

# 2 FACETS OF DARK MATTER

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Rencontre de Physique des Particules  
Institut Henri Poincaré  
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# WHY DARK MATTER?



# WHICH DARK MATTER?

OBSERVATIONS CONSISTENT  
WITH DM BEING MADE OF  
MASSIVE NON-LUMINOUS OBJECTS

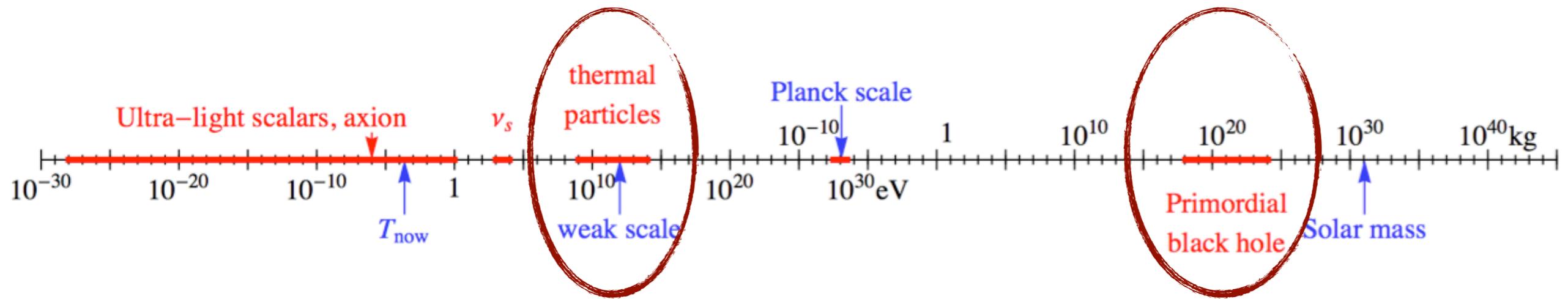
ie

A MASSIVE NEUTRAL PARTICLE WOULD DO

but

OTHER POSSIBILITIES ARE STILL “ALIVE AND WELL”

# WHICH DARK MATTER?



**ON A SIMPLIFIED  
WIMP MODEL**

**ON CONSTRAINTS ON  
PRIMORDIAL BLACK  
HOLES AS DM**

# I. DM AS PRIMORDIAL BLACK HOLES (PBH)

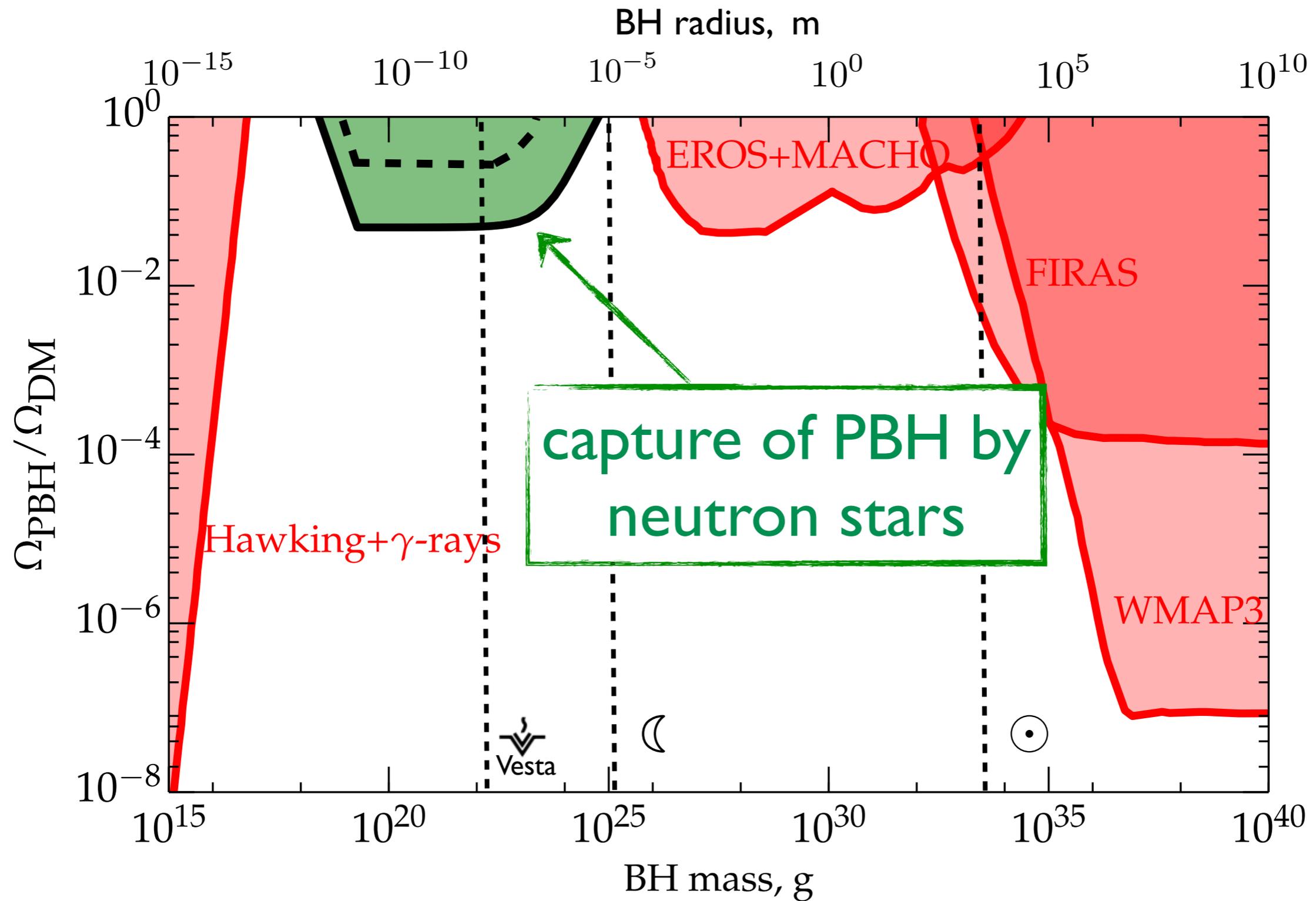
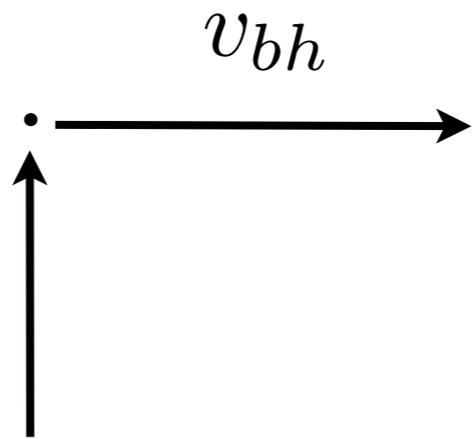


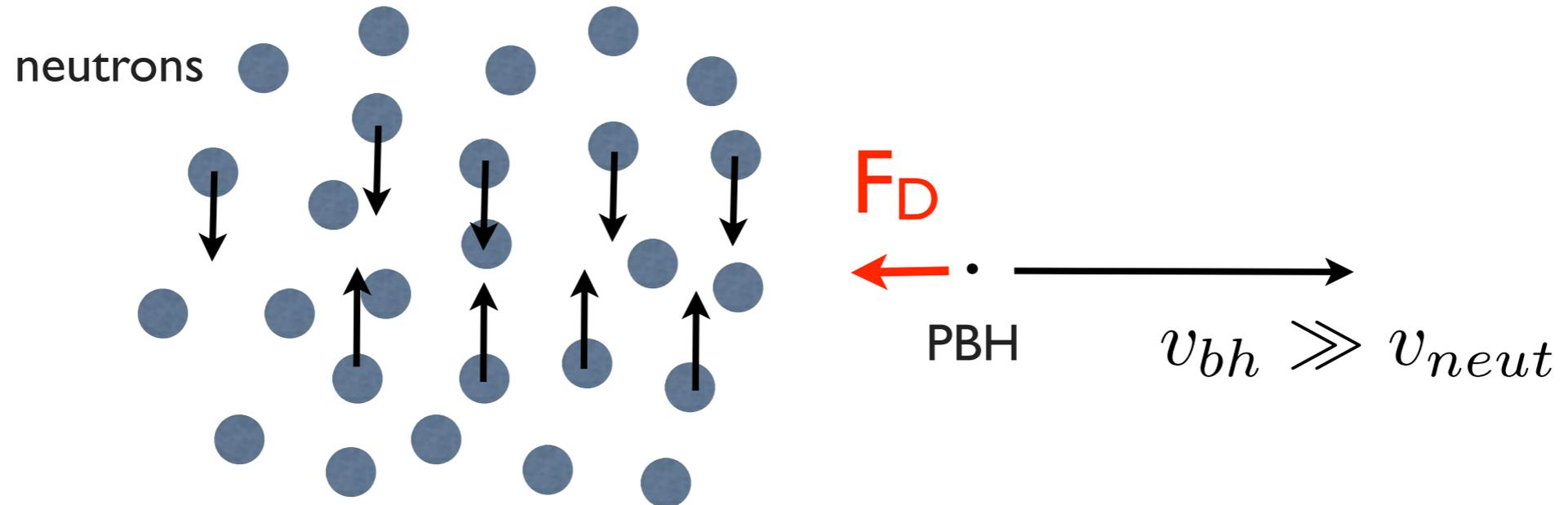
Fig. from 1301.4984  
Capela, Pshirkov & Tinyakov



**Primordial Black Hole**

**Neutron Star**  
(not to the scale)

# PBH CAPTURE BY DYNAMICAL FRICTION



$$-\frac{dE}{dx} \approx \frac{4\pi G^2 M_{bh}^2 \rho}{v_{bh}^2} \log \frac{b_{max}}{b_{min}}$$



$$E_{loss} \sim \frac{GM_{bh}^2}{R_{ns}}$$

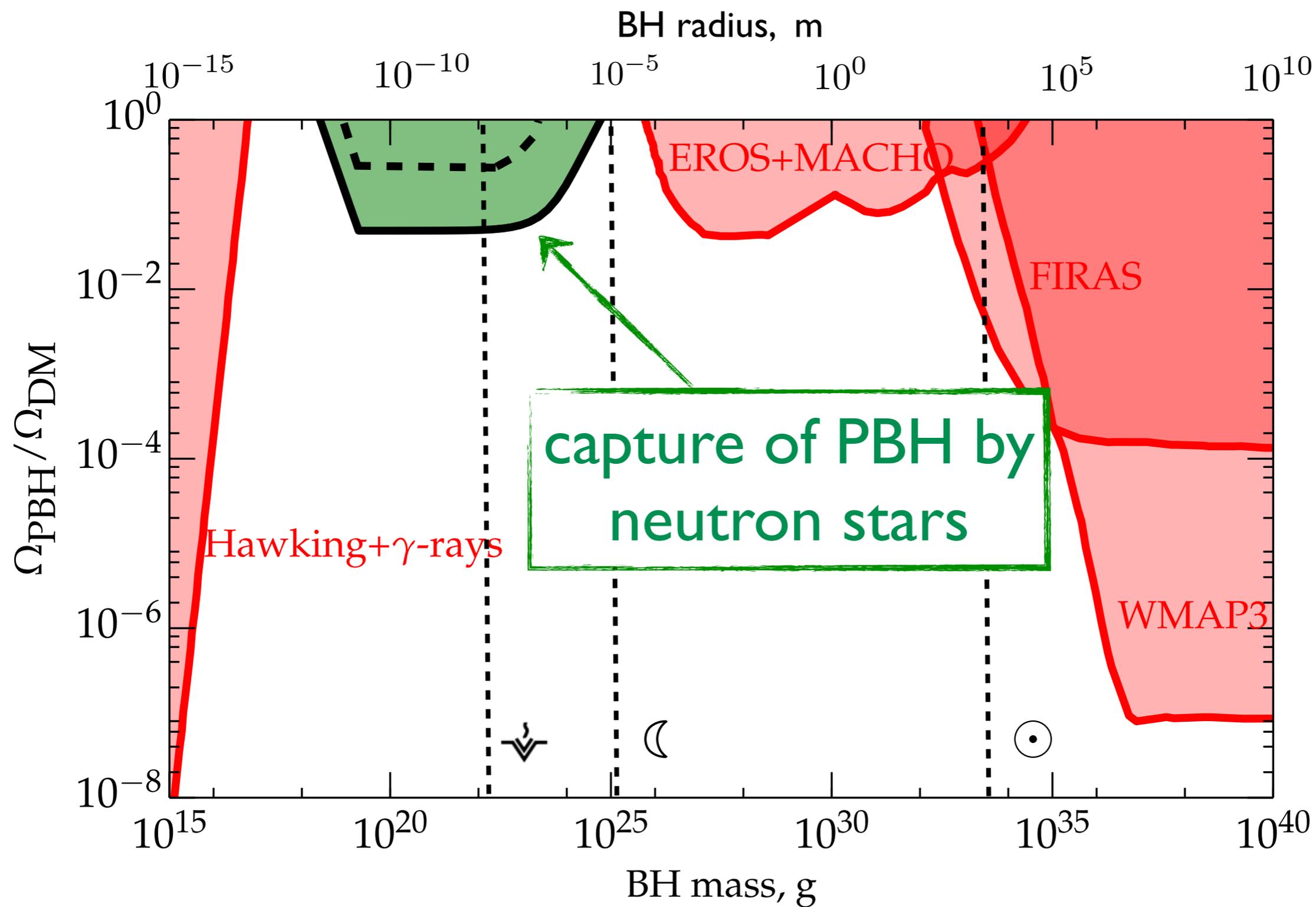


Fig. from 1301.4984  
 Capela, Pshirkov & Tinyakov

# Tidal capture of a primordial black hole by a neutron star: implications for constraints on dark matter

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<sup>b</sup>Institute for Theory and Computation, Harvard-Smithsonian CfA, 60 Garden Street, Cambridge MA 02138, USA

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**Abstract.** In a close encounter with a neutron star, a primordial black hole can get gravitationally captured by depositing a considerable amount of energy into nonradial stellar modes of very high angular number  $l$ . If the neutron-star equation of state is sufficiently stiff, we show that the total energy loss in the point-particle approximation is formally divergent. Various mechanisms – including viscosity, finite-size effects and the elasticity of the crust – can damp high- $l$  modes and regularize the total energy loss. Within a short time, the black hole is trapped inside the star and disrupts it by rapid accretion. Estimating these effects, we predict that the existence of old neutron stars in regions where the dark-matter density  $\rho_{\text{DM}} \gtrsim 10^2 (\sigma/\text{km s}^{-1}) \text{GeV cm}^{-3}$  (where  $\sigma$  is the dark-matter velocity dispersion) limits the abundance of primordial black holes in the mass range  $10^{17} \text{g} \lesssim m_{\text{PBH}} \lesssim 10^{24} \text{g}$ , which was previously unconstrained. In combination with existing limits, our results suggest that primordial black holes cannot be the dominant dark matter constituent.

$$E_{\text{loss}} \sim \frac{GM_{bh}^2}{R_{ns}} \sum_{l=2}^{l_{max}} \frac{1}{l^n}$$

same as  
Dynamical  
Friction (DF)

but sum on modes  
(spherical harmonics)  
formally **divergent**  
(worse case:  $n=0$  for an  
incompressible fluid)

