

# New Insights on Spectroscopy and Properties of light hadrons with COMPASS

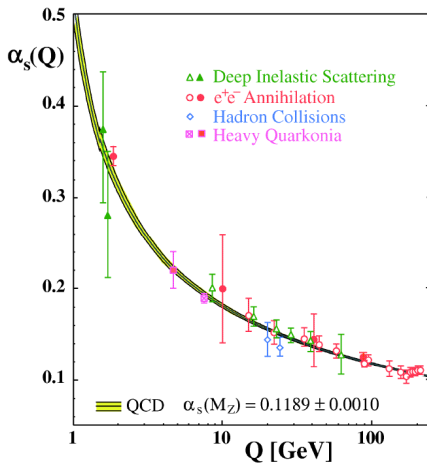
Florian Haas

Physik Department E18 - Technische Universität München  
for the COMPASS Collaboration

Annual Meeting of the GDR PH-QCD "Annihilation and Scattering"  
Group  
Recent Highlights in Hadron Structure

supported by:  
Maier-Leibnitz-Labor der TU und LMU München,  
Cluster of Excellence: Origin and Structure of the Universe, BMBF



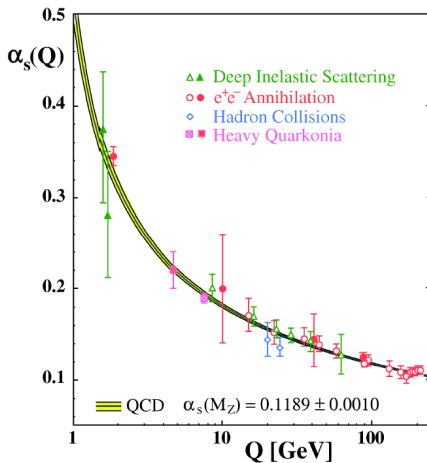


- Confinement
- Hadrons relevant DOF

- Asymptotic Freedom
- Quarks & Gluons relevant DOF
- Perturbative QCD
- Hadronization, Jets

S. Bethke

[arXiv:hep-ex/0606035v2]

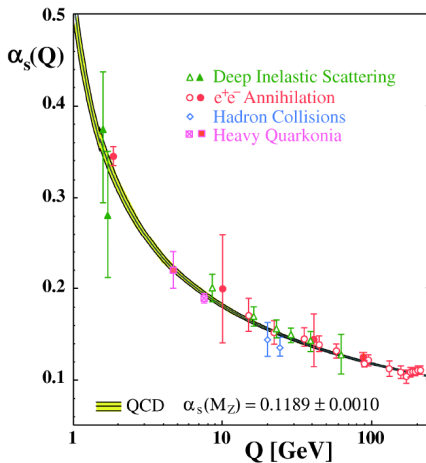


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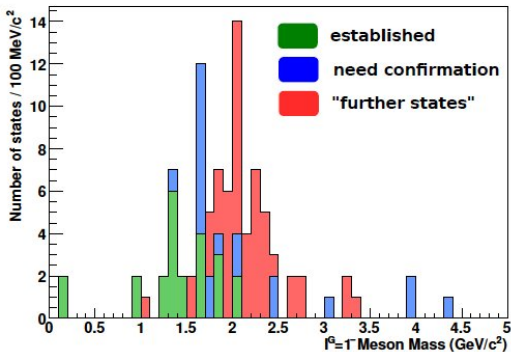
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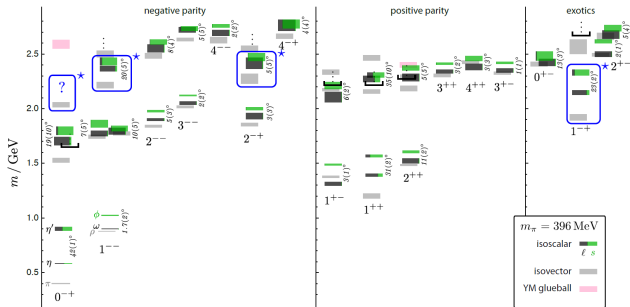


