident  $\gamma$  rays connecting the nuclear states with spins  $J_i \rightarrow J \rightarrow J_f$  is usually expressed as:

$$W(\Theta) = 1 + A_2 P_2(\cos \Theta) + A_4 P_4(\cos \Theta)$$

$\Theta$  – the angle between the direction of emission of two  $\gamma$  rays

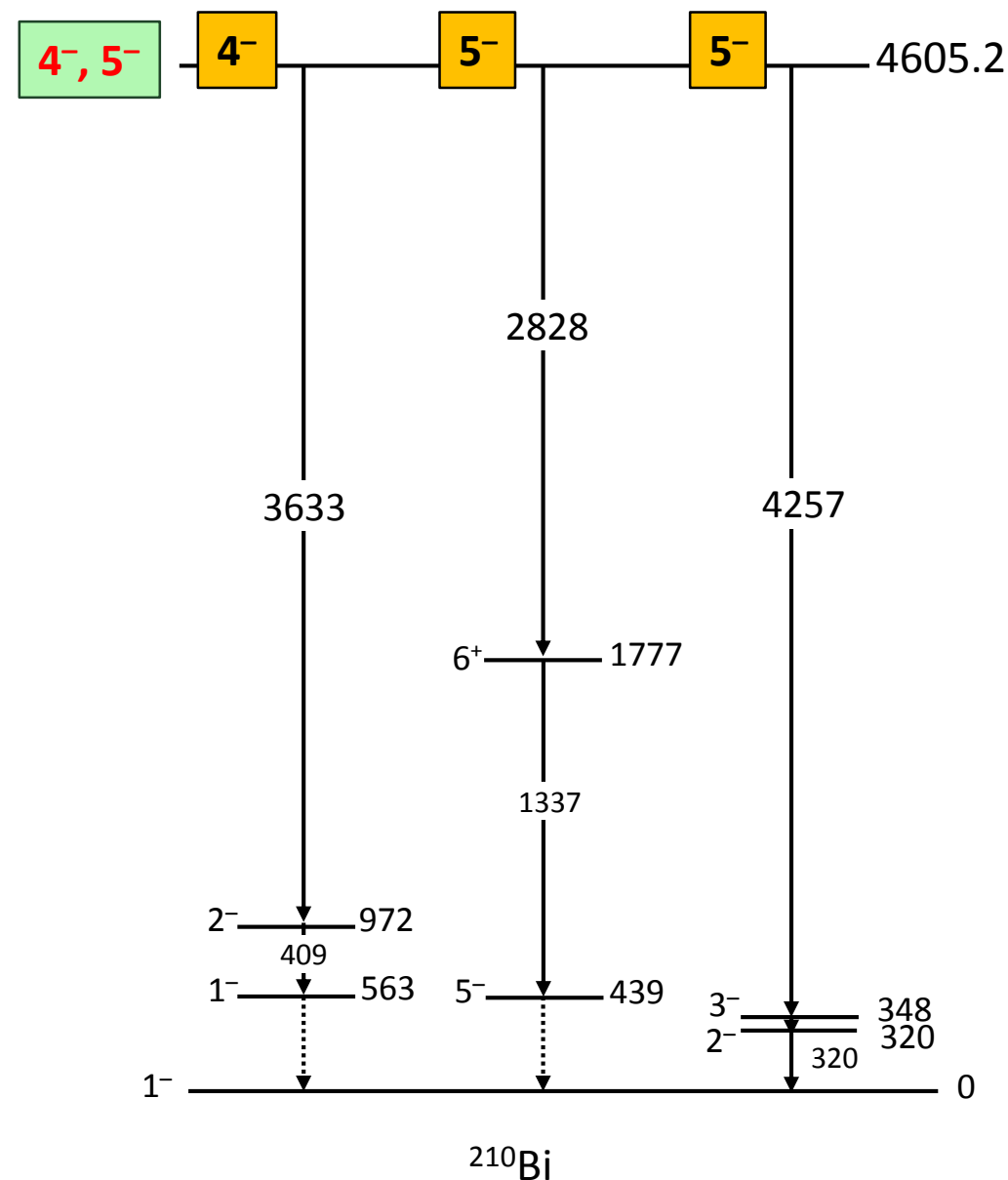
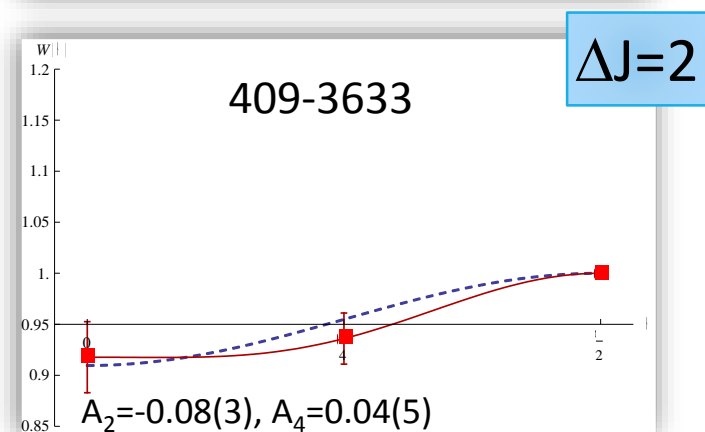
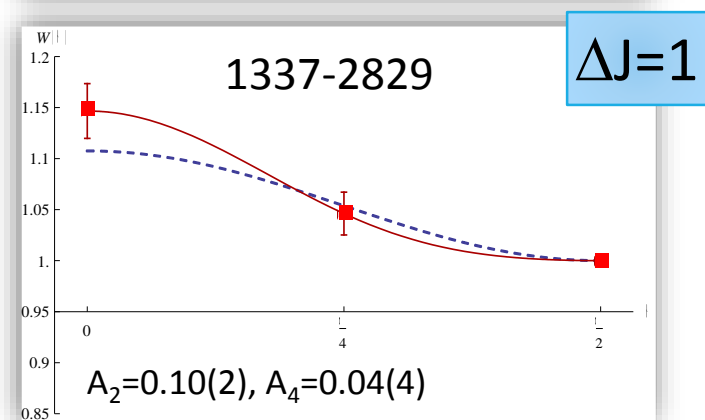
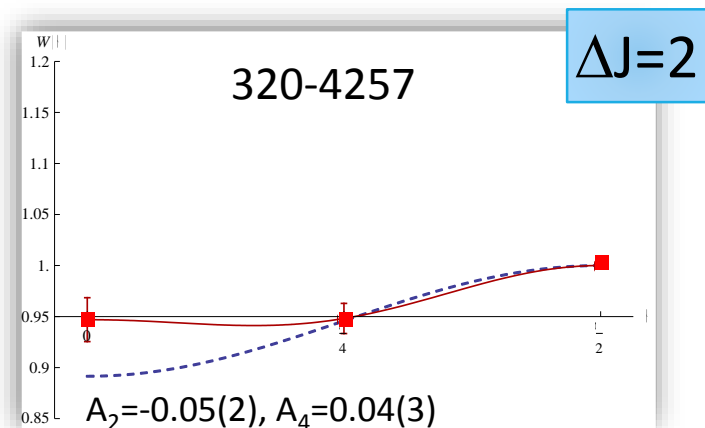
$P_n(\cos \Theta)$  – Legendre polynomials

$A_n = q_n A(1)A(2)$  – the coefficients which depend on the attenuation factor  $q_n$  as well as on the multipolarities of 1 and 2  $\gamma$  rays and the spins of involved nuclear states



experiment

theory



# Multipolarity of the main transition leading to the ground state

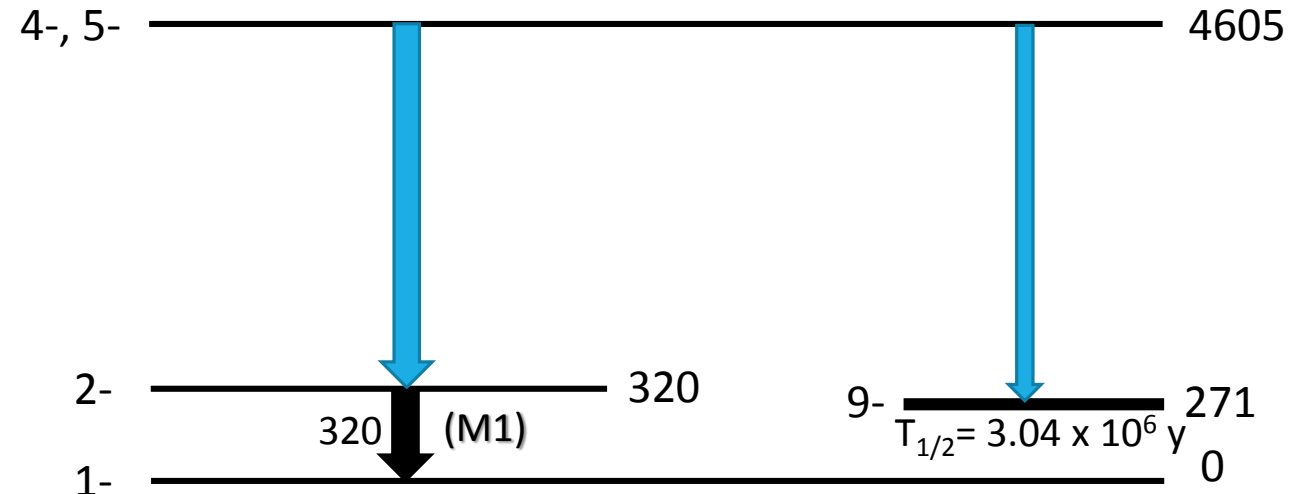
Not confirmed experimentally M1 multipolarity of 320-keV line

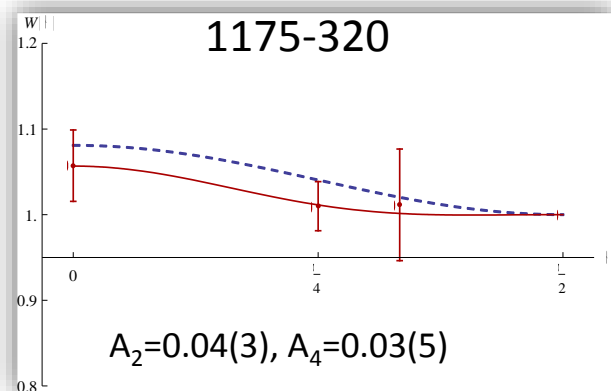
*A. Borella et al., Nucl. Phys. A 850, 1 (2011)*