Compared to DF, claim an enhancement of  $O(10^6-10^9)$

# CONSTRAINTS ON PRIMORDIAL BH

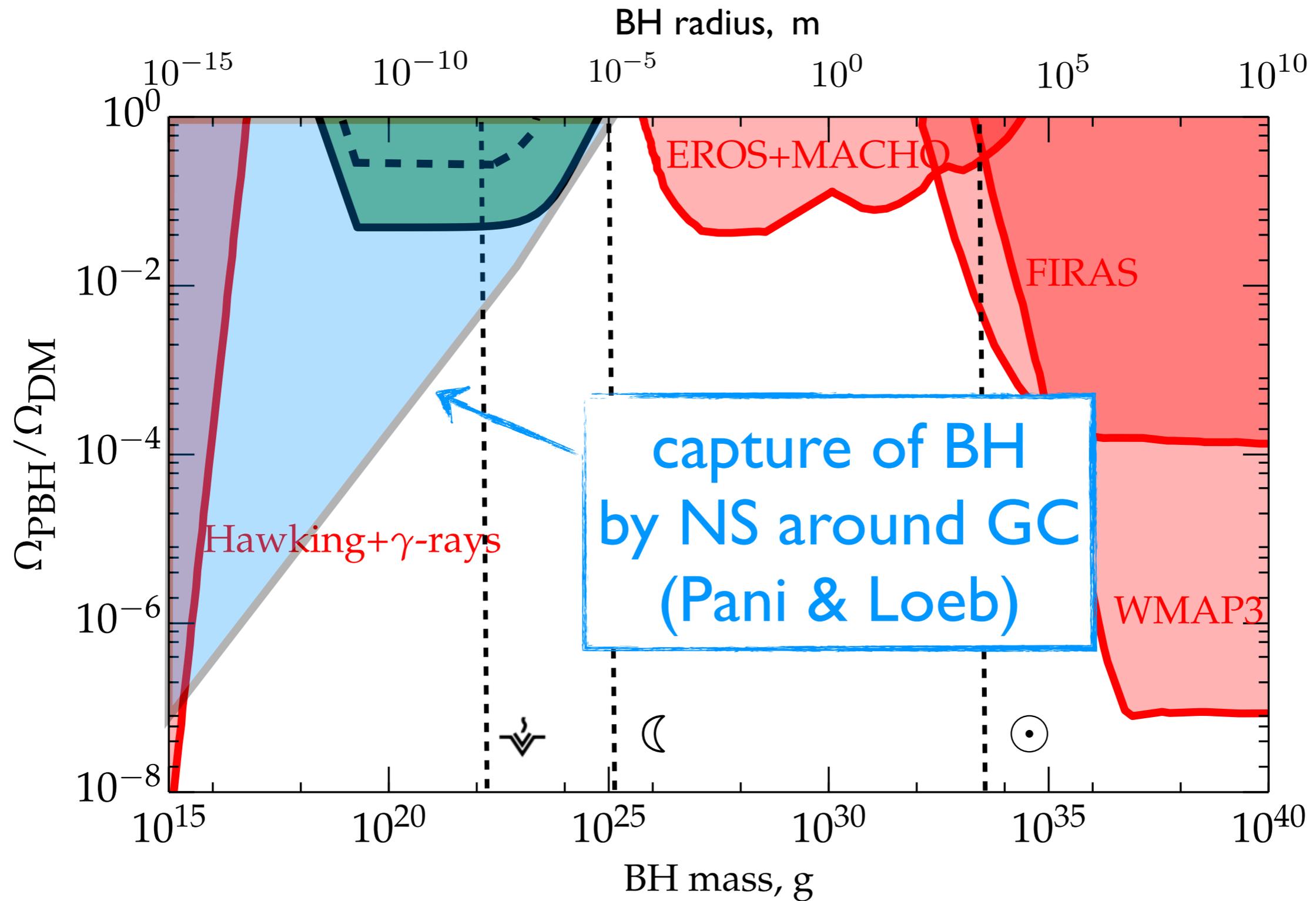


Fig. from 1301.4984  
Capela, Pshirkov & Tinyakov

Basically EXCLUDES Primordial Black Holes as  
the dominant form of DM

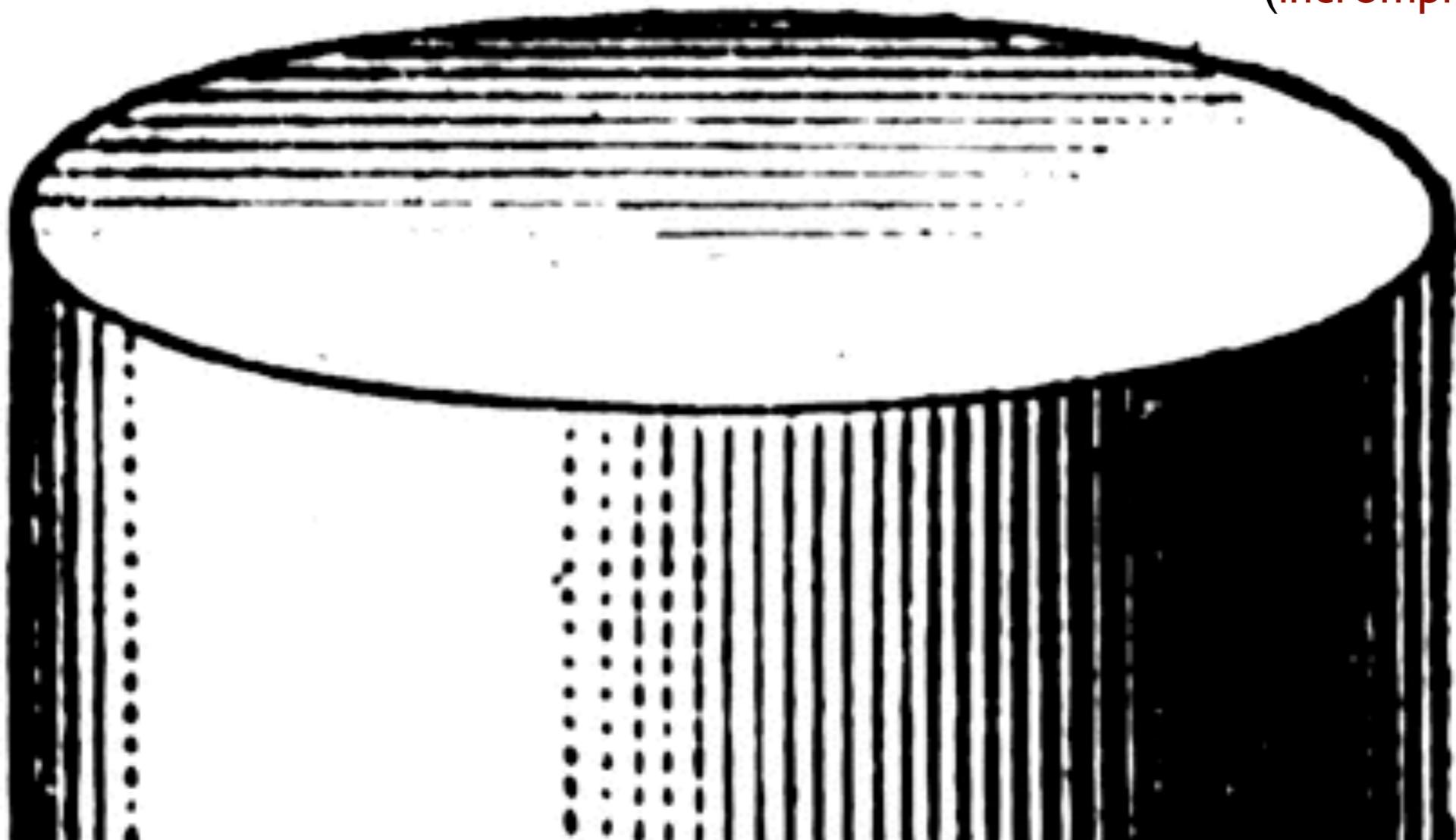
Very interesting (actually important)  
but unfortunately **INCORRECT** (we think)

It's a UV problem, so we went **planar**

primordial black hole  $\longrightarrow$   $\cdot$

$v_{bh}$

a flat 'neutron star'  
(**incompressible fluid**)



It's a UV problem, so we went **planar**

primordial black hole  $\longrightarrow$   $\cdot$   
 $\downarrow$   $v_{bh}$

a flat 'neutron star'  
(**incompressible fluid**)



In this limit the problem may be solved analytically  
(instead of numerically)

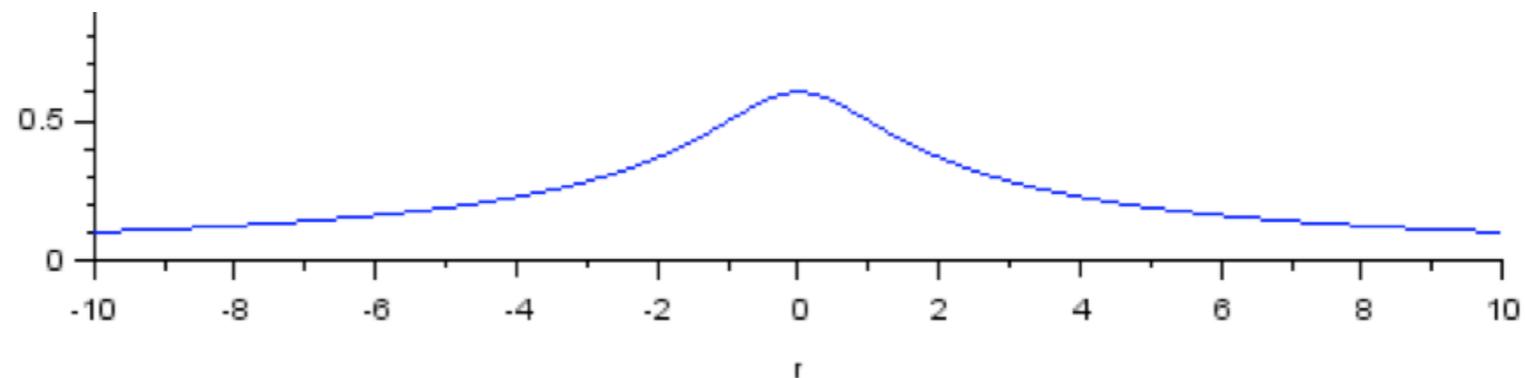
# SURFACE DEFORMATION

$$\eta(t, r) = \frac{GM_{bh}}{g} \int dk \frac{1}{1 + kv_{bh}^2/g} \left[ e^{-kv_{bh}|t|} + 2\theta(t)v_{bh}\sqrt{\frac{k}{g}} \sin(\omega_k t) \right] J_0(kr)$$

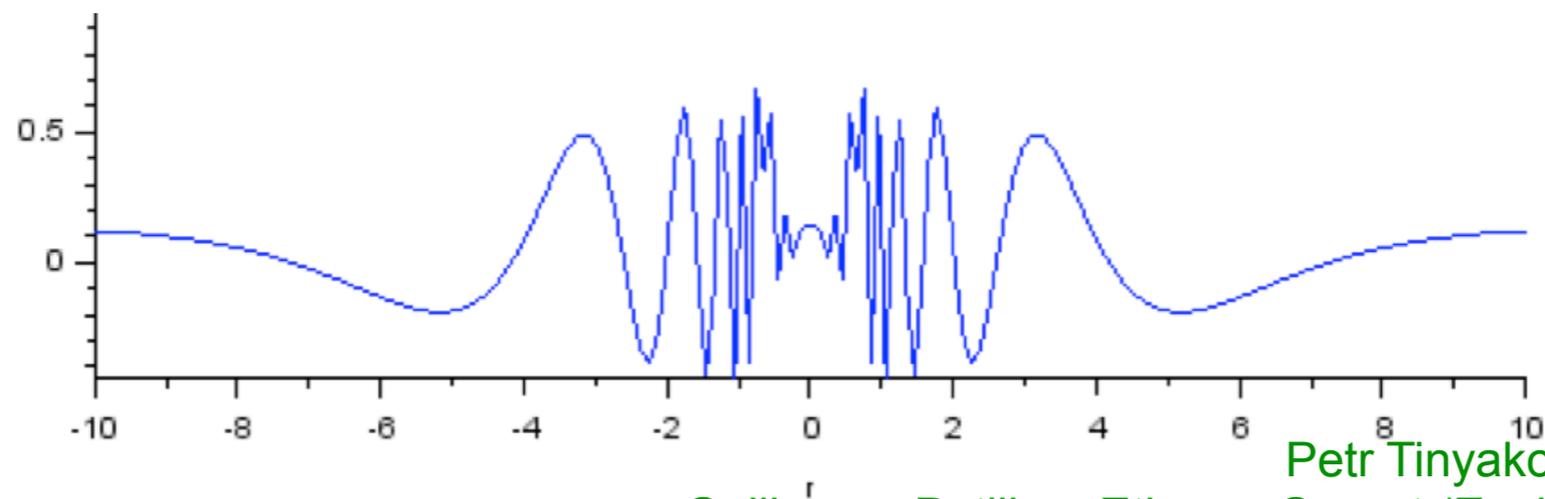
mode velocity  $v_{wave} = \sqrt{\frac{g}{k}}$

modes with  $v_{wave} \lesssim v_{bh}$  (i.e. high  $k$  or high  $l$ ) are not excited!