- Confinement
- Hadrons relevant DOF
- Dynamics of excited states?
- Models and theories
  - Quark model
  - Bag model
  - Flux tube model
  - $\chi_{PT}$  for slow pions
  - Lattice QCD





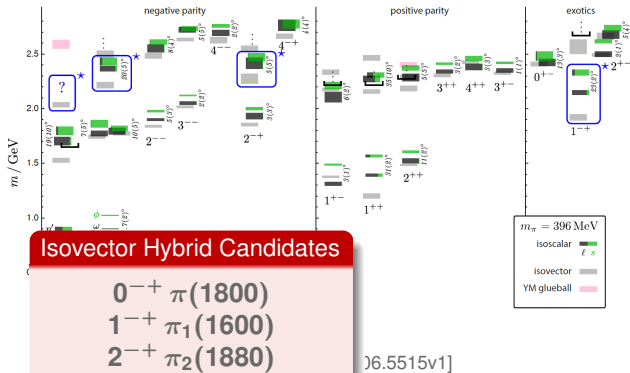
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Dudek et al. [arXiv:1106.5515v1]



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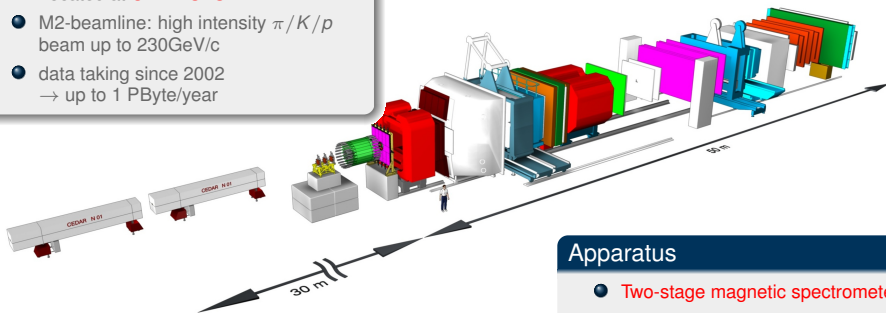


# The COMPASS Hadron Setup

## Spectrometer and Hadron Beam

### Overview

- **CO**mmun **M**uon and **P**roton **A**pparatus for **S**tructure and **S**pectroscopy <sup>1</sup>
- Located at **CERN SPS**
- M2-beamline: high intensity  $\pi/K/p$  beam up to 230GeV/c
- data taking since 2002  
→ up to 1 PByte/year



### Apparatus

- **Two-stage magnetic spectrometer**
- Large acceptance charged tracking
- Calorimetry (ECAL/HCAL)
- Kaon PID (CEDARs/RICH)

<sup>1</sup> [Nucl. Instr. and Meth. A 577 (2007) 455]