Thermal capture cross section for the  $^{209}\text{Bi}(n,\gamma)^{210}\text{Bi}$  reaction to the ground state [mb]

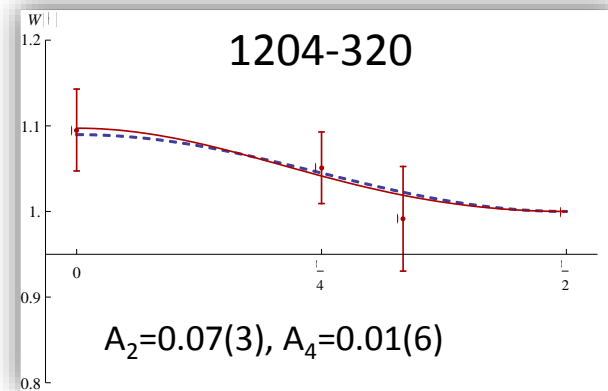
100% M1	50% M1 +50 % E2	100% E2
21.5(0.9)	19.3(0.8)	17.2(0.7)

*A. Borella et al., AIP Conf. Proc. 769, 648 (2005)*

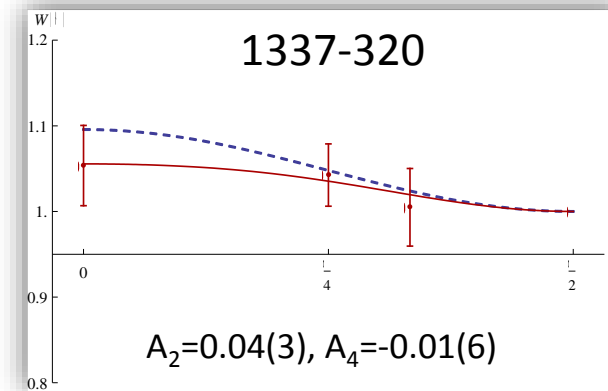




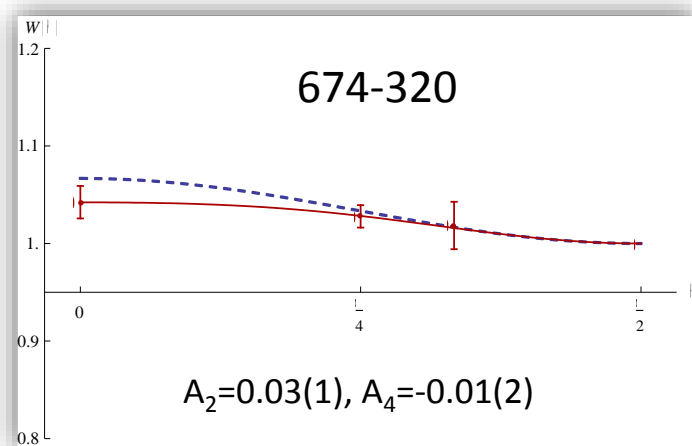
Theory E1-M1  
 $A_2=0.06, A_4=0.00$



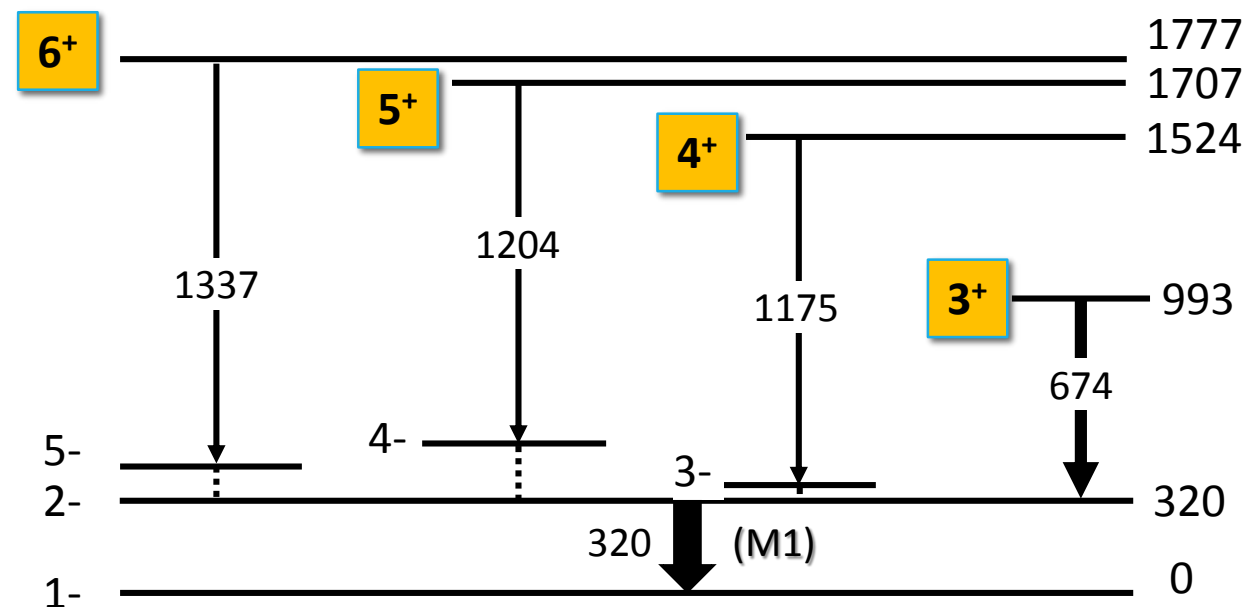
Theory E1-M1  
 $A_2=0.07, A_4=0.00$



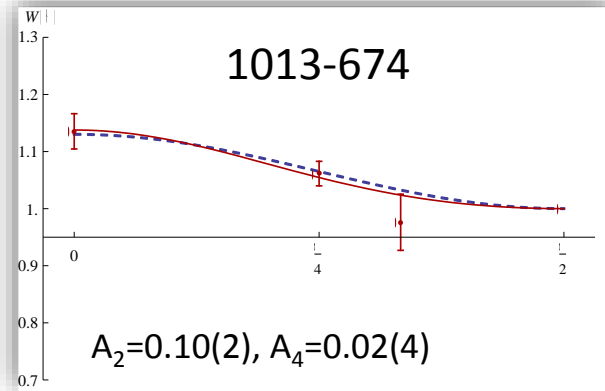
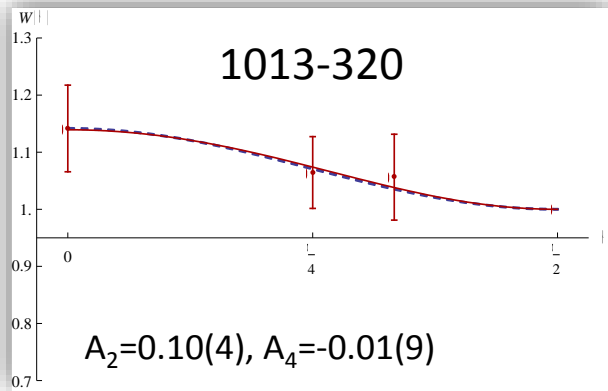
Theory E1-M1  
 $A_2=0.07, A_4=0.00$



Theory E1-M1  
 $A_2=0.05, A_4=0.00$



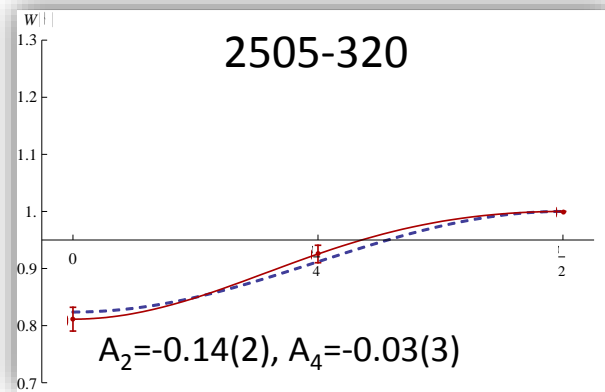
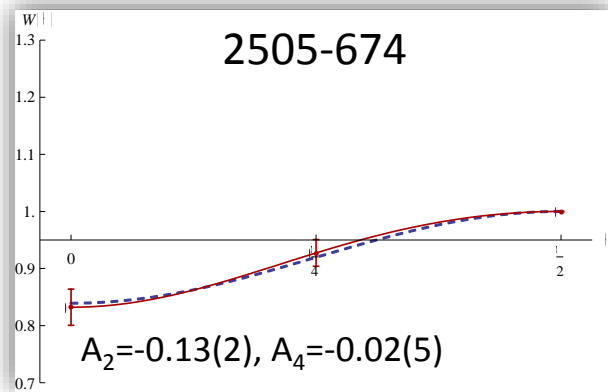




$$\delta_{1013}=-0.108$$

$$\delta_{674}=0.015(32)$$

$$\delta_{320}=0.04(8)$$

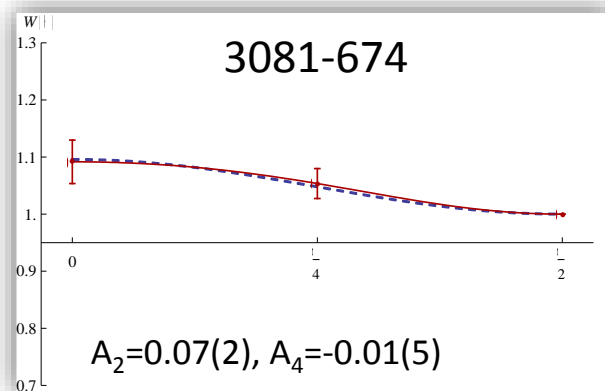
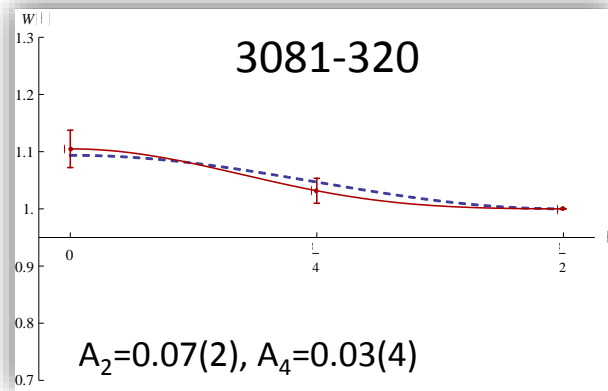