$t < 0$



$t > 0$





# ENERGY LOSS FROM TIDAL DEFORMATION

$$E_{loss} = \frac{4\pi\rho GM_{BH}^2 v_{BH}^2}{g^2} \int dk \frac{1}{(1 + kv_{bh}^2/g)^2}$$

$$= 4\pi\rho \frac{G^2 M_{bh}^2}{g} \approx \frac{GM_{bh}^2}{R_{ns}}$$



**SIMILAR TO DYNAMICAL FRICTION**  
(ie **nothing new** from tidal deformation)

# CONSTRAINTS ON PRIMORDIAL BH

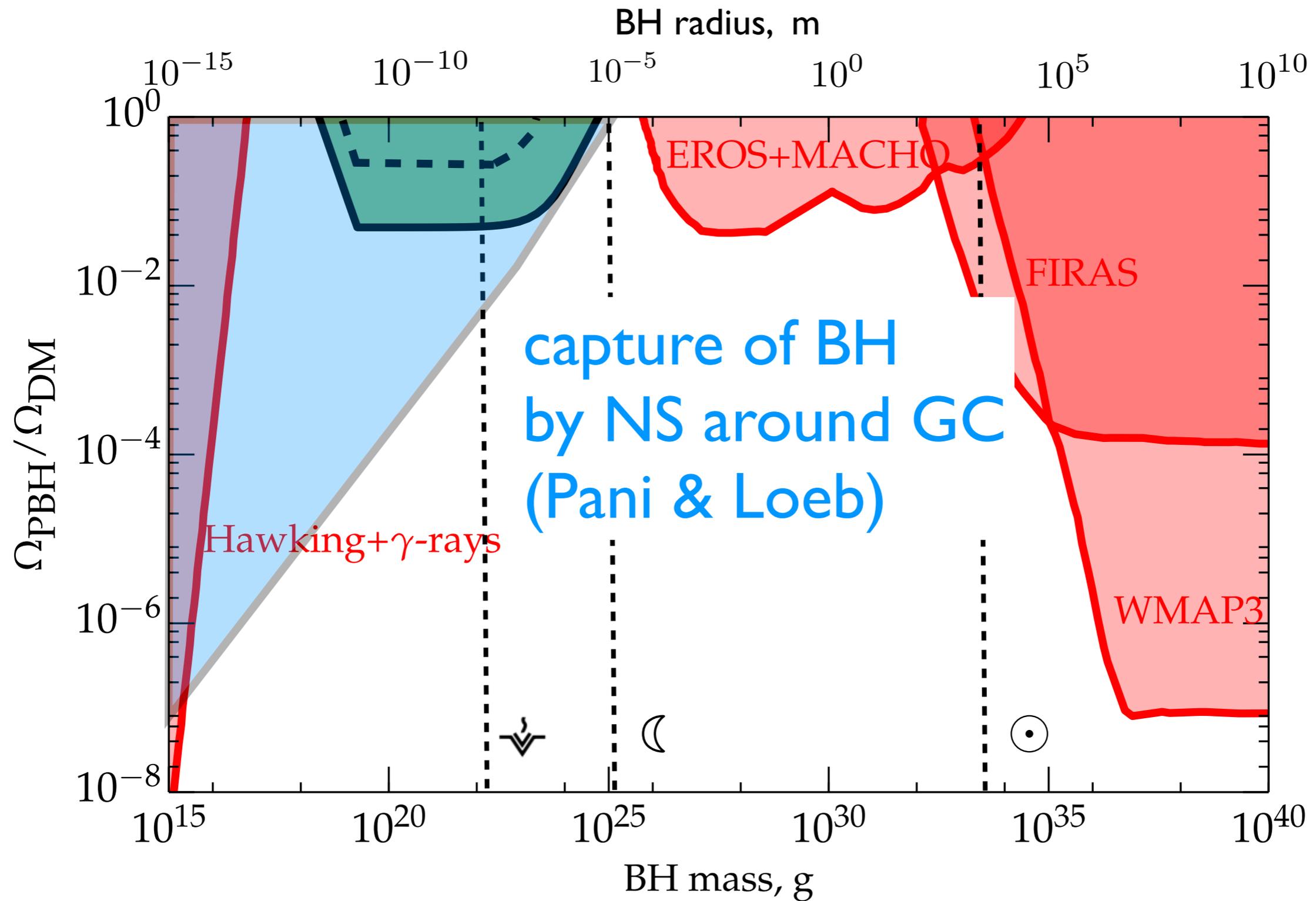


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# CONSTRAINTS ON PRIMORDIAL BH

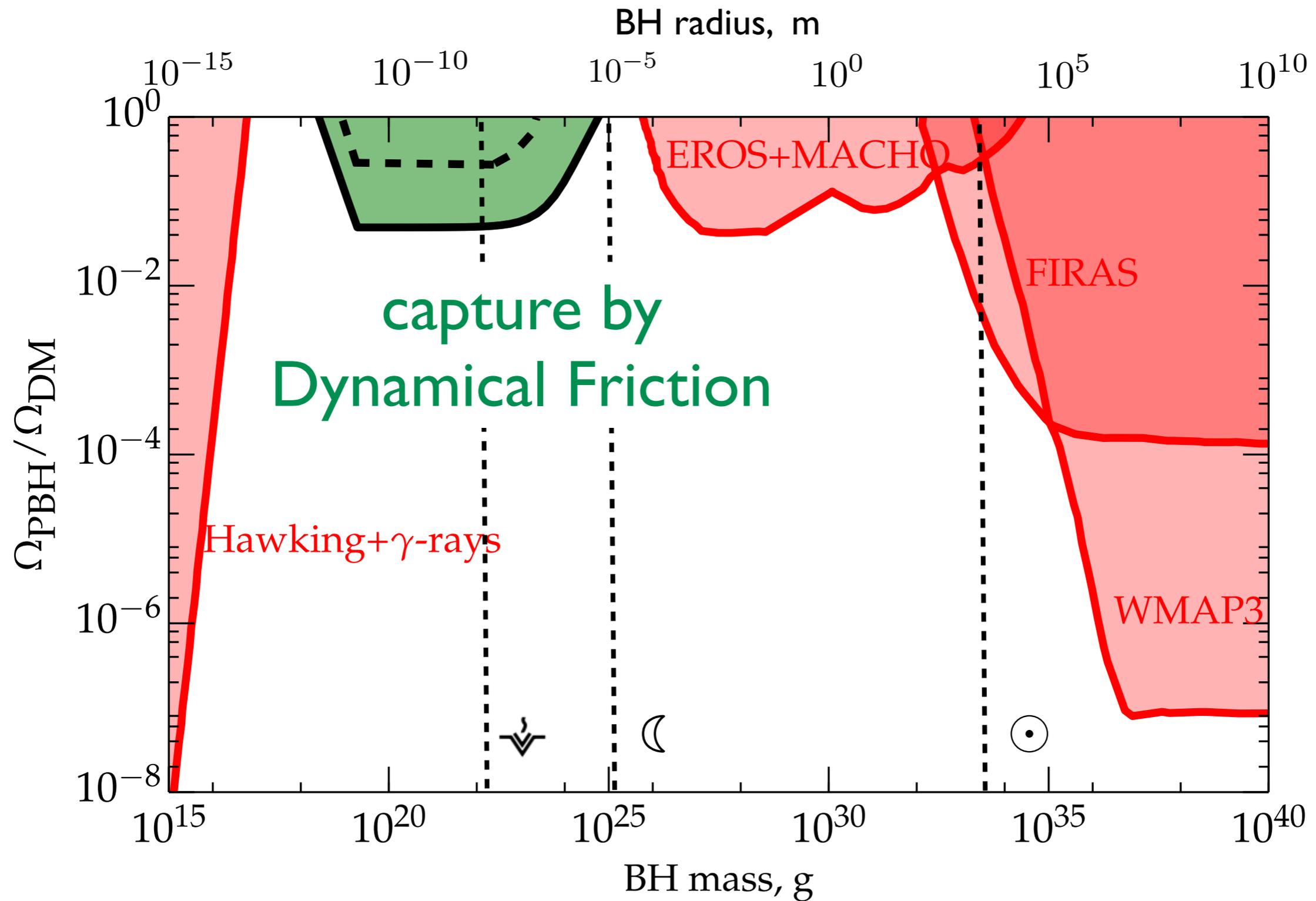
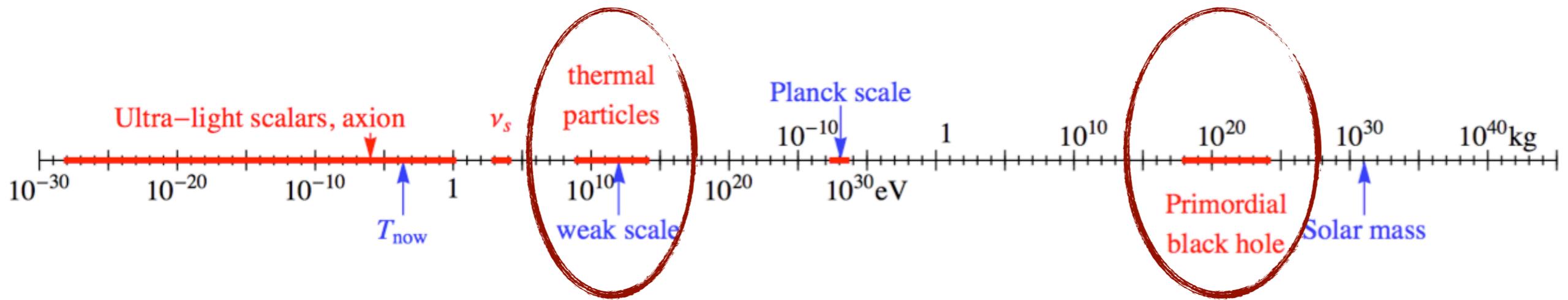


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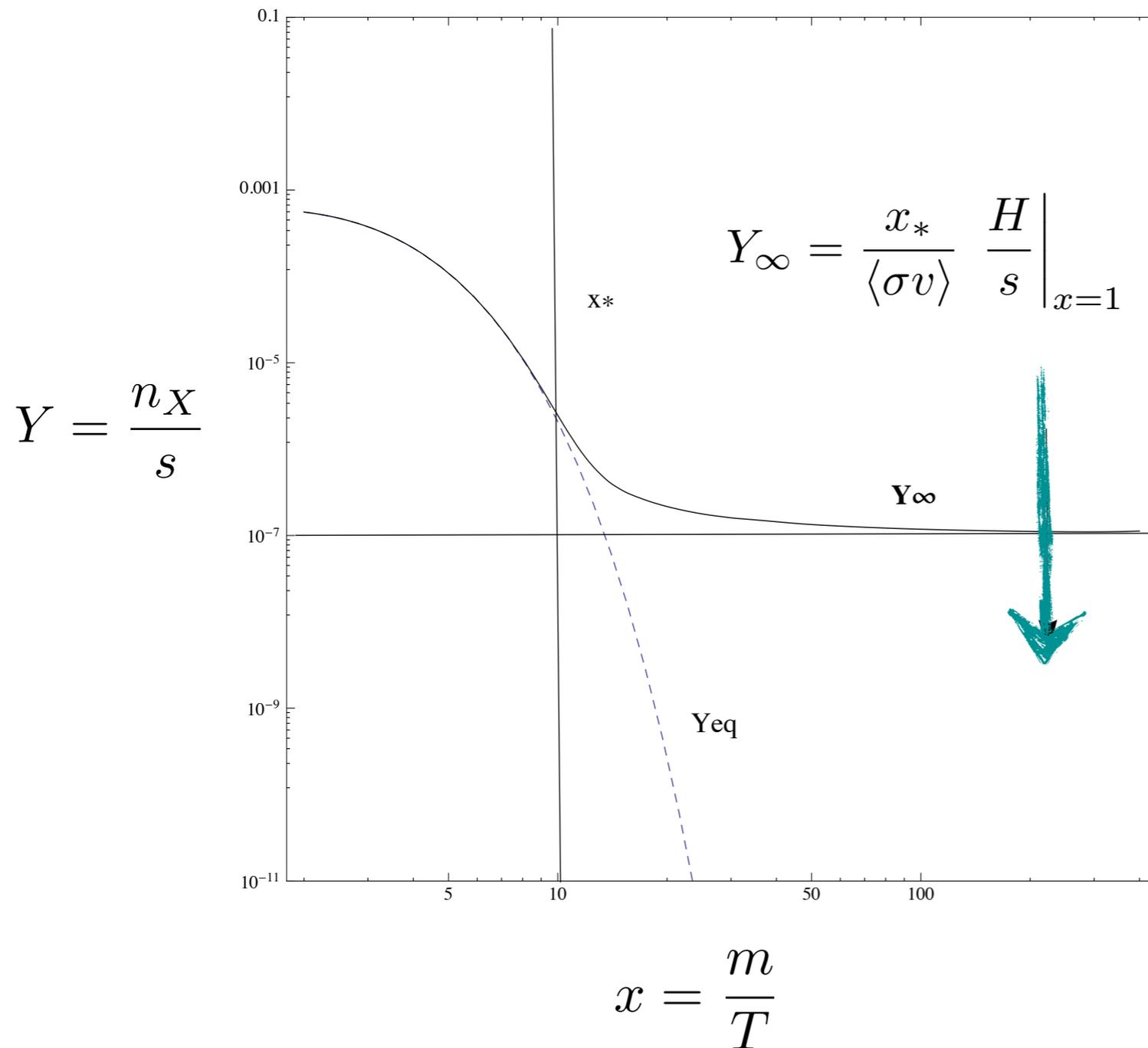
# WHICH DARK MATTER?



ON A SIMPLIFIED  
WIMP MODEL

ON CONSTRAINTS ON  
PRIMORDIAL BLACK  
HOLES AS DM

# A MASSIVE PARTICLE WITH A WEAK INTERACTION OR WIMP COULD HAVE THE RIGHT ABUNDANCE



relic abundance  
from  
thermal freeze-out

cosmology requires

$$\langle \sigma v \rangle \approx 3 \cdot 10^{-26} \text{cm}^3 \cdot \text{s}^{-1}$$