## Light-Meson Spectroscopy

$\pi^- \pi^- \pi^+$  and  $\pi^- \pi^0 \pi^0$

$\eta \pi^-$  and  $\eta' \pi^-$

Status of the  $J^{PC} = 1^{-+}$  Spin Exotic Partial Wave

$\pi\pi$  Production at Central Rapidities

## Tests of Chiral Dynamics

$3\pi$  Primakoff Production

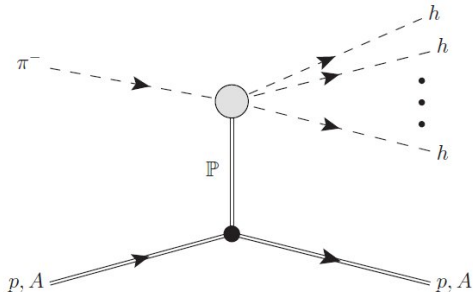
Pion Polarizability



# Light-Meson Spectroscopy

## Isovector Mesons

### Diffractive Pion Dissociation



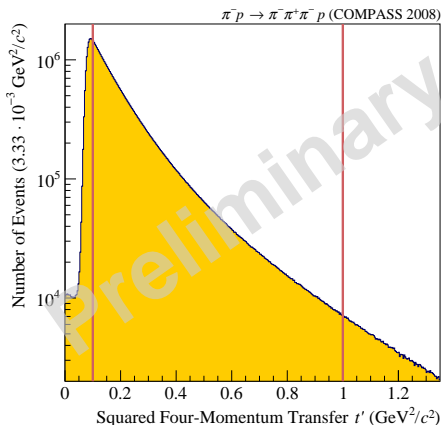
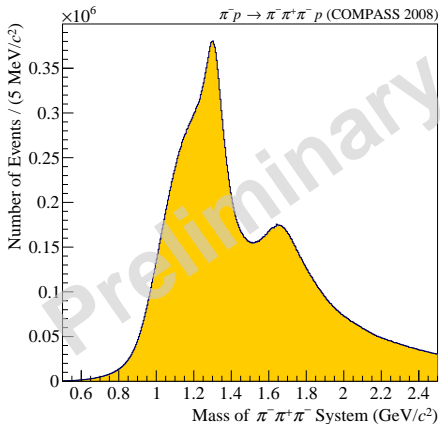


# Diffractive Dissociation into $\pi^- \pi^+ \pi^-$

relevant kinematic distributions

- 190 GeV/c hadron beam  $\rightarrow$   
96% $\pi^-$ , 3.5% $K^-$ , 0.5% $\bar{p}$
- 40cm liquid hydrogen target

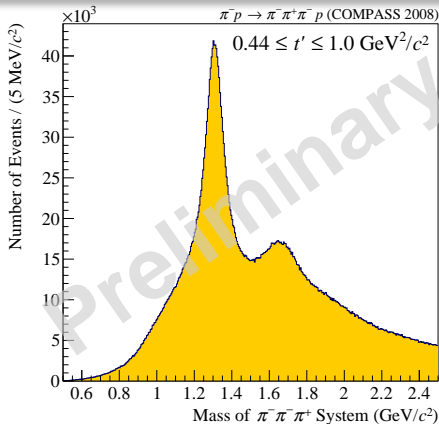
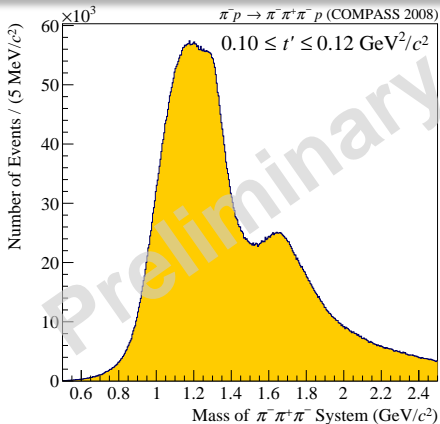
- $0.1 \text{ GeV}^2/c^2 < t' < 1.0 \text{ GeV}^2/c^2$
- $\sim 50 \text{ M}$  exclusive events (2008)





# Diffractive Dissociation into $\pi^- \pi^+ \pi^-$

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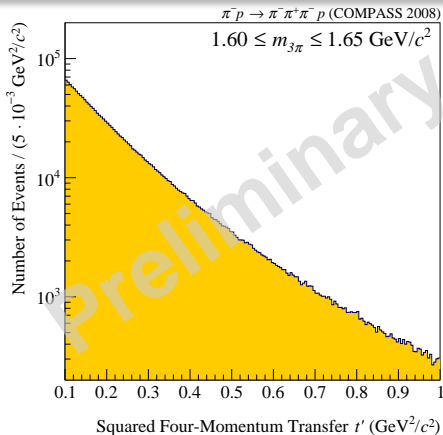
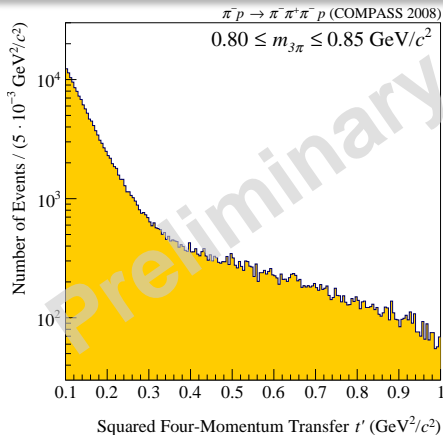