$$\delta_{2505}=0.055$$

$$(\delta_{2505}=-0.845)$$

$$\delta_{674}=0.015(29)$$

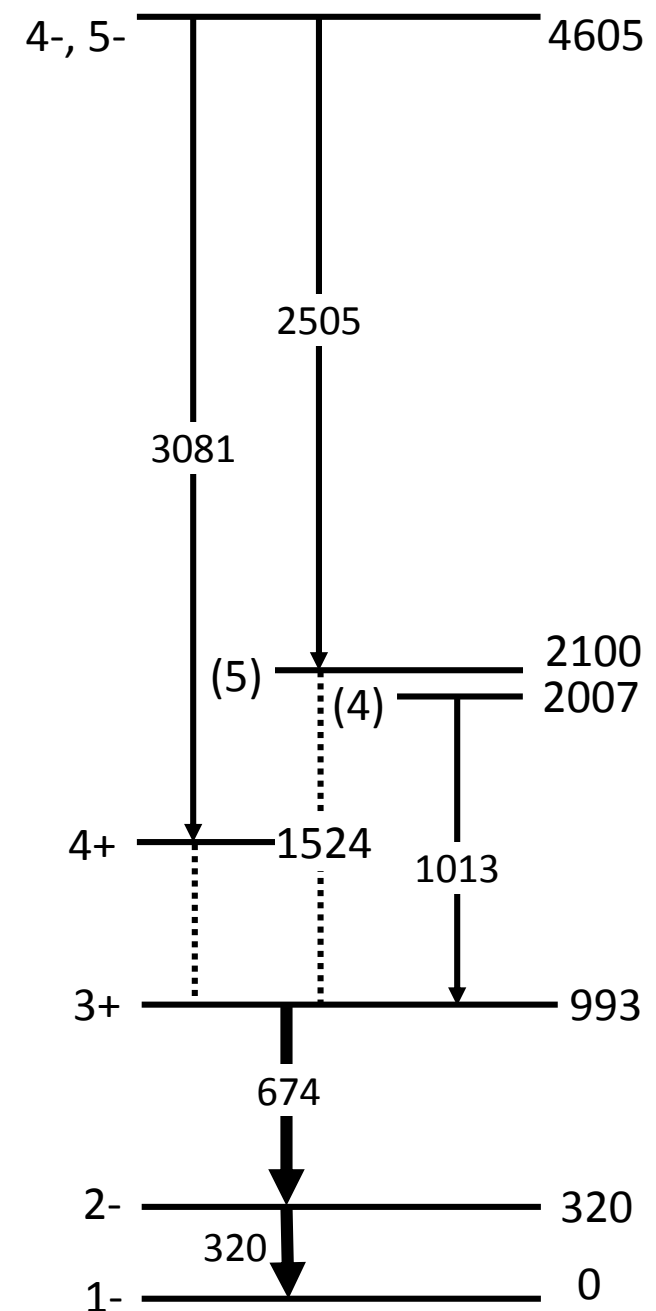
$$\delta_{320}=0.036(20)$$



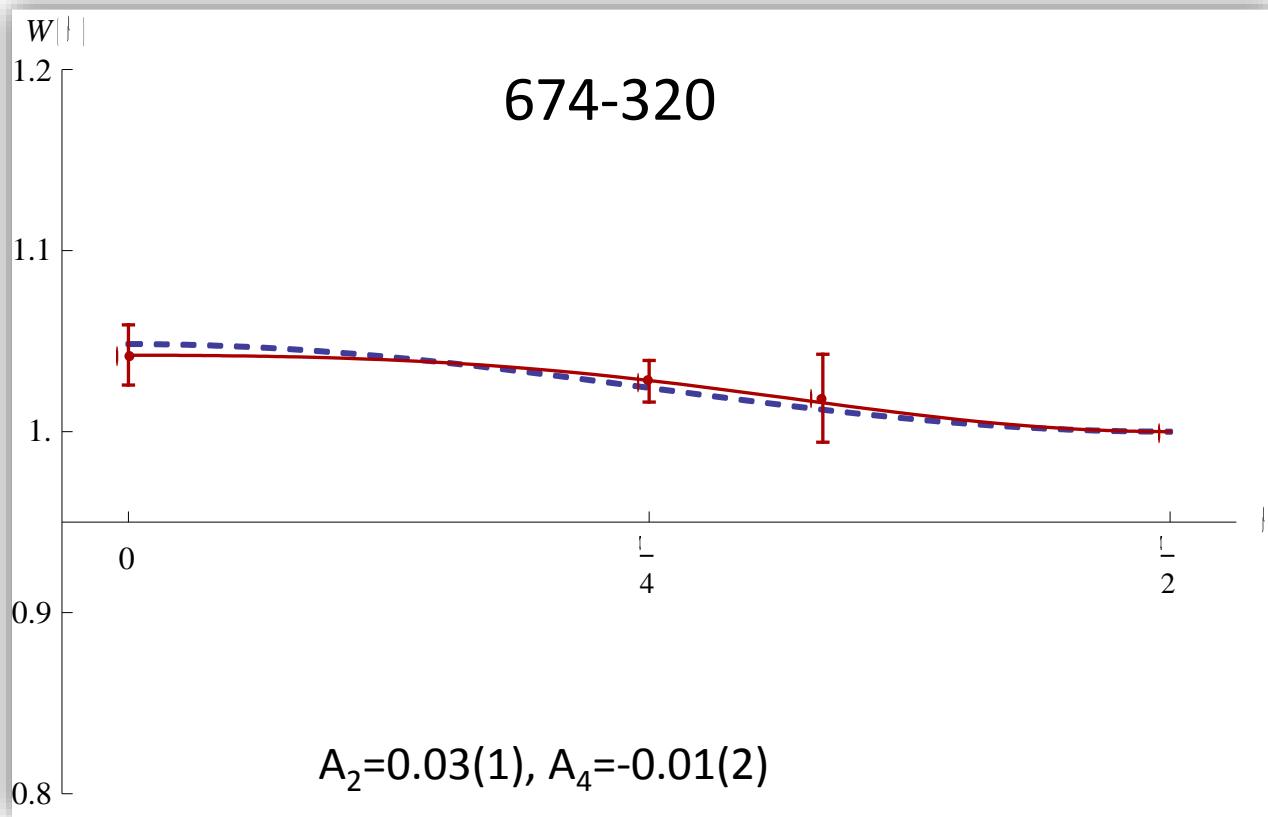
$$\delta_{3081}=-0.037$$

$$\delta_{674}=0.009(56)$$

$$\delta_{320}=0.05(5)$$



# Multipolarity of 320-keV transition



$$\delta_{674}=0.01(3)$$

$$\delta_{320}=0.04(3)$$

$$\delta^2 = \frac{I_{L'}}{I_L}$$

$$I(L) = \frac{1}{\delta^2 + 1}$$

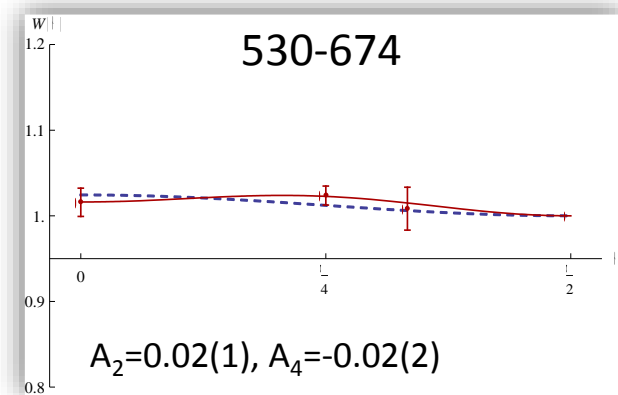
$$I(L') = \frac{\delta^2}{\delta^2 + 1}$$