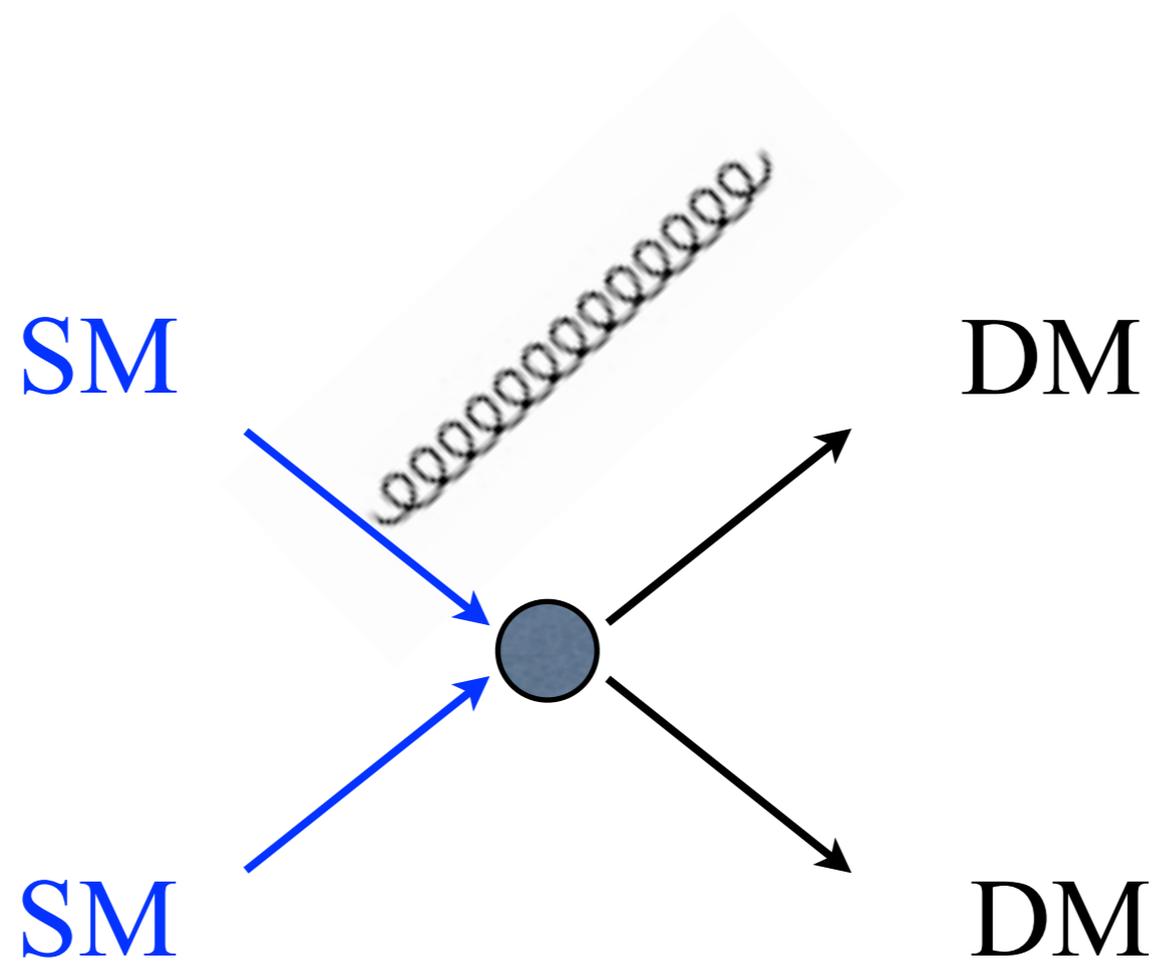
ie a “weak scale”  
cross section

A MASSIVE PARTICLE WITH A WEAK INTERACTION  
OR WIMP COULD HAVE THE RIGHT ABUNDANCE



SOME CALL IT A MIRACLE

# ULTIMATE TEST OF THE WIMP HYPOTHESIS



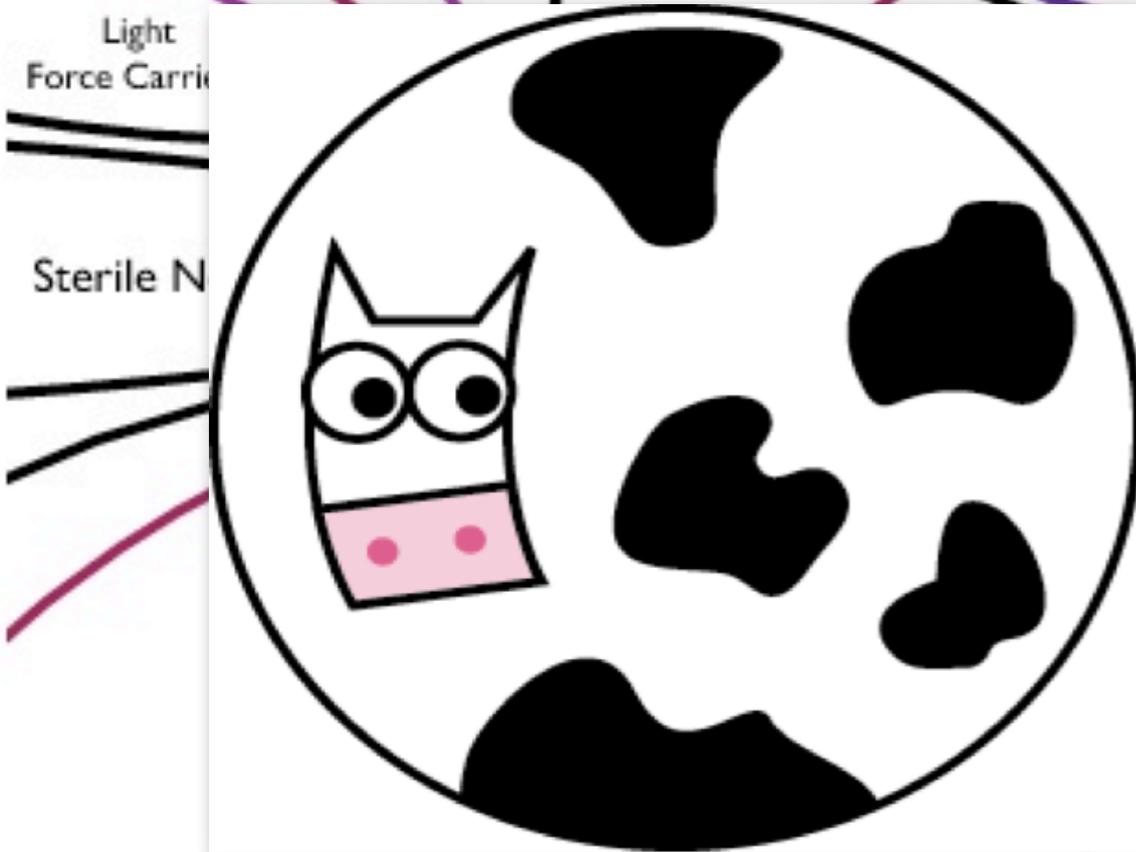
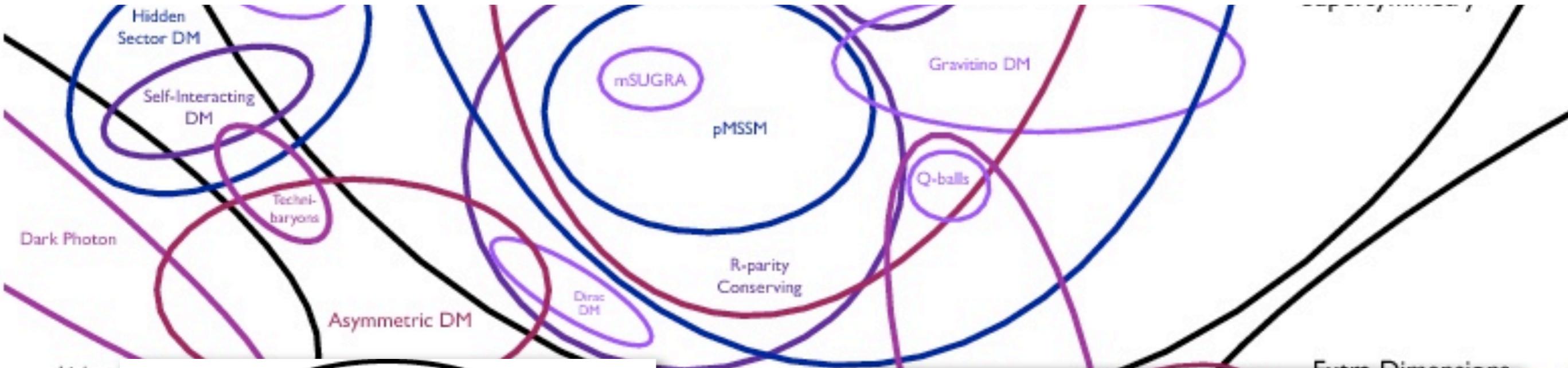
**DM CREATION AT THE LHC!**

MSSM

R-parity violating

NMSSM

# WHICH DARK MATTER?



QCD Axions



Axion-like Particles

Littlest Higgs

THIS **PLETHORA** OF DM CANDIDATES

(and, arguably, the absence -so far- of SUSY at the LHC)

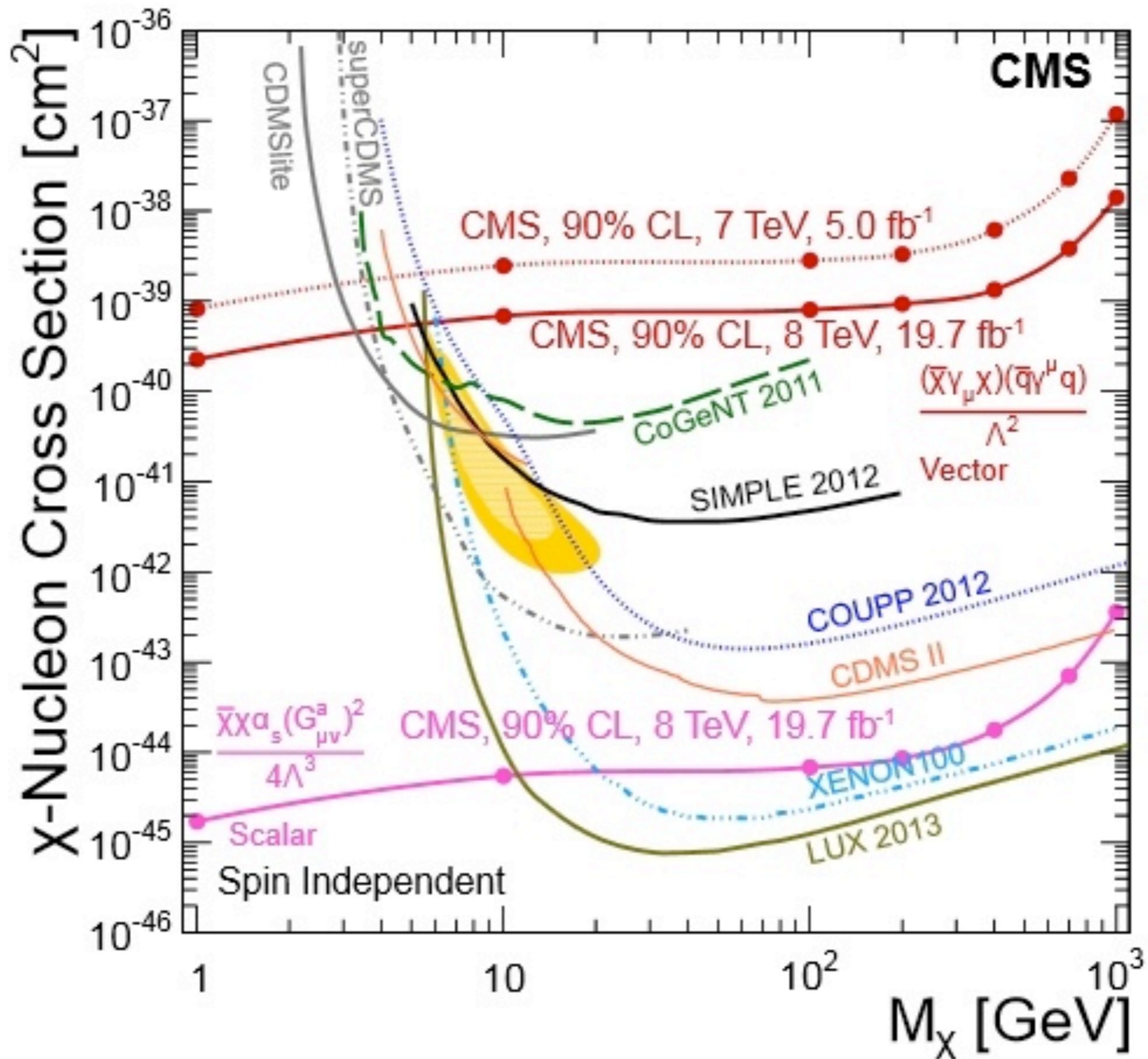
has motivated the use of

**EFFECTIVE OPERATORS**

ie

**A MODEL INDEPENDENT APPROACH**

5 orders of magnitude!?



# INTERPRETATION OF RESULTS BASED ON EFFECTIVE OPERATORS REQUIRES CAUTION

\* MAYBE PHYSICALLY INCONSISTENT \*

\* MAY GIVE BIASED CONCLUSIONS \*

\* LOSS OF SIGNIFICANT INFORMATION \*

# A New Trend (?)

## SIMPLIFIED WIMP MODELS

PARAMETERIZE EXPERIMENTAL SIGNATURES  
WITH FEW PARAMETERS:

i.e.

MASS OF DM & MEDIATOR + COUPLING(S)

PROVIDE CONSISTENT CORRESPONDENCE BETWEEN  
COMPLEMENTARY SEARCHES

BOTH CONFIRMATION

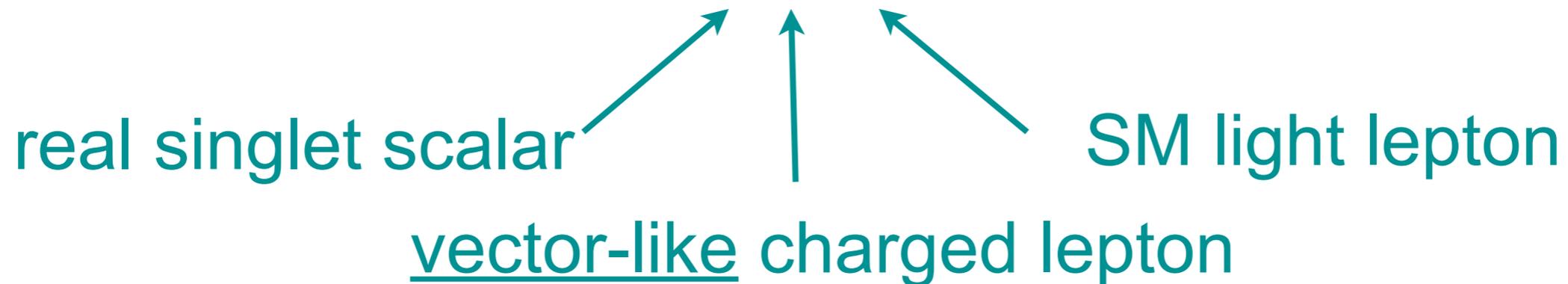
(obviously)

AND REJECTION OF PREDICTIONS ARE INSTRUCTIVE

(may point to a need for more degrees of freedom, etc)

# AN INSTANCE OF SIMPLIFIED WIMP

$$\mathcal{L} \supset y_l S \bar{\Psi} l_R + h.c.$$



$Z_2$  symmetry

$$S \longrightarrow -S$$

$S = \text{Dark Matter}$

$$\Psi \longrightarrow -\Psi$$

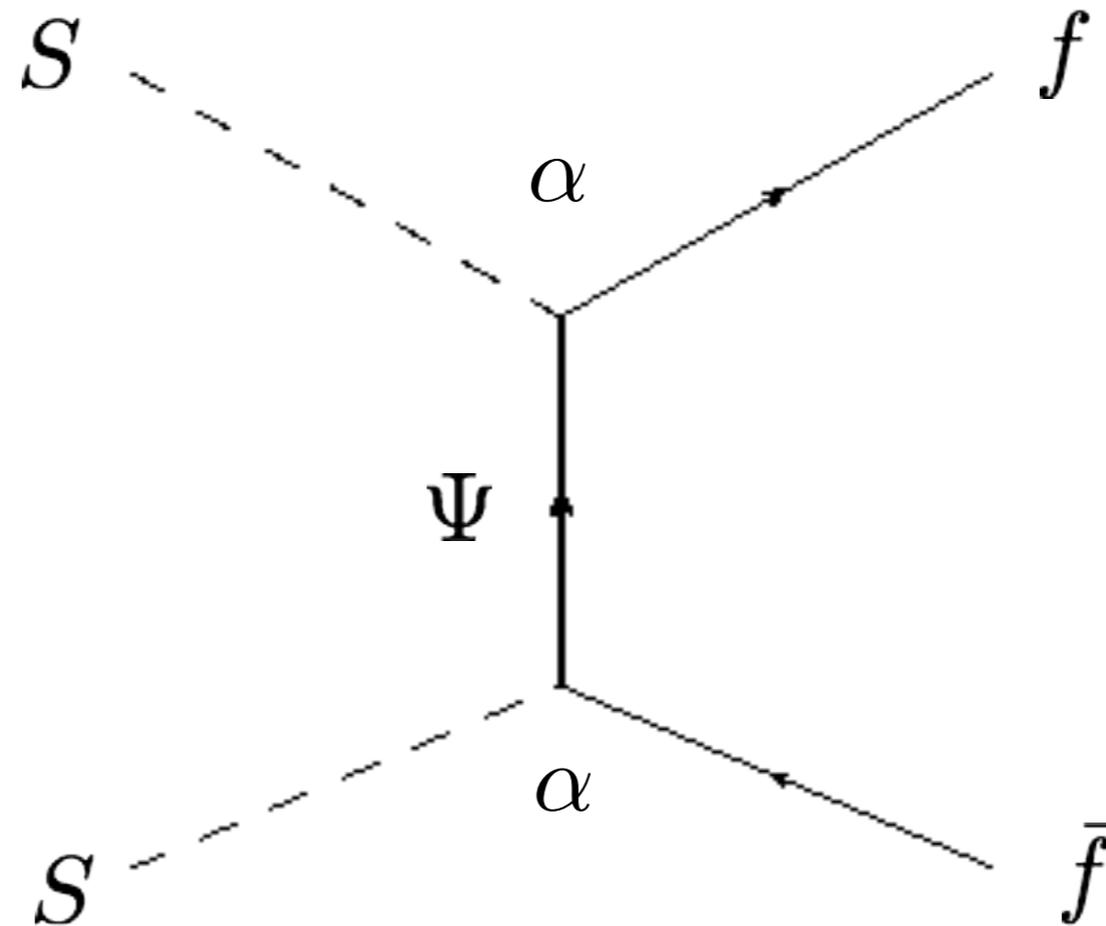
$\Psi = \text{Mediator}$

**➔ WE CALL IT THE VECTOR-LIKE PORTAL**

following P. Fileviez Perez, M.B. Wise  
arXiv:1303.1452

but aka “Effective WIMP” or “Fermionic Portal”

# THE VECTOR-LIKE PORTAL



assume 1 coupling (MFV?)

fixing the abundance leaves a 2-dim parameter space  
(masses of DM and mediator)

# ANNIHILATION CROSS SECTION

$$\sigma v(SS \rightarrow l\bar{l}) = \frac{y_l^4}{60\pi} \frac{v^4}{M_S^2} \frac{1}{(1+r^2)^4}$$



$$r = \frac{M_\Psi}{M_S} > 1$$

The annihilation cross section is **d-wave** in chiral limit  
(I don't know of another instance. Do you?)