The invariant mass of the final state depends on squared four-momentum transfer  $t$



# Diffractive Dissociation into $\pi^- \pi^+ \pi^-$

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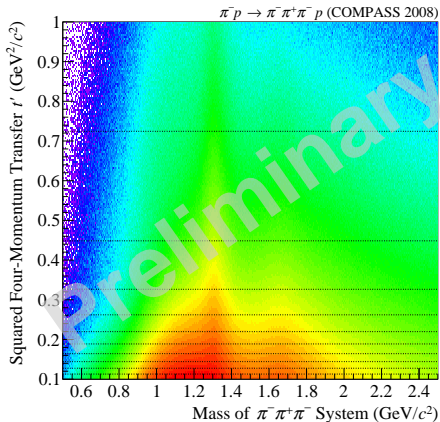


The squared four-momentum transfer  $t$  depends on the invariant mass of the final state



# Diffractive Dissociation into $\pi^- \pi^+ \pi^-$

relevant kinematic distributions



Ansatz: Split data into small bins of  $t$  and  $m_{3\pi}$



# Partial Wave Analysis - Formalism

## Step One: Decomposition in Spin-Parity States

### Spin-Parity Decomposition for each bin of $t$ and $m_{3\pi}$ (2D)

Assumption 1: Partial waves that contribute to the same final state are fully coherent.

$$\mathcal{I}(\tau) \sim \left| \sum_i \psi_i \right|^2$$

- $T_i$ : Transition amplitude  $\in \mathbb{C}$  (unknown, contains information on intensity and phases)
- $\psi_i$ : Decay amplitude  $\in \mathbb{C}$  (calculable, based on a set of kinematical distributions  $\tau$ )
- $i$ : partial waves  $J^{PC} M^{\pm} \xi \pi L$  e.g.  $3\pi$ : 87 waves up to spin 6 + one incoherent isotropic wave



# Partial Wave Analysis - Formalism

## Step One: Decomposition in Spin-Parity States

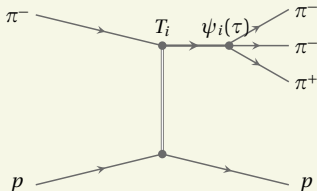
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### Production and Decay







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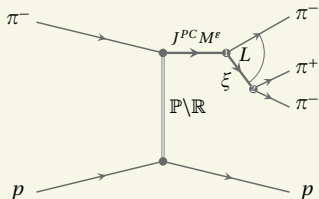
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### Isobar Model





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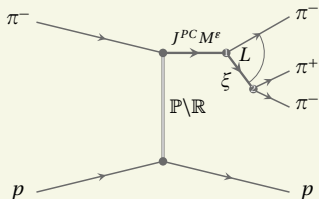
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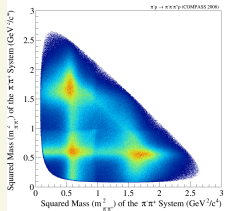
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### Dalitz Plot $\pi_2(1670)$ region





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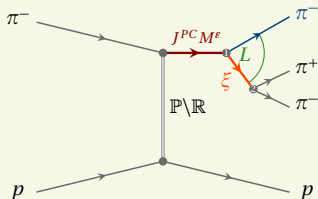
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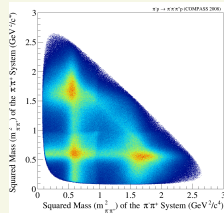
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### Extraction of Resonance Parameters for $t'$ and $m$

- Use full information of the spin density matrix elements  $T_i T_j^*(m_x, t')$ 
  - Intensities
  - Phases
- Parametrise the spin density matrix
  - Breit-Wigner forms
  - $t'$ -dependent non-resonant contributions
- $\chi^2$  fit of the spin-density submatrix