674 keV: 99.99% E1 + 0.01% M2

320 keV: 99.84% M1 + 0.16% E2

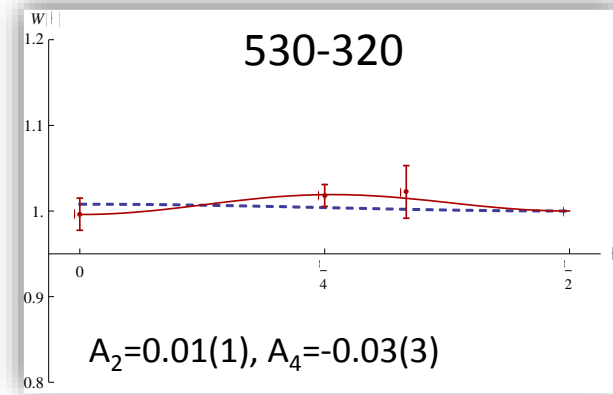
Decays to:  
3+, 4-, 3-

# Spin-parity values: state at 1524 keV



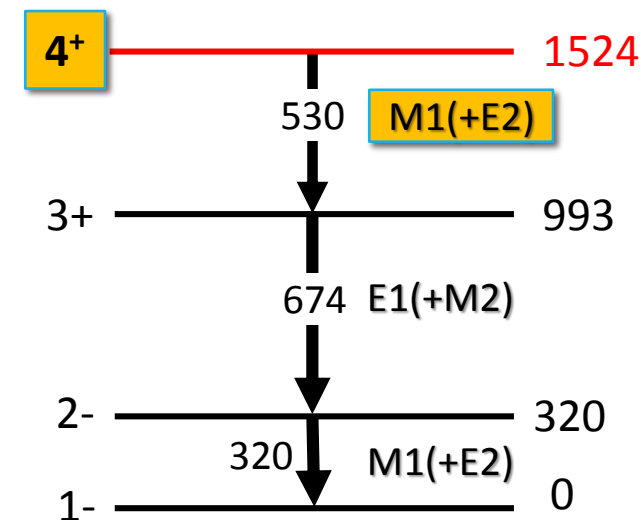
$$\delta_{530}=0.06(2)$$

$$(\delta_{530}=5.7(8))$$



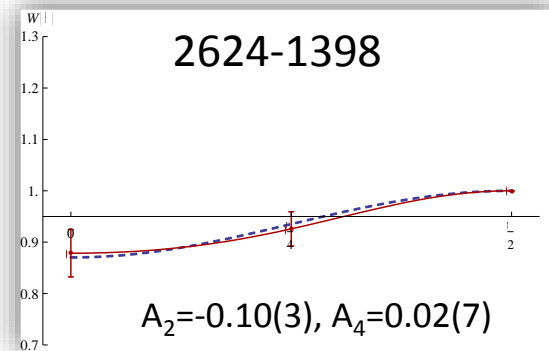
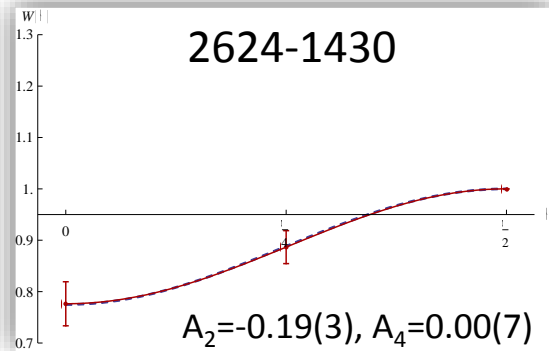
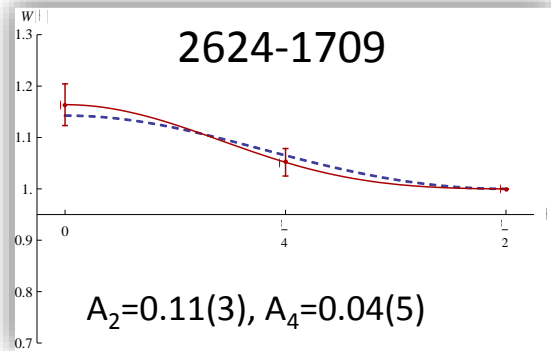
$$\delta_{530}=0.09(3)$$

$$(\delta_{530}=4.9(7))$$



Decays to:  
(6-), 8-, 8-, 6-, 7-, 9-

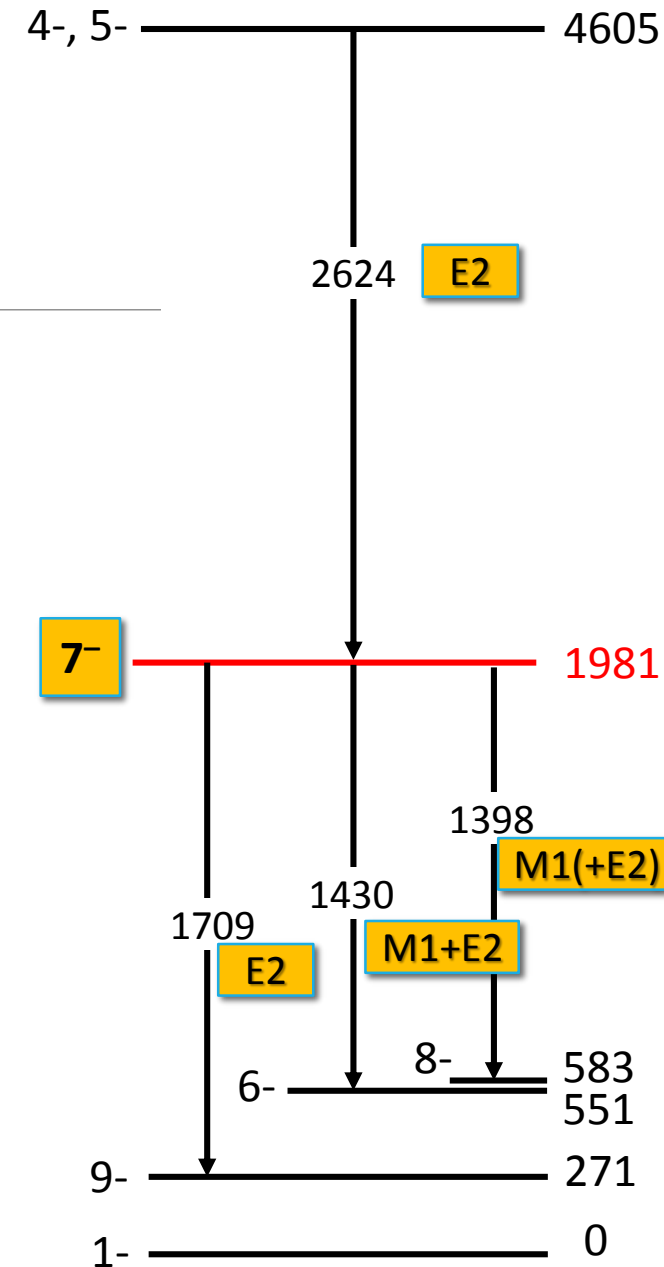
# Spin-parity values: state at 1981 keV



Theory E2-E2  
 $A_2=0.10, A_4=0.01$

$$\delta_{1430}=-0.11(5)$$

$$\delta_{1398}=0.05(5)$$

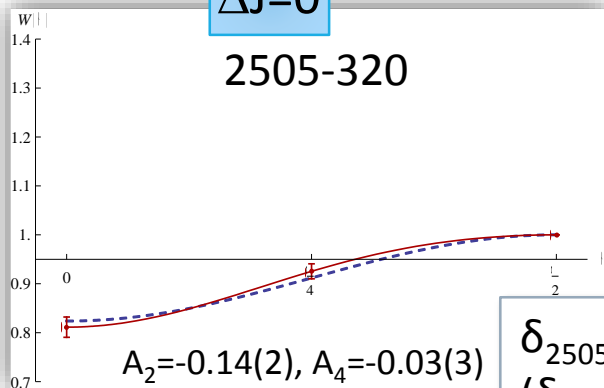


Decays to:  
(6+), (5+), (4+), (4-), (6-), 6-, 4-

# Spin-parity values: state at 2100 keV

$\Delta J=0$

2505-320

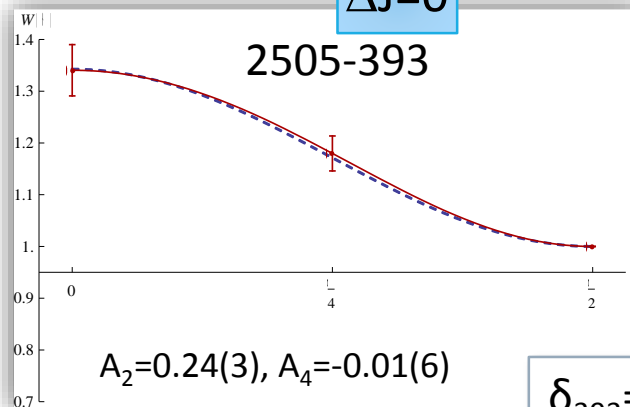


$A_2=-0.14(2)$ ,  $A_4=-0.03(3)$

$\delta_{2505}=0.04(8)$   
( $\delta_{2505}=-0.82(12)$ )

$\Delta J=0$

2505-393

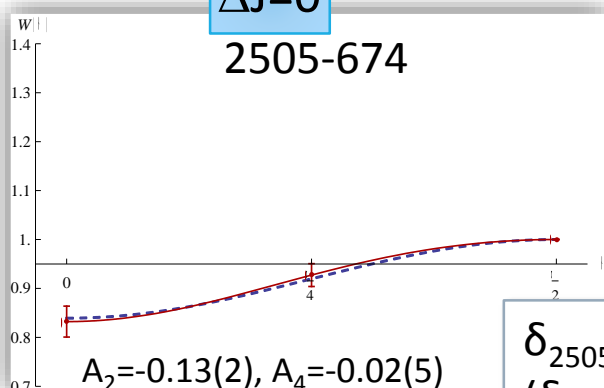


$A_2=0.24(3)$ ,  $A_4=-0.01(6)$

$\delta_{393}=-0.3(3)$

$\Delta J=0$

2505-674

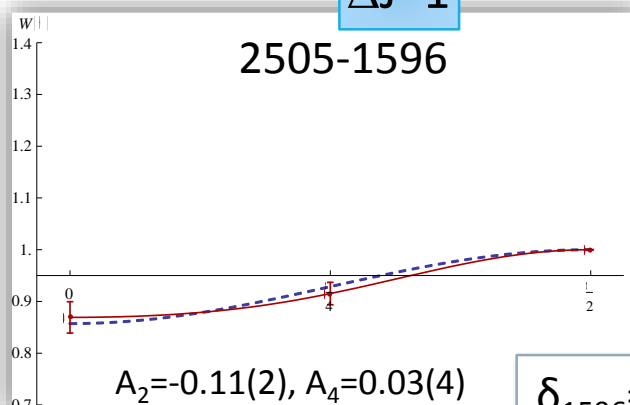


$A_2=-0.13(2)$ ,  $A_4=-0.02(5)$

$\delta_{2505}=0.07(12)$   
( $\delta_{2505}=-0.88(19)$ )