Takashi Toma

arXiv:1307.6181

Giacchino, Lopez Honorez & M.T.

arXiv:1307.6480

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$$\sigma v(\chi\chi \rightarrow l\bar{l}) = \frac{\tilde{y}_l^4}{48\pi} \frac{v^2}{M_\chi^2} \frac{1+r_\chi^4}{(1+r_\chi^2)^4} \quad r_\chi = \frac{M_{\tilde{\Psi}}}{M_\chi} > 1$$

As is well-known, Majorana annihilation  
is **p-wave**

Goldberg

«Constraint on the Photino mass from  
cosmology»

Phys.Rev.Lett. 50 (1983) 1419

EARLY UNIVERSE

$$\langle v^2 \rangle \approx 0.3$$

GALACTIC CENTRE

$$v \sim 10^{-3}$$

2-BODY DM ANNIHILATION SUPPRESSED AT GC

NO INDIRECT DETECTION?

YES, LOOK FOR RADIATIVE CORRECTIONS!

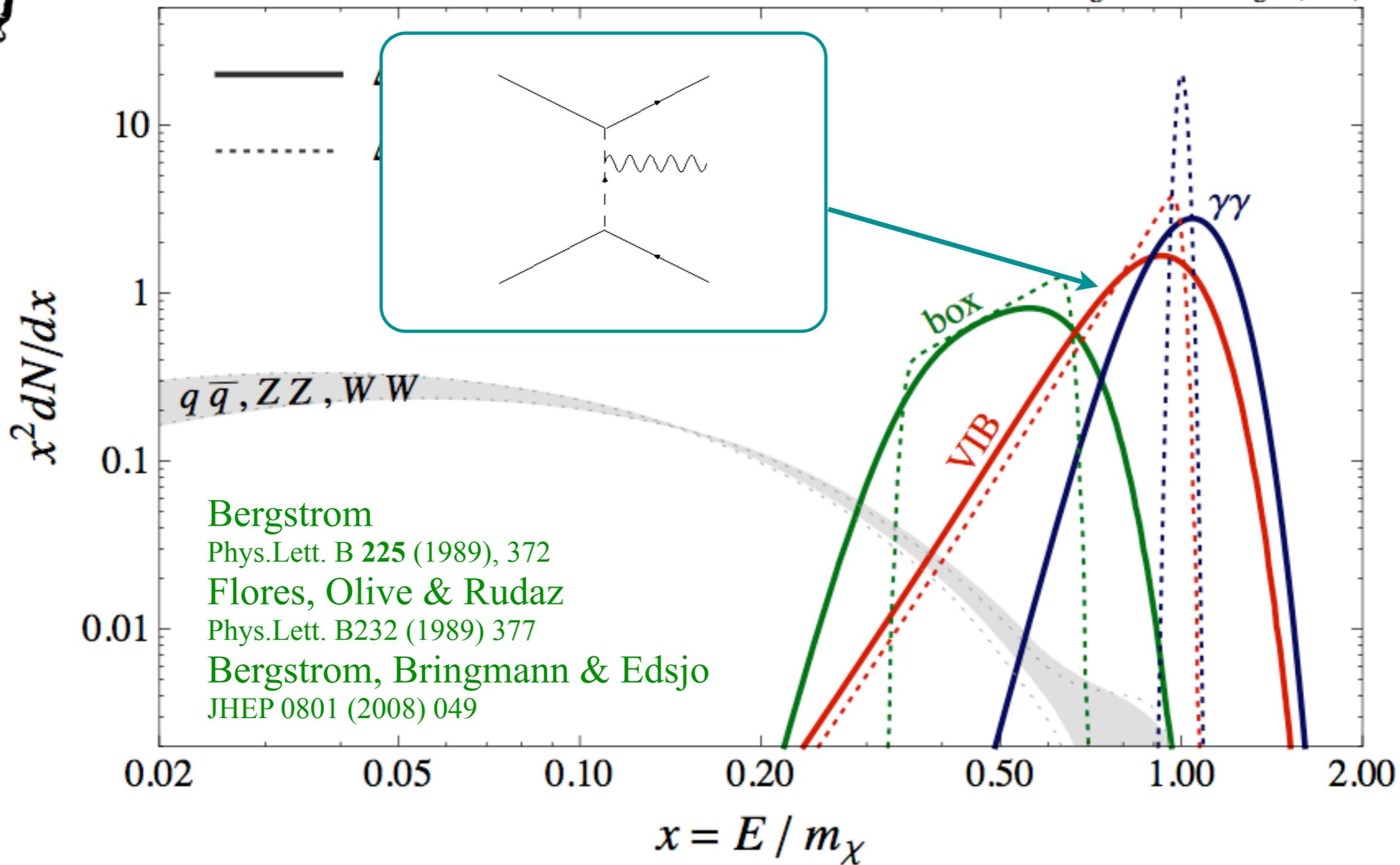
power of  $\alpha$  and phase-space suppressed, but s-wave



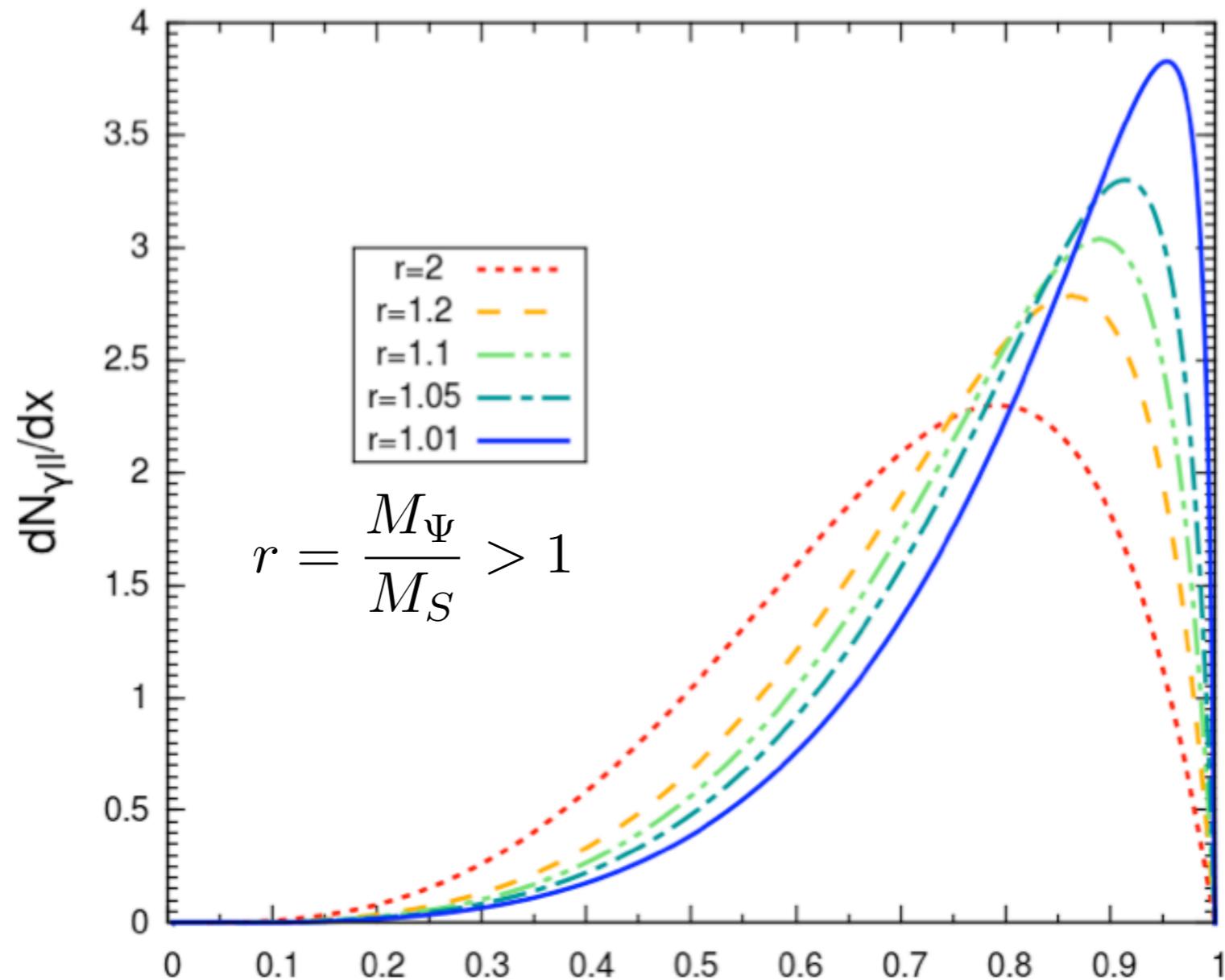
# GAMMA RAY FEATURES

## INTERNAL BREMSSTRAHLUNG

Bringmann & Weniger (2012)



# INTERNAL BREMSSTRAHLUNG SPECTRUM (same for scalar and Majorana)



**PEAKED  
AT**  
 $E \sim M_{DM}$

Barger, Keung & Marfatia

arXiv:1111.4523

Takashi Toma

arXiv:1307.6181

Giacchino, Lopez Honorez & M.T.

arXiv:1307.6480

$$x = \frac{E_{\gamma}}{M_{DM}}$$

# SAME BUT **CROSS SECTION** DIFFER BY A FACTOR OF 8


$$\frac{\sigma(SS \rightarrow f\bar{f}\gamma)}{\sigma(\chi\chi \rightarrow f\bar{f}\gamma)} = \frac{8y_l^4}{g_l^4}$$

VIB ENHANCED

while


$$\frac{\langle\sigma v\rangle(SS \rightarrow f\bar{f})}{\langle\sigma v\rangle(\chi\chi \rightarrow f\bar{f})} < 0.16 \frac{y_l^4}{g_l^4}$$