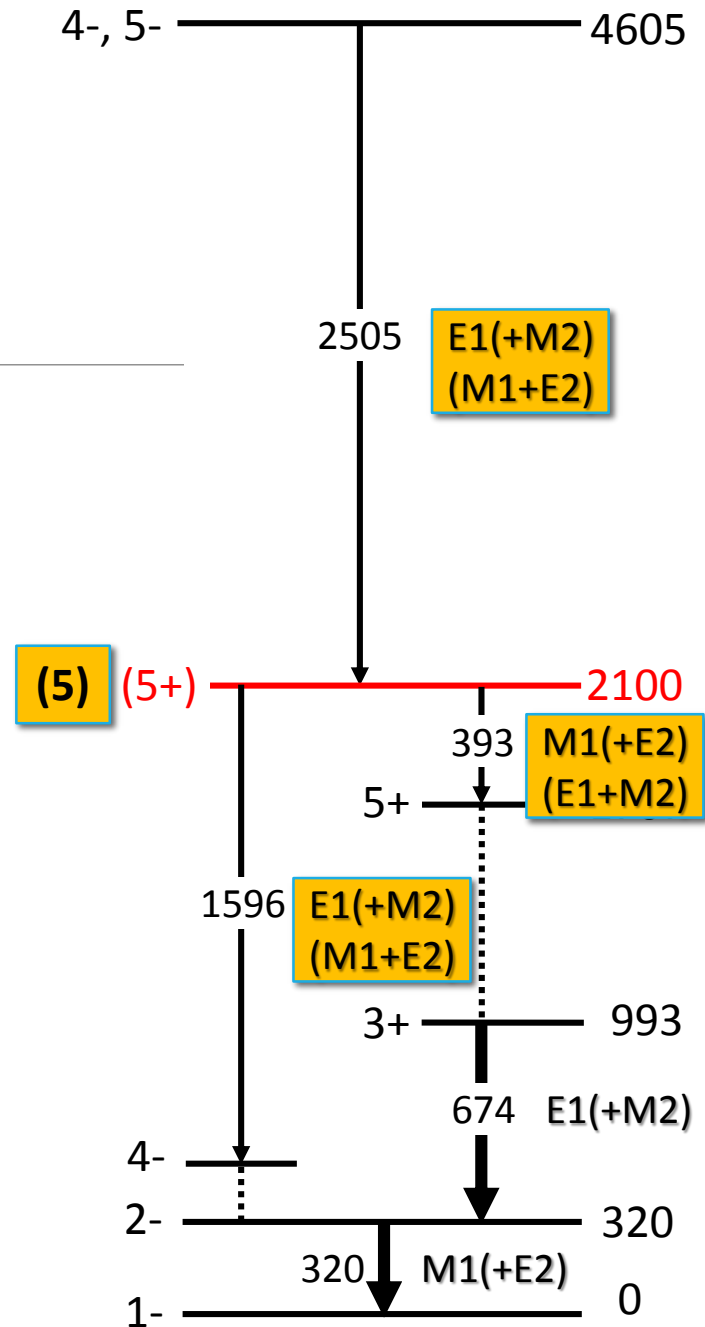
$\Delta J=1$

2505-1596



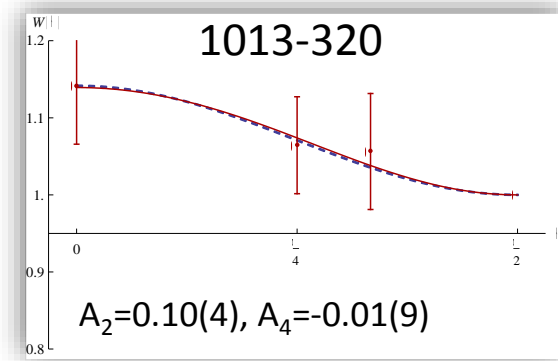
$A_2=-0.11(2)$ ,  $A_4=0.03(4)$

$\delta_{1596}=0.01(3)$

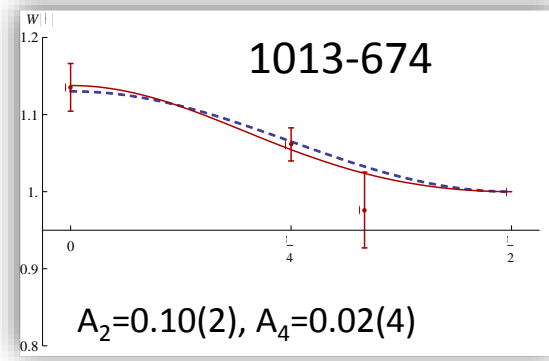


Decays to:  
5+, 4+, 3-, 4-, 3+, 4-, 5-, 3-, 2-

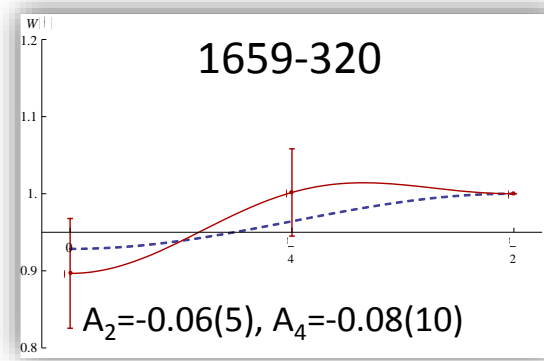
# Spin-parity values: state at 2007 keV



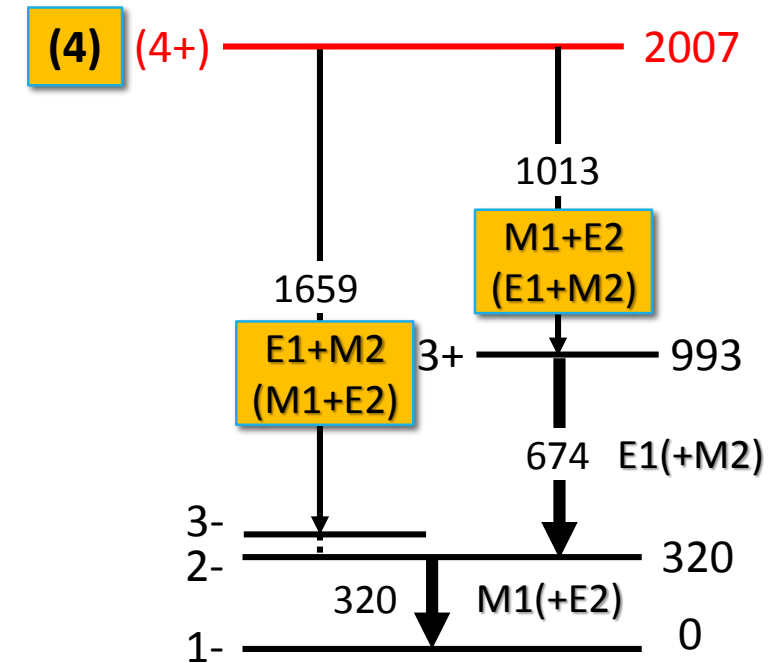
$$\delta_{1013} = -0.11(9)$$



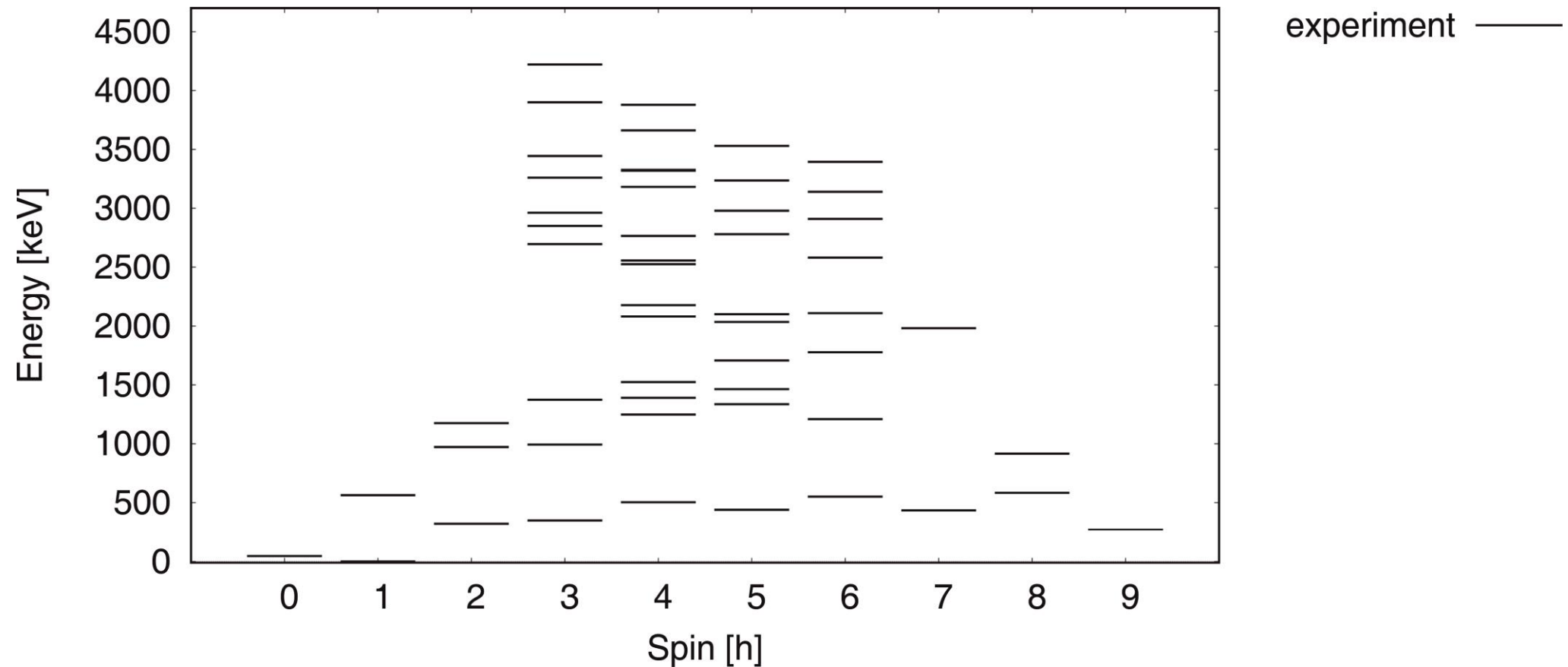
$$\delta_{1013} = -0.10(4)$$



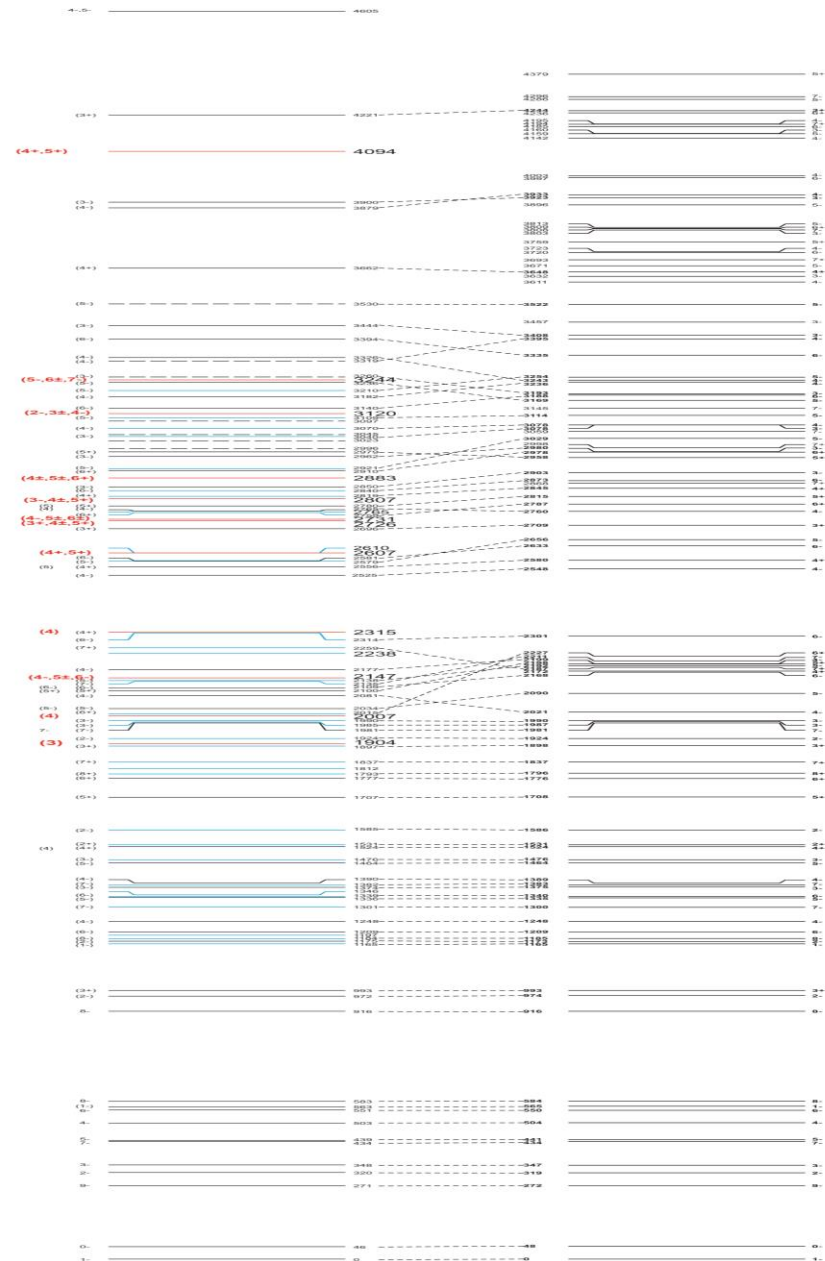
$$\delta_{1659} = 0.23(14)$$



# Spin distribution from $^{209}\text{Bi}(n,\gamma)^{210}\text{Bi}$ reaction



## Comparison with shell-model calculations

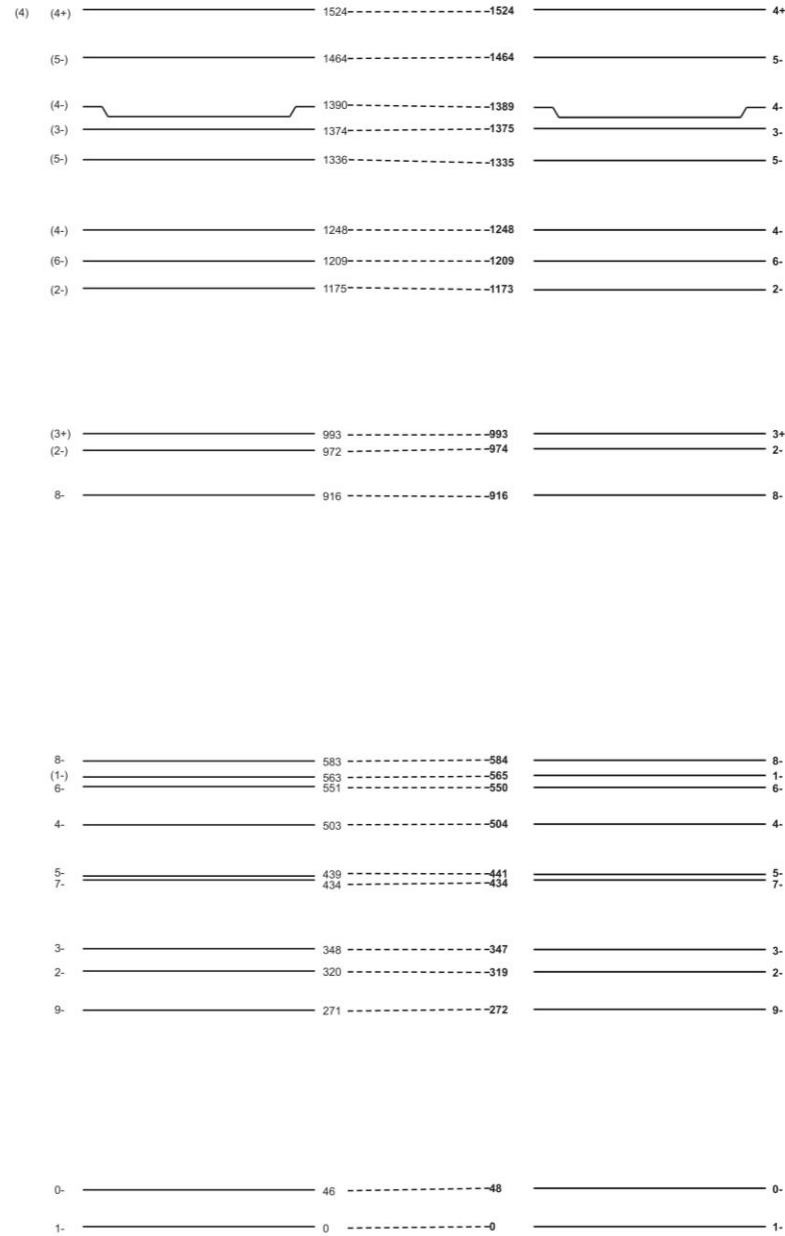


## Experimental results

## Shell-model calculations

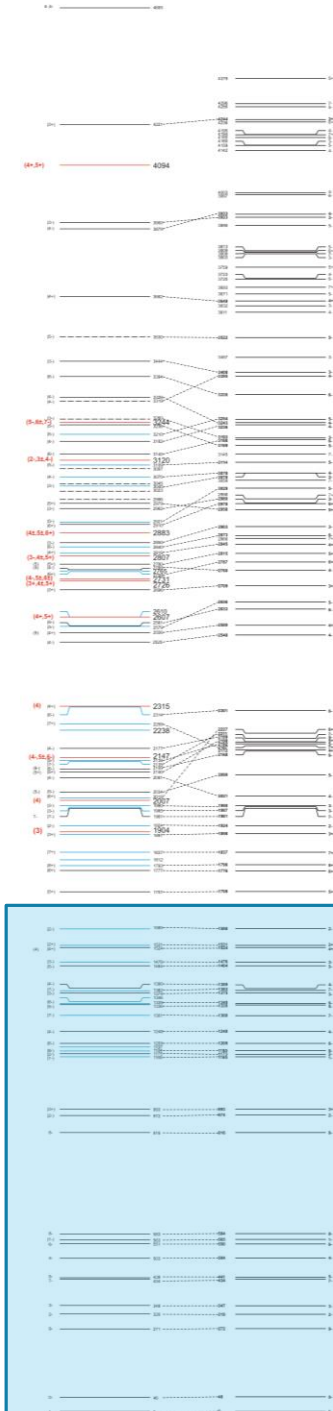


# Comparison with shell-model calculations

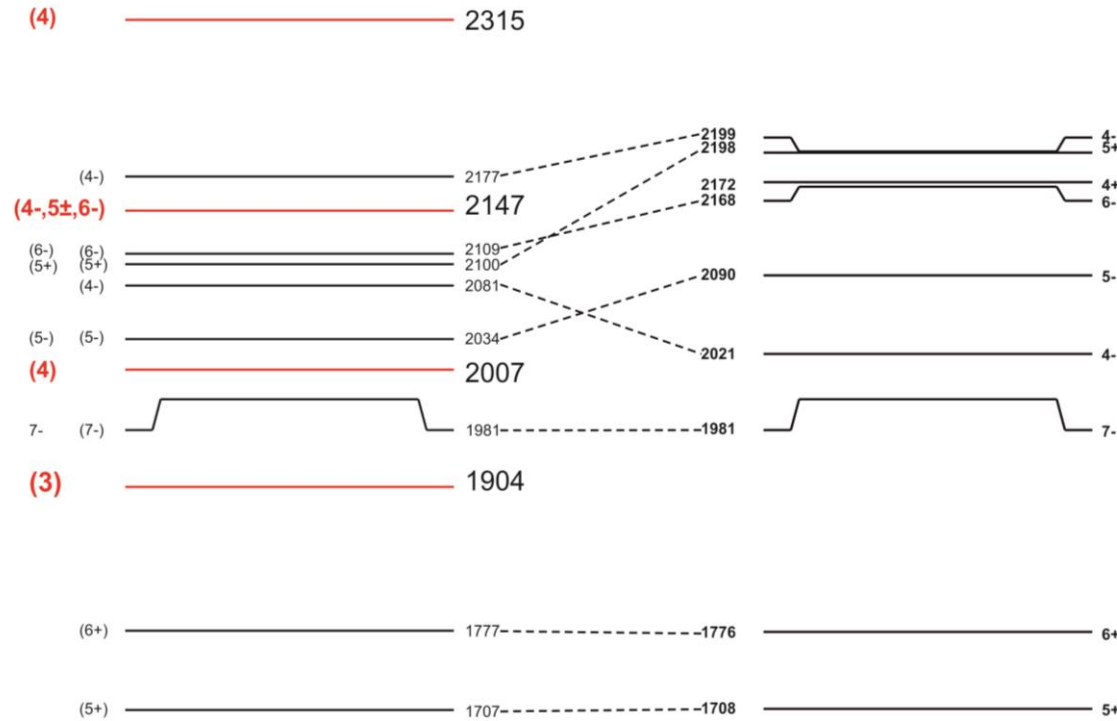


Experimental results

Shell-model calculations

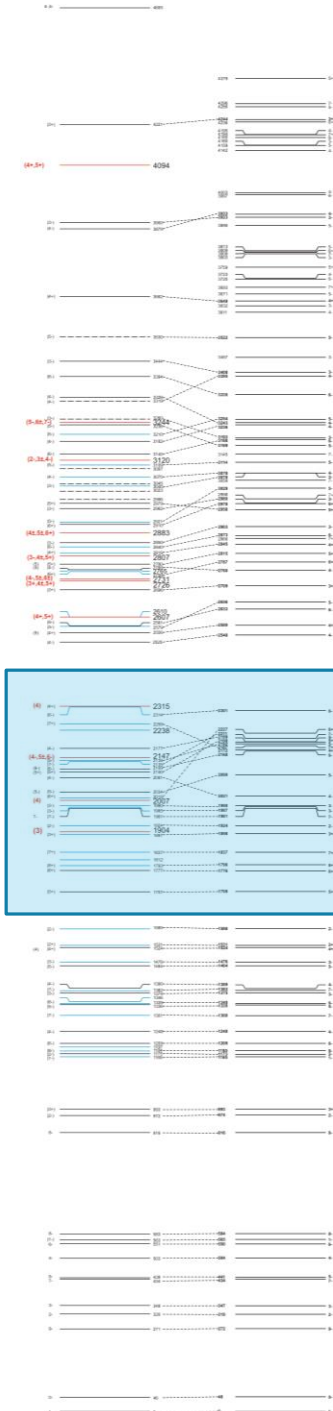


# Comparison with shell-model calculations



Experimental results

Shell-model calculations