2-BODY SUPPRESSED



huge **enhancement** of VIB for scalar DM  
w.r.t. Majorana DM

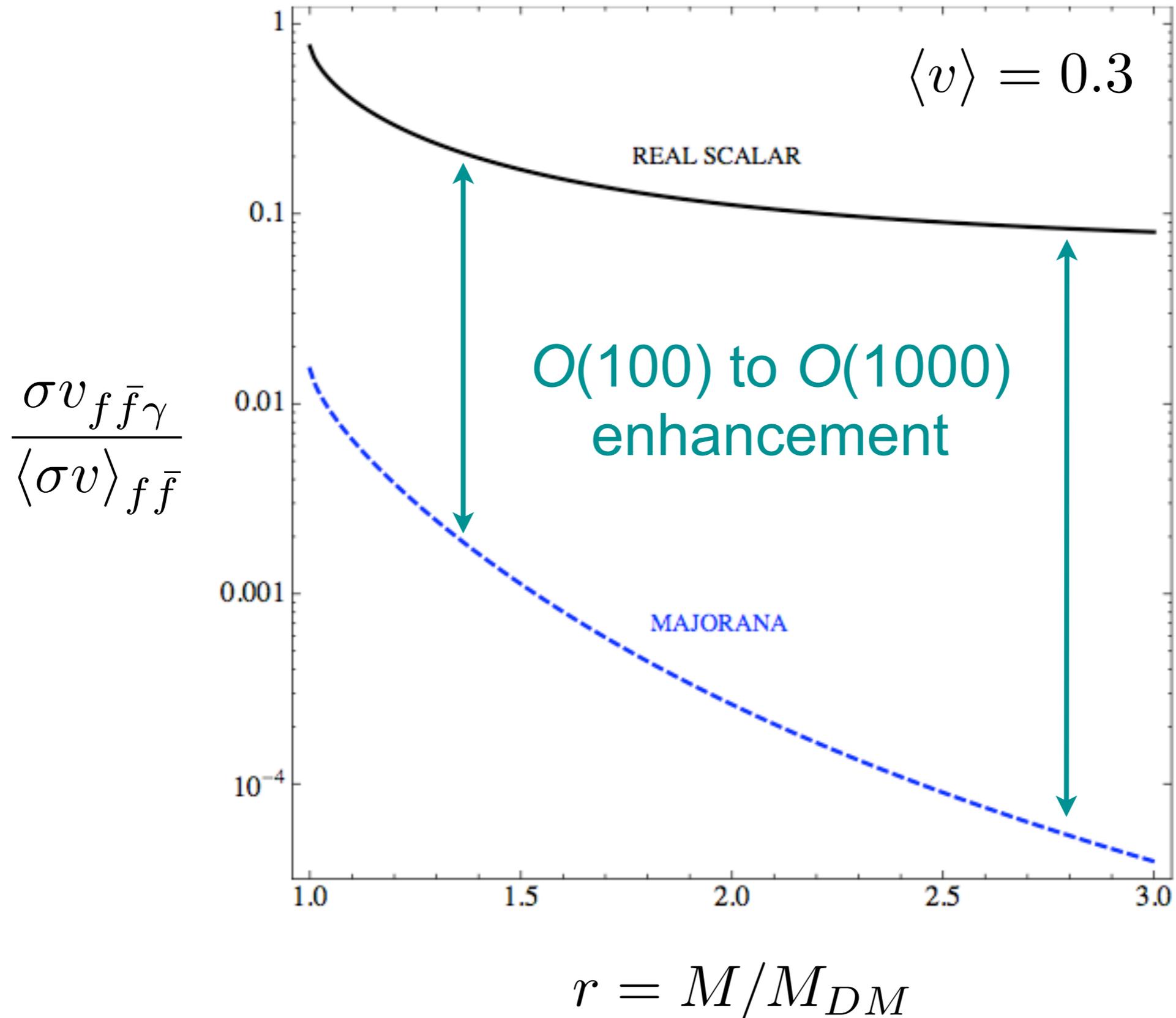
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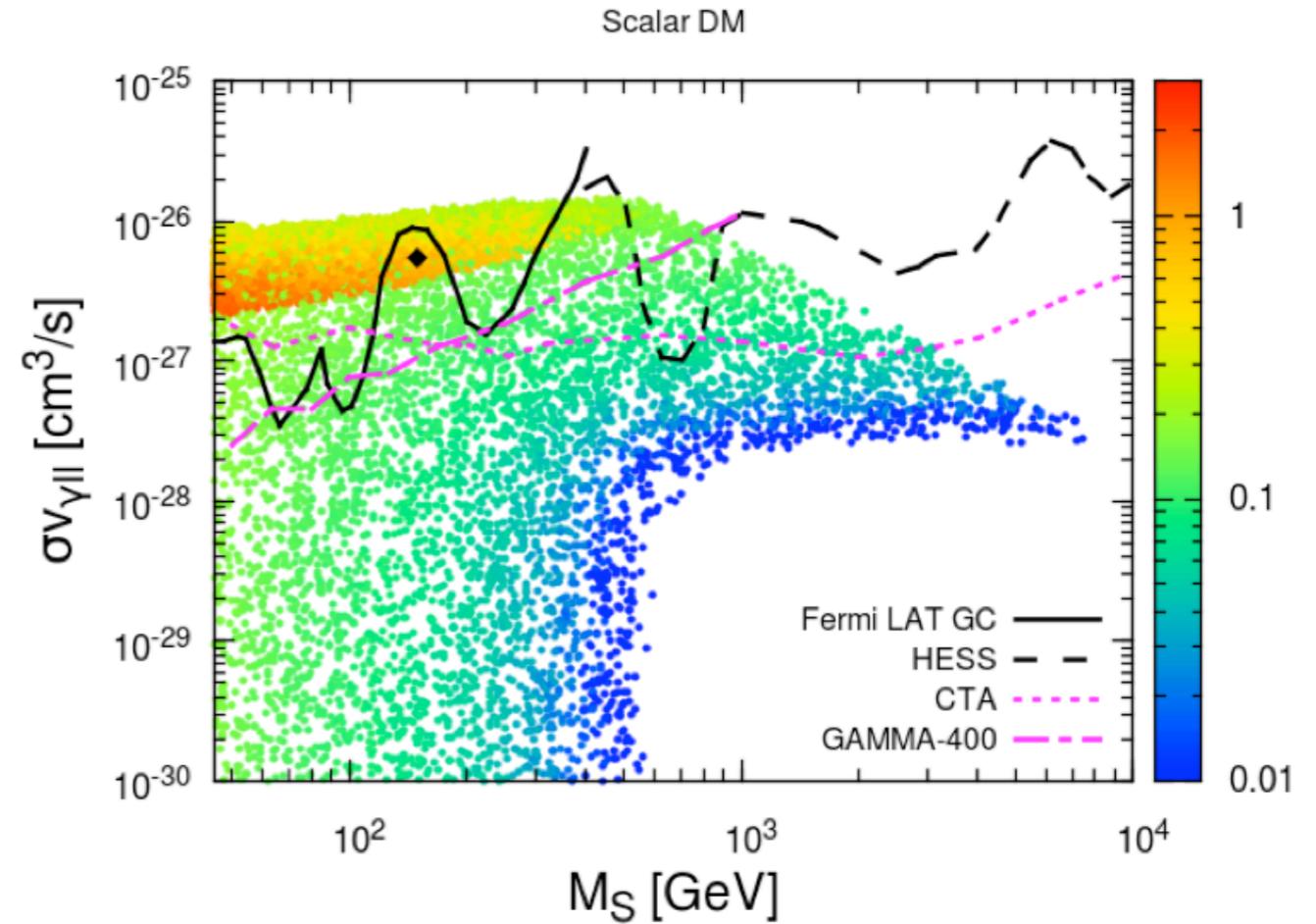
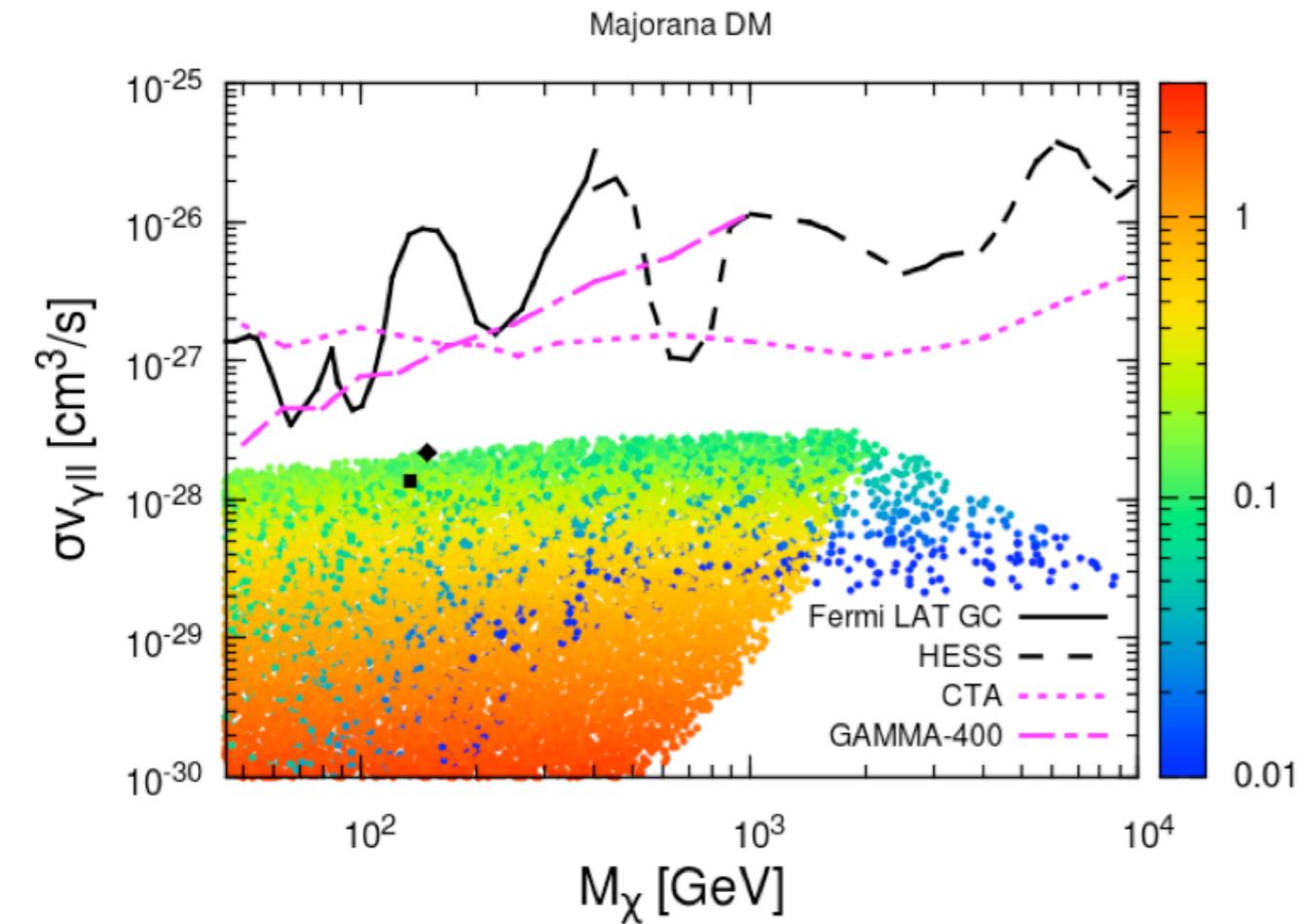
arXiv:1307.6480

# VIB ENHANCEMENT



# MAJORANA

# SCALAR



Giacchino, Lopez Honorez & M.T.

arXiv:1307.6480

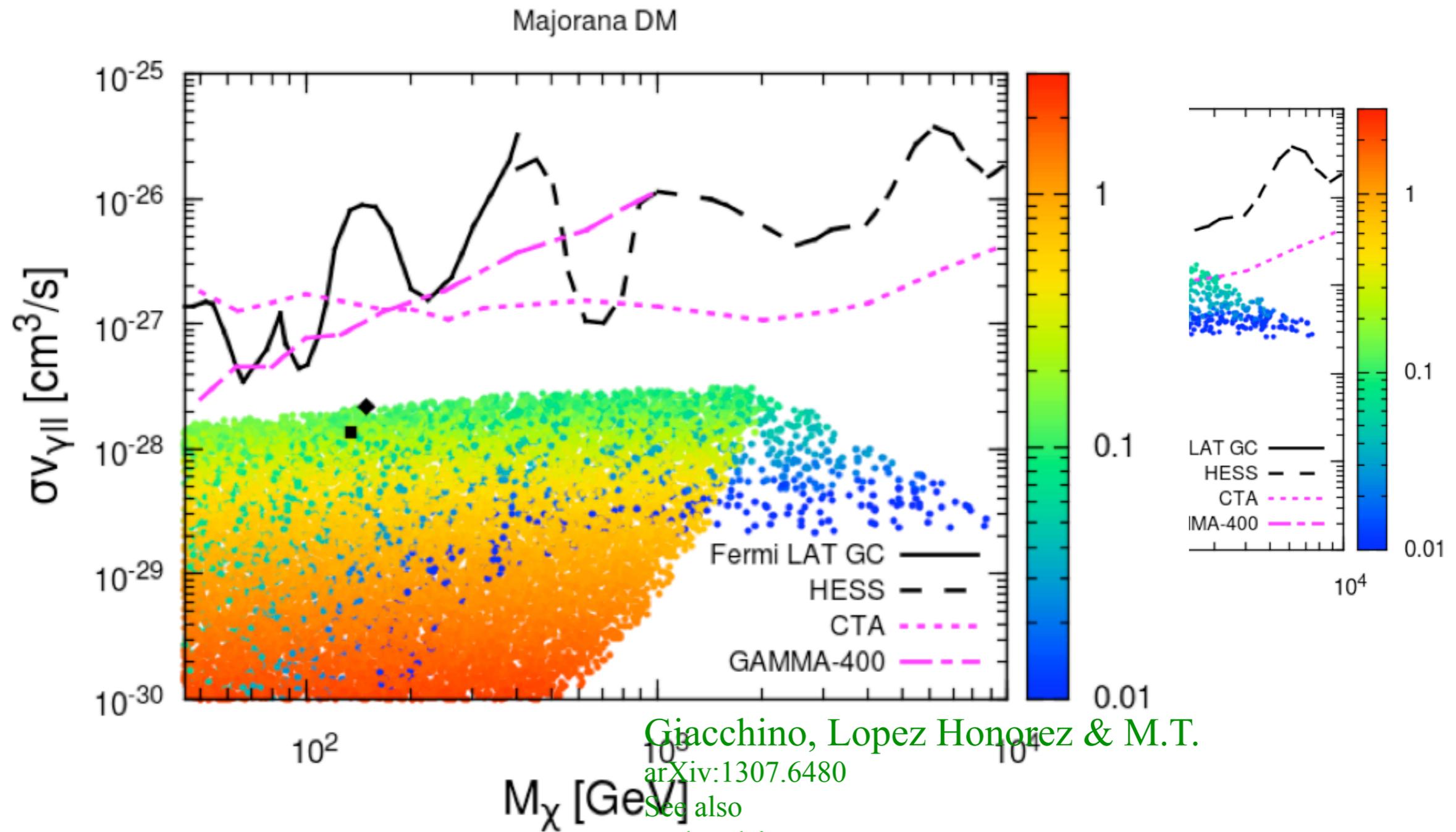
See also

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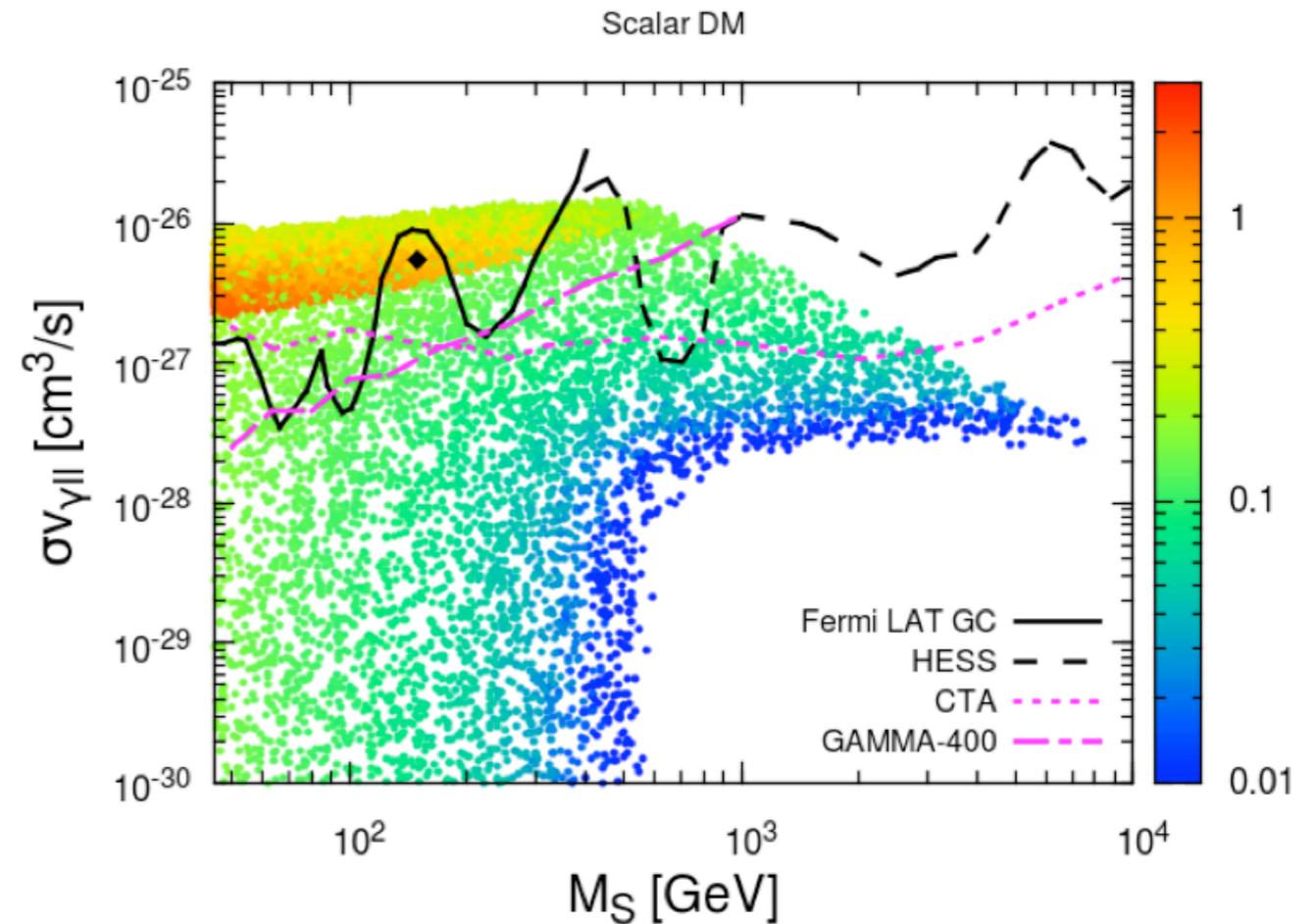
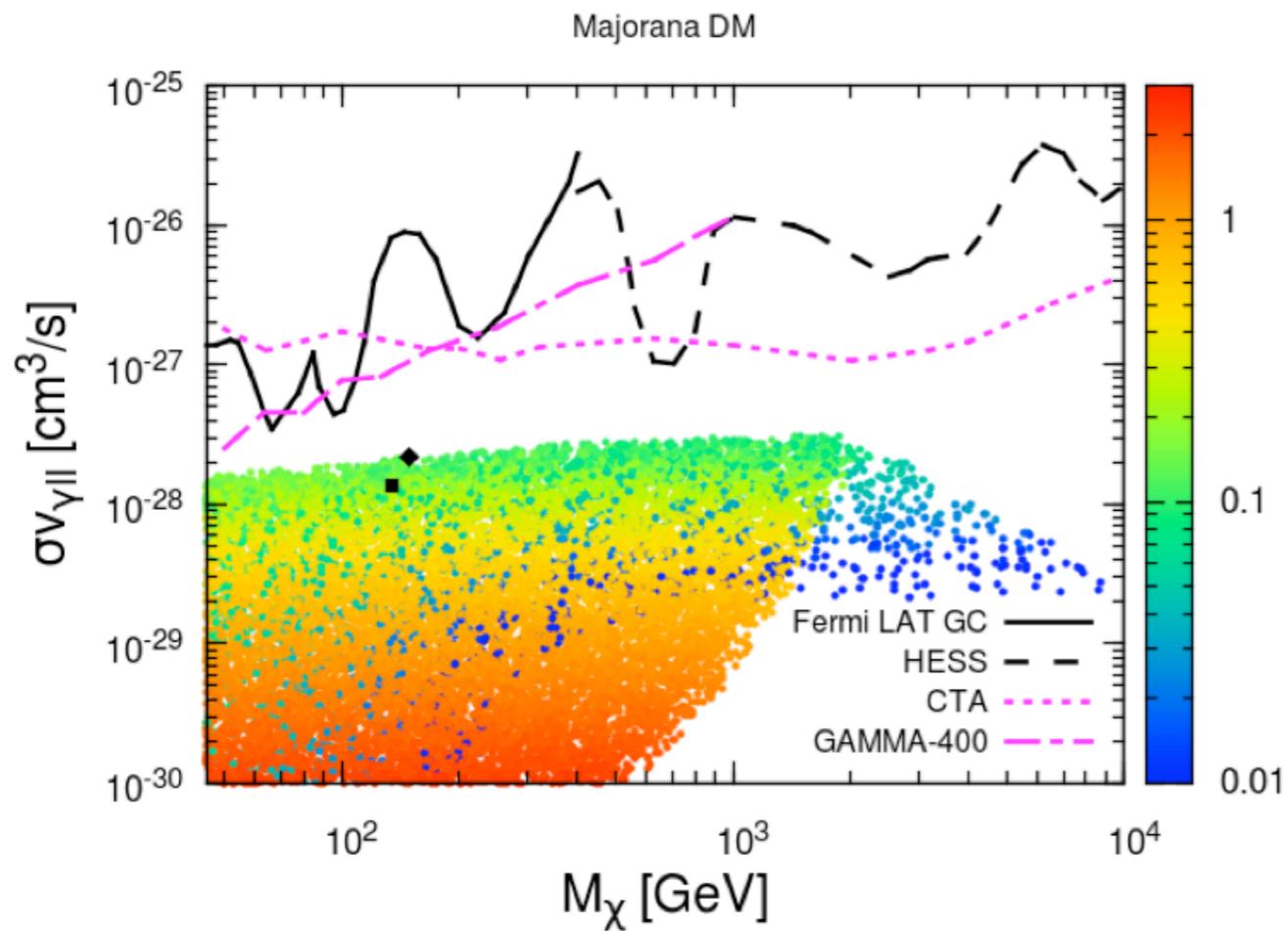
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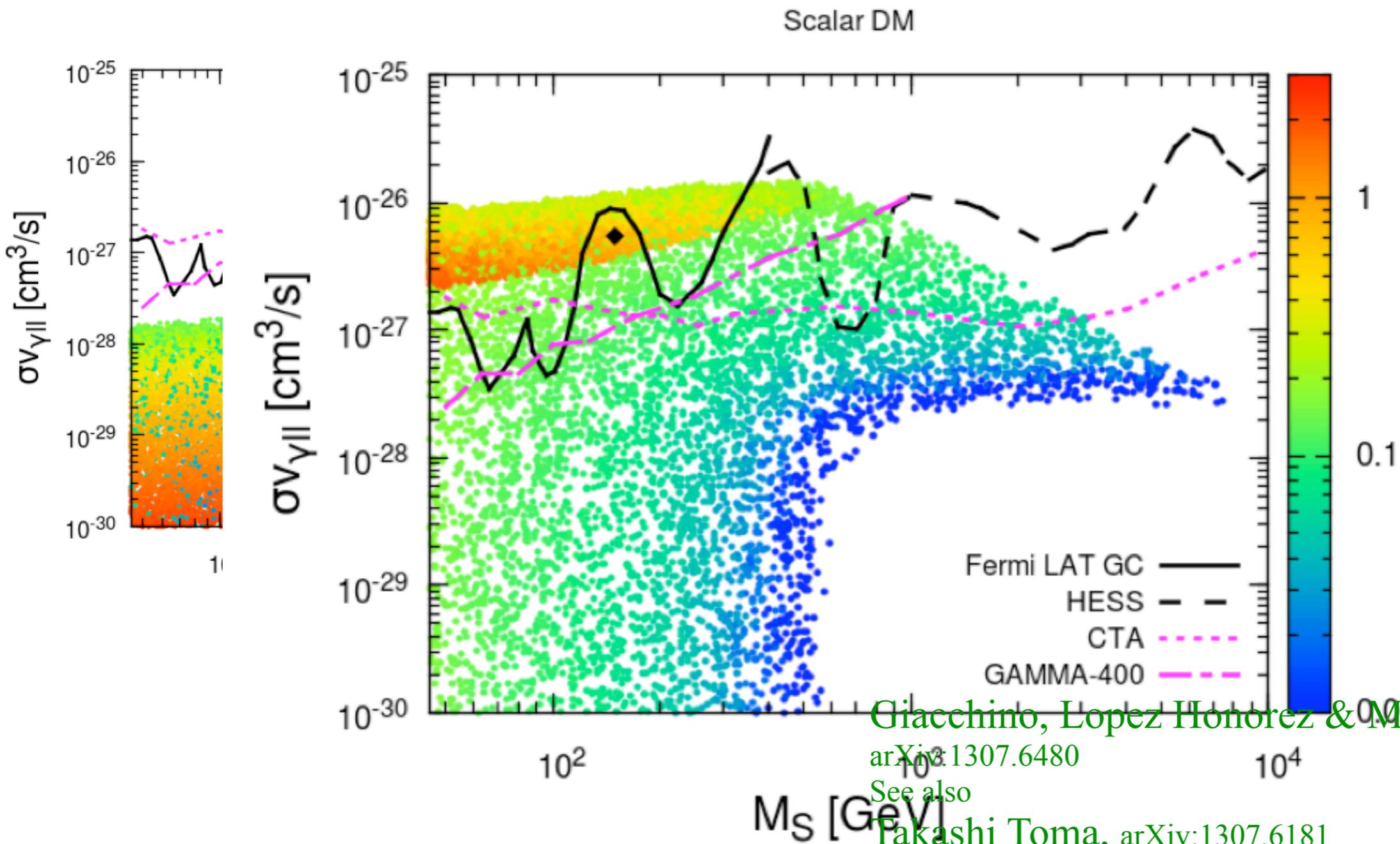
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# FINAL WORDS

**WE STILL DON'T KNOW WHAT DM IS MADE OF  
BUT  
WE KNOW MORE AND MORE WHAT IT IS NOT**

THE WIMP PARADIGM IS VERY APPEALING  
PROVIDED WE FIND DM  
(LEPTOGENESIS IS ALSO APPEALING)

IN THAT RESPECT  
SIMPLIFIED MODELS ARE USEFUL BECAUSE THEY ARE SENSICAL & INSTRUCTIVE

## KEY MESSAGE

**NATURE OF THE PORTAL/MEDIATOR IS IMPORTANT**  
(WE MAY VERY WELL FIND THE MEDIATOR BEFORE DM)

IMPORTANT TO **CONSIDER ALTERNATIVES**

## KEY MESSAGE

**PBH** ARE STILL ALIVE (BUT HAVE PROBLEMS OF THEIR OWN)  
CAN WE COMPLETELY KILL THIS POSSIBILITY?

**BACKUP SLIDES**

# WHAT'S NEXT? A POSSIBLE EXTENSION

$$\mathcal{L} \supset y_l S \bar{\Psi} l_R + h.c.$$

A SINGLET SCALAR WITH VL LEPTONS

$$\mathcal{L} \supset y_q S \bar{\Psi} q_R + h.c.$$

THE SAME WITH VL QUARKS

$$\frac{\langle \sigma v \rangle_{g\bar{q}q}}{\langle \sigma v \rangle_{\gamma\bar{q}q}} = \frac{N_c^2 - 1}{2N_c} \frac{\alpha_s}{Q^2\alpha}$$

~ 40 (up-like quarks)

~ 150 (down-like quarks)

$$\langle \sigma v \rangle_{q\bar{q}} \ll \langle \sigma v \rangle_{q\bar{q}g}$$



ABUNDANCE FROM  
(GLUON) BREMSSTRAHLUNG

EVEN IN EARLY UNIVERSE

+ DIRECT DETECTION  
+ CONSTRAINTS FROM CR ANTI-PROTONS  
+ **LHC constraints**  
etc...

Work in progress

# SO, WHAT WENT WRONG?

$$\vec{s}(\vec{x}, t) = \sum_{l=2}^{\infty} \vec{s}_l(\vec{x}) \int dt' \int_{\text{star}} dV \vec{f}_{bh} \cdot \vec{s}_l(\vec{x}') G_l^+(t - t')$$

↑  
fluid displacement

↑  
long range force

Formal manipulations lead to dropping seemingly innocuous terms but which are singular for long range forces

Quite hidden, but clearly seen in planar, incompressible fluid limit

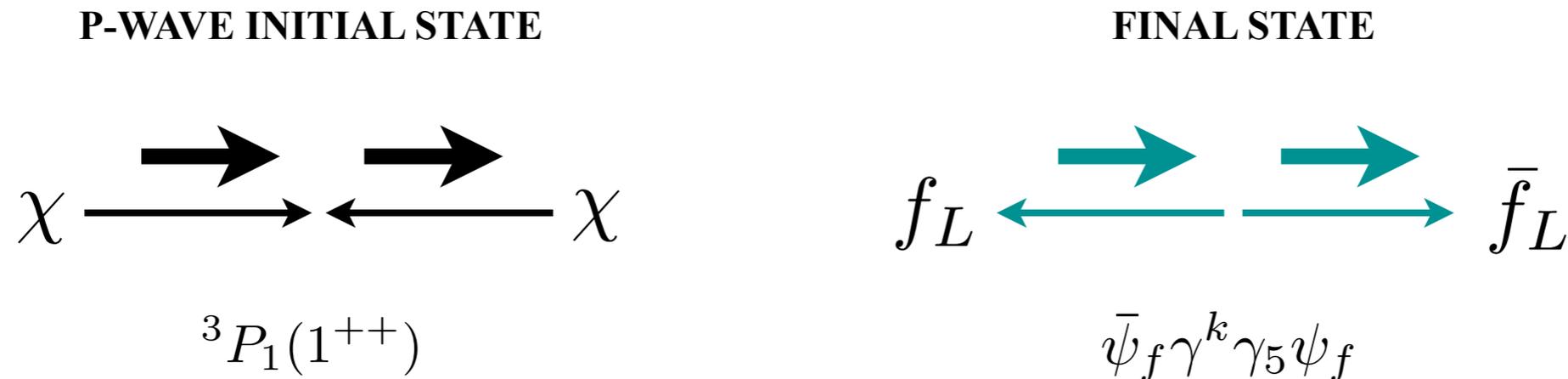
$$\vec{s}(\vec{x}, t) = GM_{bh} \text{Re} \int dk \frac{k}{\omega_k^2} \left( 1 - \frac{k v_{bh}}{k v_{bh} - i \omega_k} \right) e^{kz + k v_{bh} t} \left( J_0(kr) \vec{1}_z - J_1(kr) \vec{1}_r \right)$$

a forgotten boundary term  
(UV divergent)

Pani & Loeb kept only this  
(UV divergent too)

# A DIGRESSION

## ANNIHILATION OF MAJORANA DM INTO LIGHT SM FERMIONS



P-WAVE IN CHIRAL LIMIT (remember that  $v \sim 10^{-3}$  )

$$\sigma v \propto y_f^4 \frac{v^2}{M_\chi^2}$$

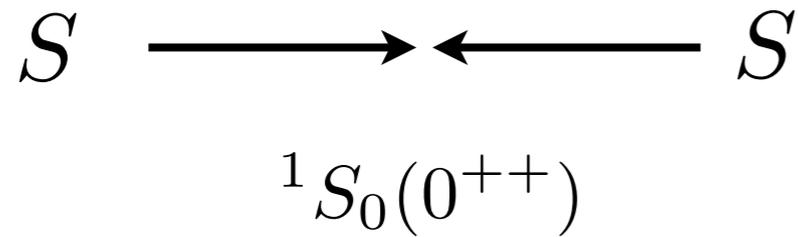
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«Constraint on the Photino mass from cosmology»

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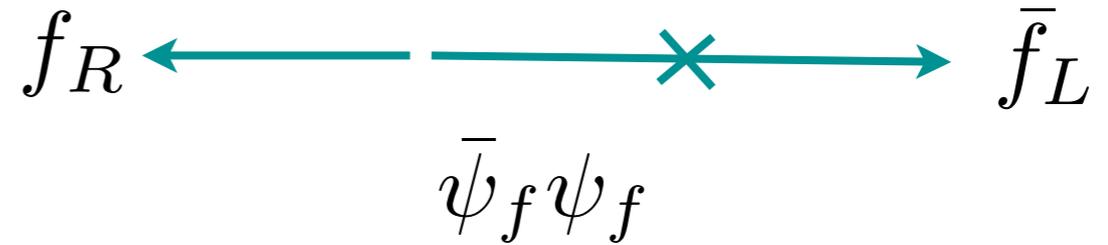
# WHY?