# Comparison with shell-model calculations

$3- \times (\pi h_{9/2} \nu g_{9/2})$

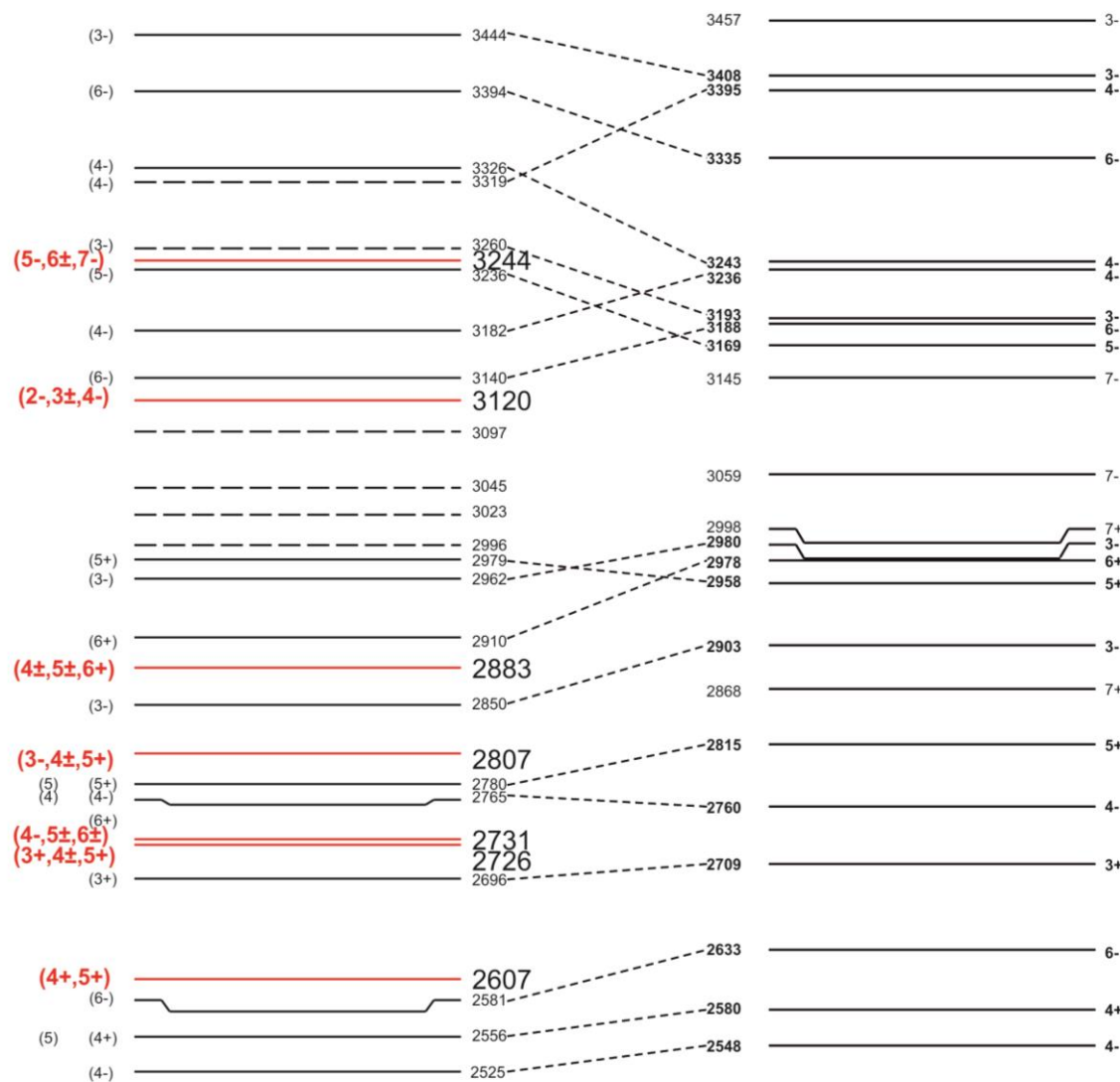
$3- \times 0- \rightarrow 3+$

$3- \times 1- \rightarrow 2+, 3+, 4+$

$3- \times 9- \rightarrow 6+, 7+, 8+, (9+, 10+, 11+, 12+)$

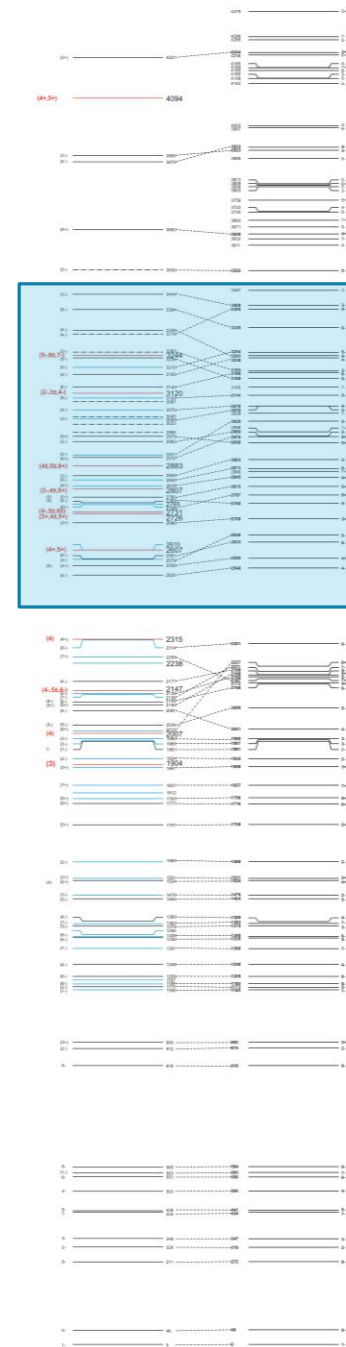
$3- \xrightarrow{2.6 \text{ MeV}}$

$^{208}\text{Pb}$

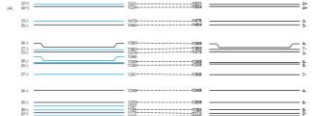
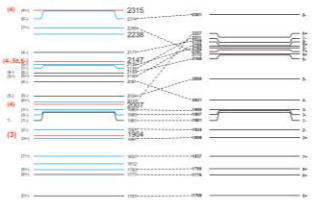
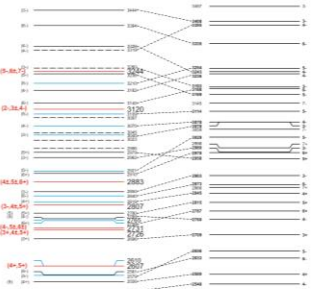
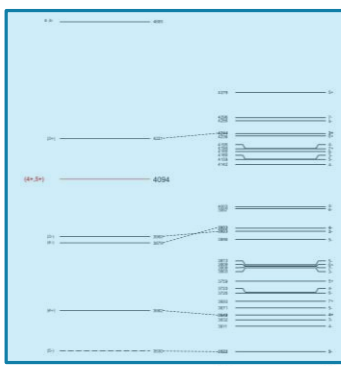
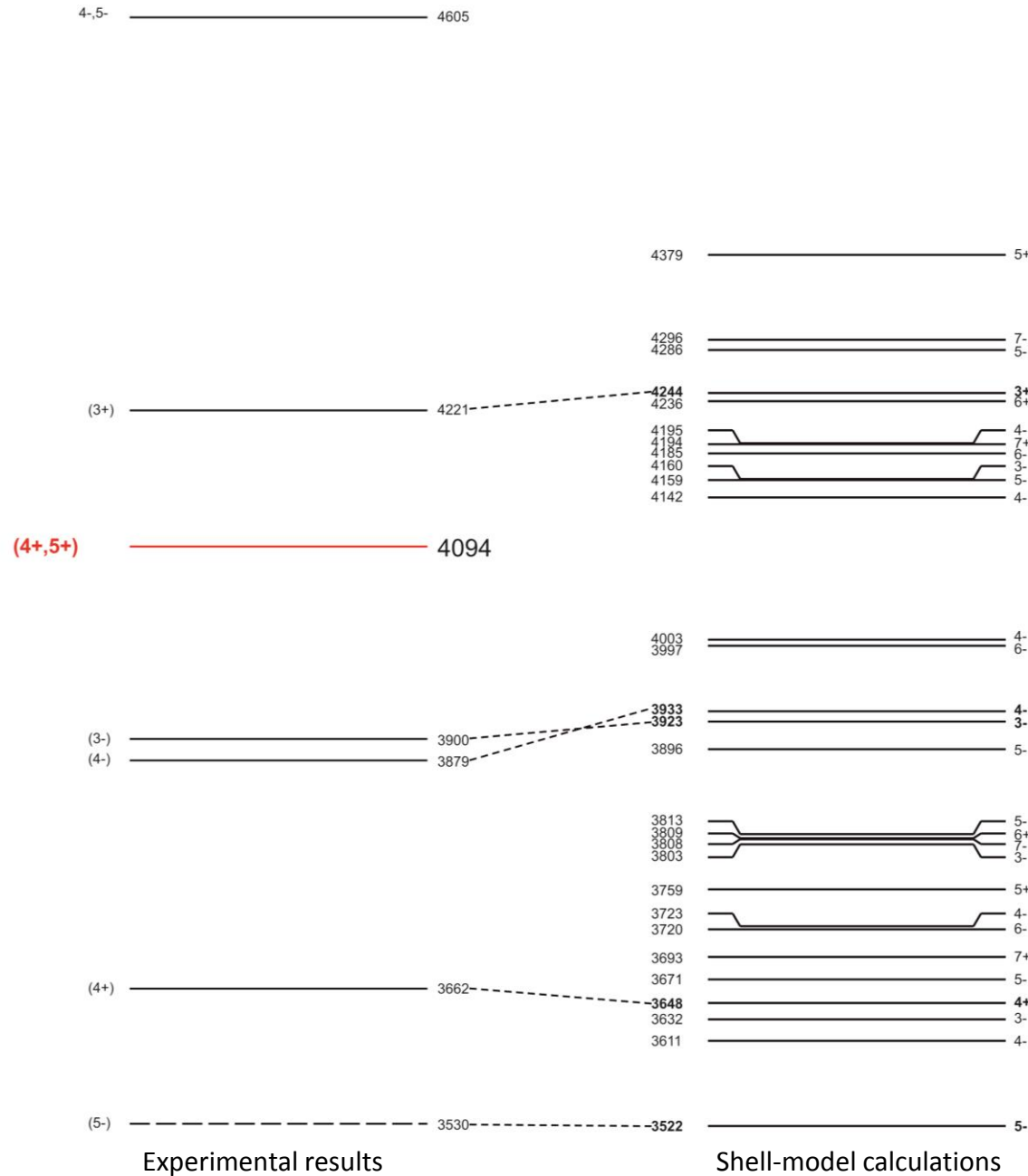


Experimental results

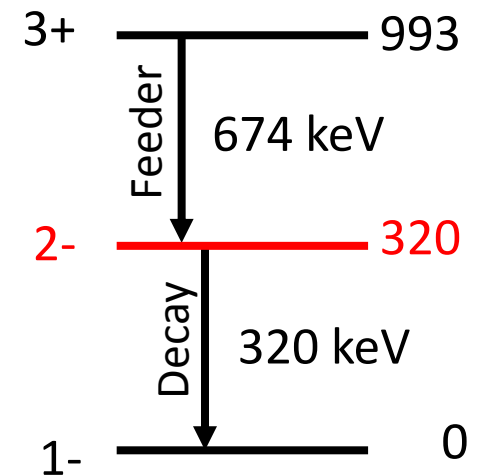
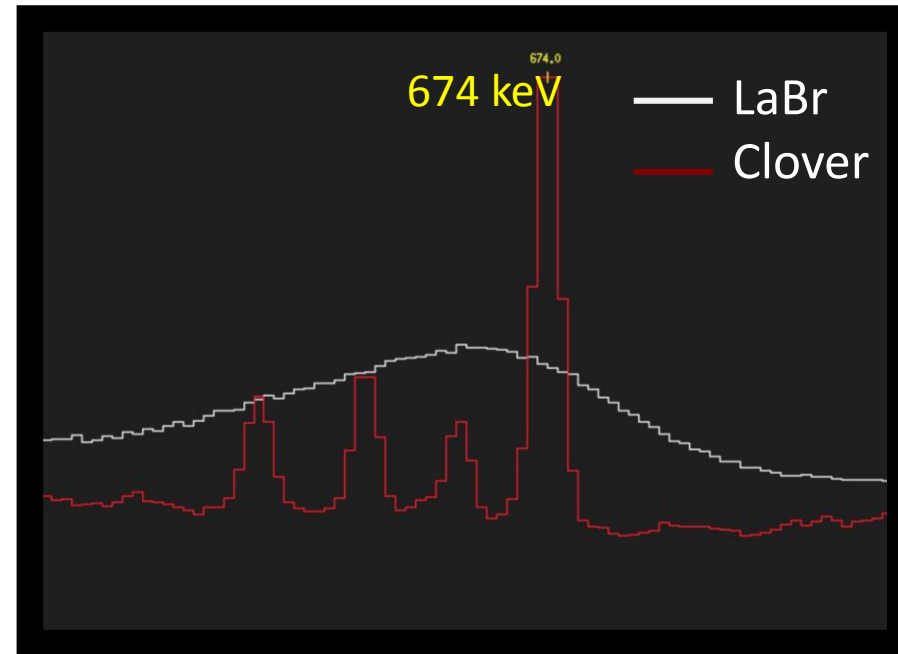
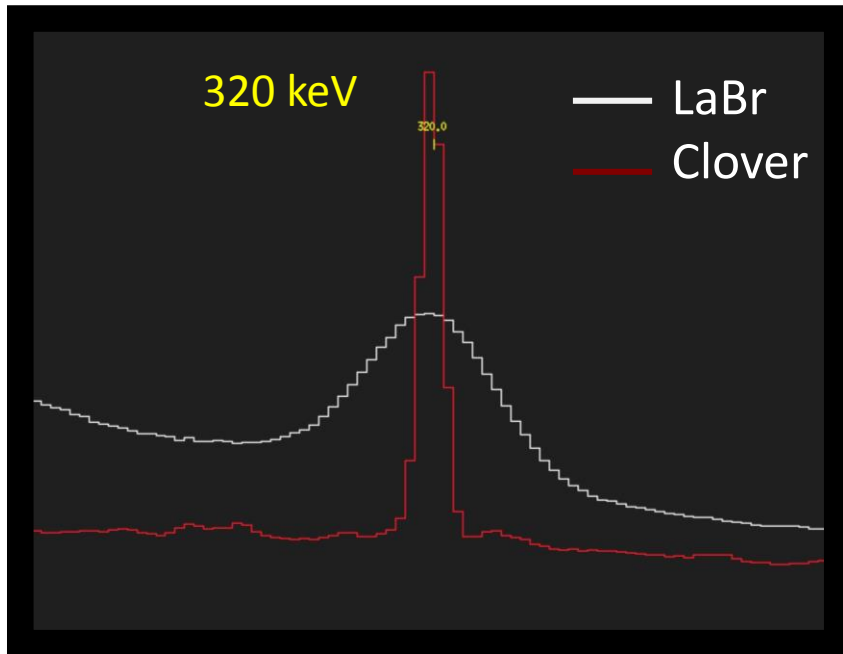
Shell-model calculations



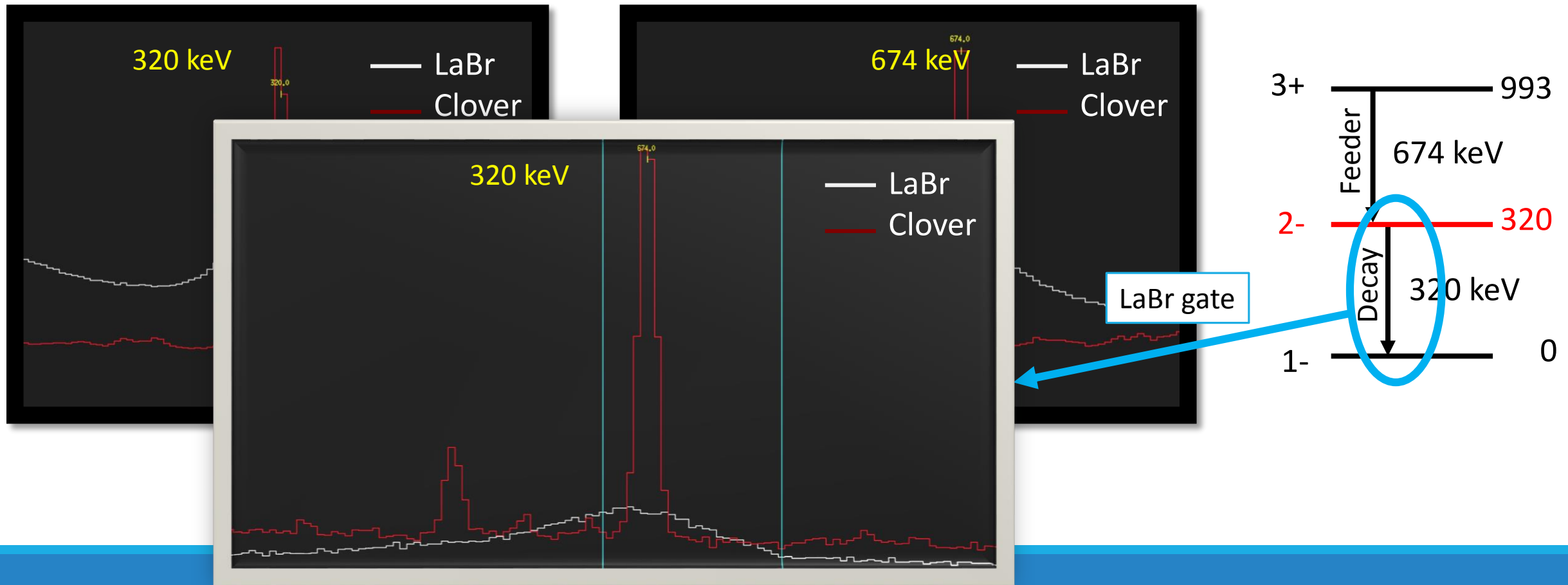
# Comparison with shell-model calculations



# Measurements of the lifetimes of excited states in $^{210}\text{Bi}$



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# Measurements of the lifetimes of excited states in $^{210}\text{Bi}$

$$\tau = \frac{1}{2} \left[ \frac{\Delta C - \Delta C_{\text{compton}}}{\pi} + \Delta C - PRD \right]$$

$$\Delta C = 22 \text{ ps}$$

$$\Delta C_{\text{compton}} = 106.8 \text{ ps}$$

$$PRD (E_{\text{feeder}} - E_{\text{decay}}) = -83.4 \text{ ps}$$

$$\pi = 0.8$$



$$\tau = 2.4 \text{ ps}$$

$$\tau_{\text{lit}} = 7.5(14) \text{ ps}$$

*Phys Rev. C 12, 1547(1975)*

*With this method the lower limit is  
between 5 and 10 ps*

# Summary

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- The level structure of  $^{210}\text{Bi}$  investigated in cold neutron capture on  $^{209}\text{Bi}$  was compared to shell model calculations – some of the states must come from the core excitations.
- The analysis of angular correlations allowed to confirm almost pure M1 character of the main transition leading to the ground state.
- The results of present analysis of  $^{210}\text{Bi}$  structure, including the measurements of the lifetimes will serve as an excellent testing ground for the future calculations.

**Thank you for your attention!**