## S-WAVE INITIAL STATE



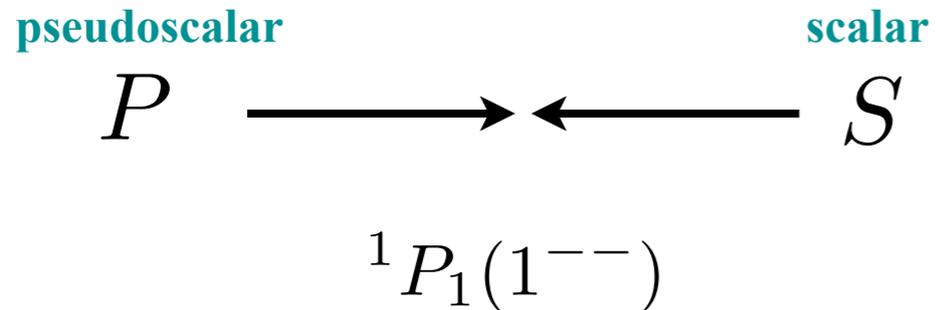
chirally suppressed

## FINAL STATE



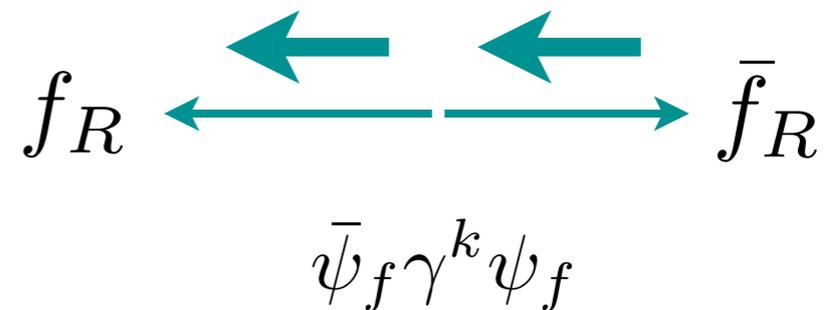
$$\mathcal{O}_S = m_f S^2 \bar{\psi}_f \psi_f$$

## P-WAVE INITIAL STATE



a complex scalar could have p-wave annihilation

## FINAL STATE



$$\mathcal{O} = P \overleftrightarrow{\partial}_\mu S \bar{\psi}_f \gamma^\mu \psi_f$$

# WHY?

**S-WAVE INITIAL STATE**

$$S \begin{array}{c} \longrightarrow \\ \longleftarrow \end{array} S$$

$${}^1S_0(0^{++})$$

chirally suppressed

**FINAL STATE**

$$f_R \begin{array}{c} \longleftarrow \\ \longrightarrow \end{array} \bar{f}_L$$

$$\bar{\psi}_f \psi_f$$



$$\mathcal{O}_S = m_f S^2 \bar{\psi}_f \psi_f$$

**D-WAVE INITIAL STATE**

$$S \begin{array}{c} \longrightarrow \\ \longleftarrow \end{array} S$$

$${}^1D_2(2^{++})$$

**d-wave  
in chiral limit**

**FINAL STATE**

$$f_R \begin{array}{c} \longleftarrow \\ \longrightarrow \end{array} \bar{f}_R$$

$$\Theta^{ij} = \frac{i}{2} \bar{\psi}_f (\gamma^i \overleftrightarrow{\partial}^j - \gamma^j \overleftrightarrow{\partial}^i) \psi_f$$



$$\mathcal{O}_T = \partial_\mu S \partial_\nu S \Theta_{f_R}^{\mu\nu}$$

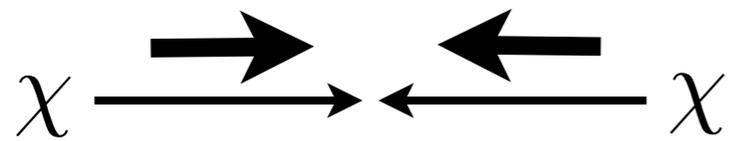
**FERMION  
STRESS-ENERGY TENSOR**



# A DIGRESSION

## ANNIHILATION OF MAJORANA DM INTO LIGHT SM FERMIONS

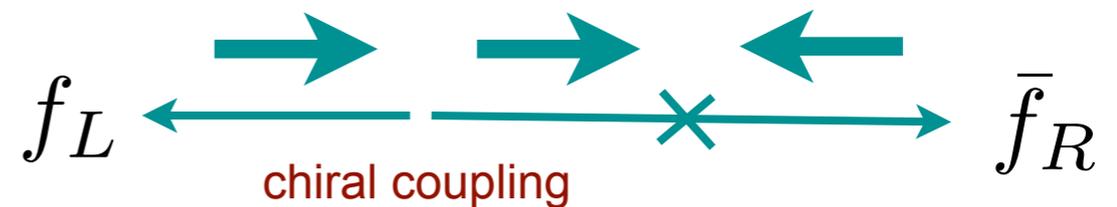
**S-WAVE INITIAL STATE**



$${}^{2S+1}L_J(J^{PC}) = {}^1S_0(0^{-+})$$

$$|S=0\rangle = \frac{1}{2}(|\downarrow\rangle|\uparrow\rangle - |\uparrow\rangle|\downarrow\rangle)$$

**FINAL STATE**



$$\bar{\psi}_f \gamma_5 \psi_f$$

**S-WAVE ANNIHILATION  
IS MASS SUPPRESSED**



$$\mathcal{O}_{\text{s-wave}} = m_f \bar{\chi} \gamma_5 \chi \bar{\psi}_f \gamma_5 \psi_f$$



$$\sigma v \propto y_f^4 \frac{m_f^2}{M_\chi^4}$$

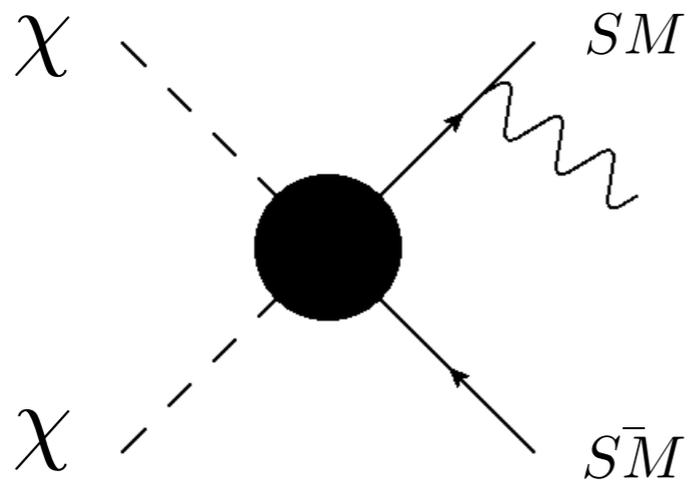
**Goldberg**

«Constraint on the Photino mass from cosmology»

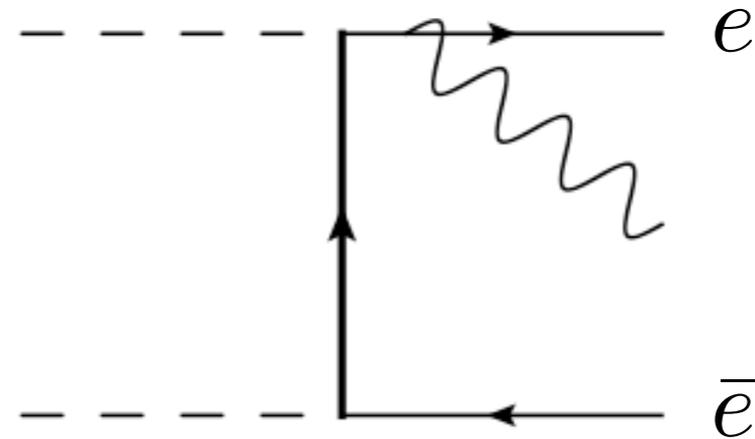
Phys.Rev.Lett. 50 (1983) 1419

# VIRTUAL INTERNAL BREMSSTRAHLUNG (VIB)

annihilation of DM into charged particles



e.g.



Final State Radiation (FSR)

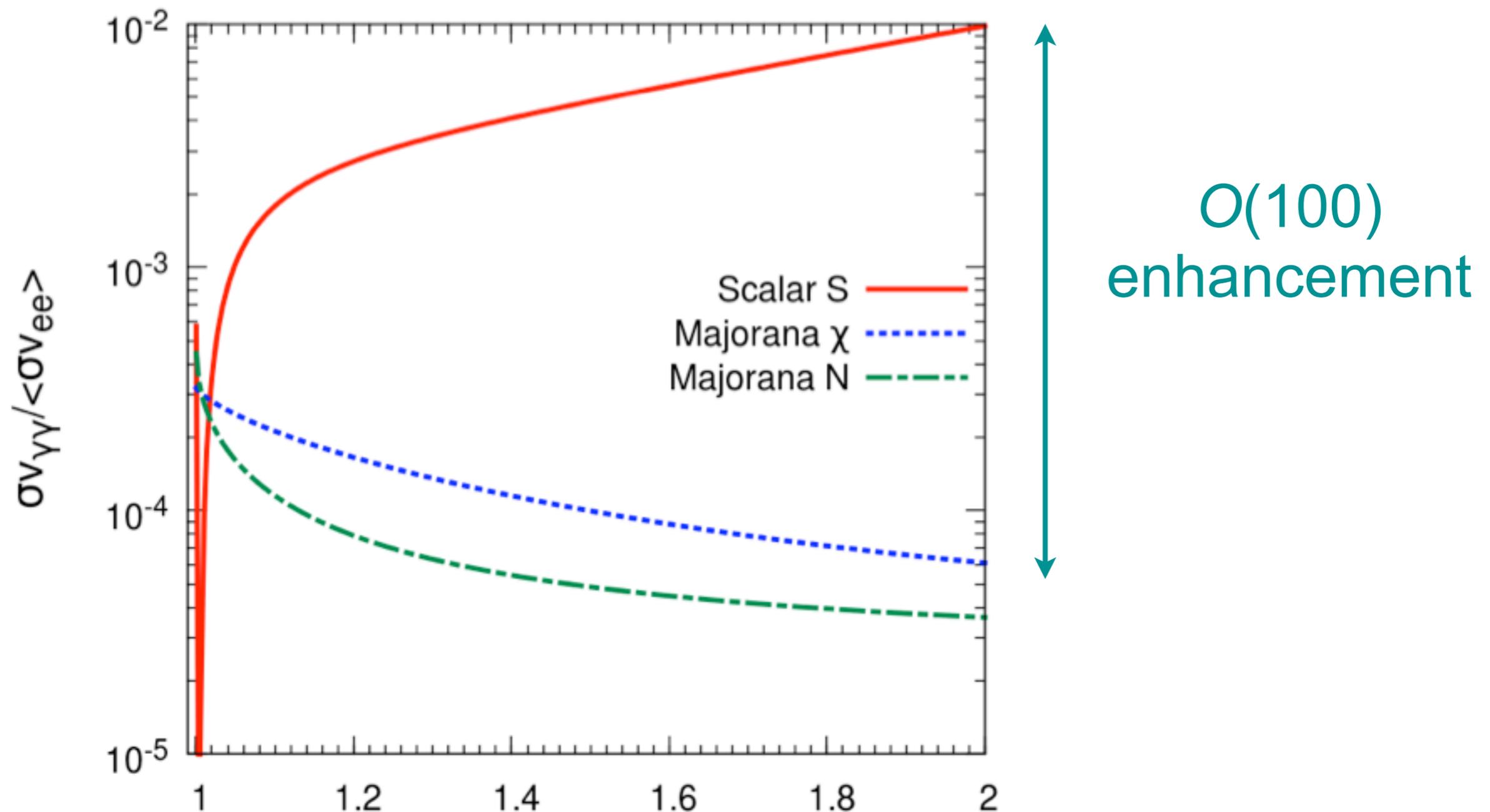
$$\frac{d\sigma(\chi\chi \rightarrow X\bar{X}\gamma)}{dx} \approx \frac{\alpha Q_X^2}{\pi} \mathcal{F}_X(x) \log\left(\frac{s(1-x)}{m_X^2}\right) \sigma(\chi\chi \rightarrow X\bar{X})$$



Collinear/soft emission.  
 Universal (but final state dependent) feature,  
 encoded in splitting function.

Birkedal, Matchev, Perelstein  
 and Sprey (2005)

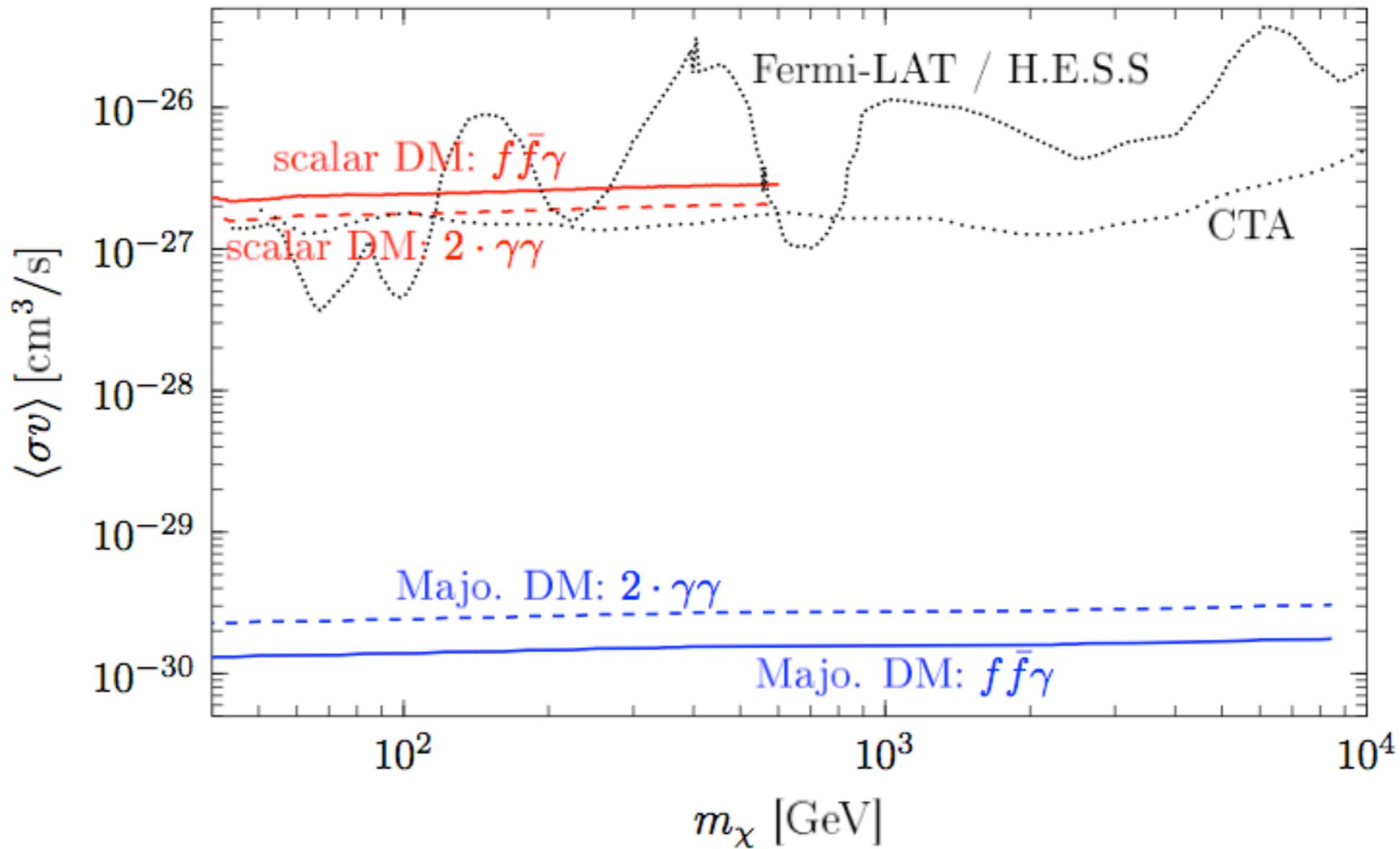
# MONOCHROMATIC GAMMA RAYS



$$r = \frac{M_\Psi}{M_S} > 1$$

Ibarra, Toma, Totzauer & Wild  
arXiv:1405.6917  
Giacchino, Lopez Honorez, M.T.  
arXiv:1405.6921

$$m_\psi/m_\chi = 3, \lambda = 0, y = y_{\text{thermal}}$$



Ibarra, Toma, Totzauer & Wild  
arXiv:1405.6917