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## Partial-wave analysis of

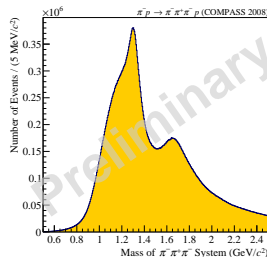
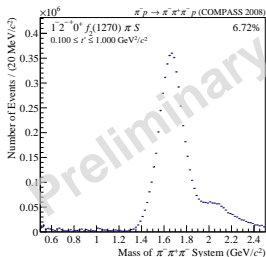
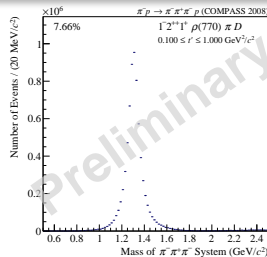
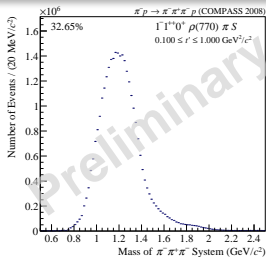
$$\pi^- + p \rightarrow \pi^- \pi^- \pi^+ + p$$

$$\pi^- + p \rightarrow \pi^- \pi^0 \pi^0 + p$$



# $\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$ (2008)

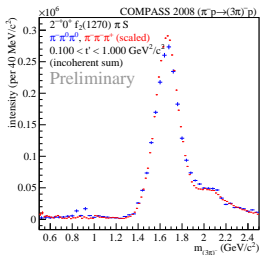
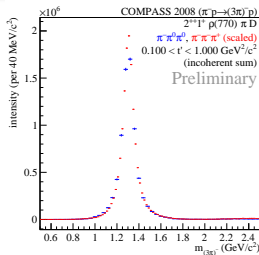
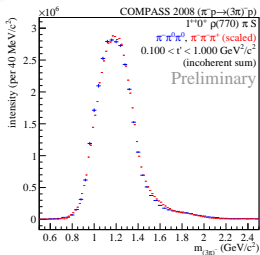
## Intensities of dominant $J^{PC}$ states





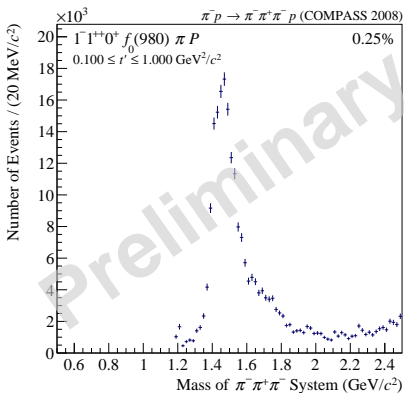
# $\pi^- p \rightarrow (3\pi)^- p$ (2008)

## Intensities of dominant $J^{PC}$ states



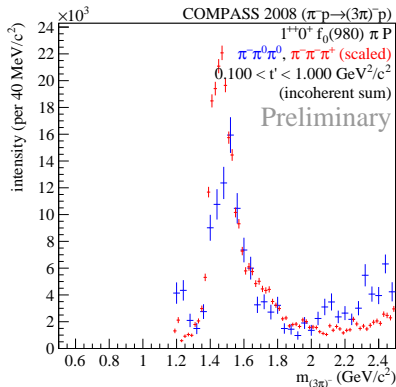
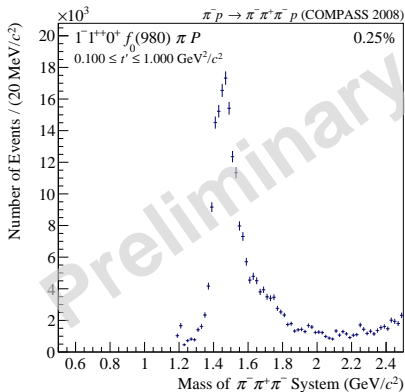


# A new Axialvector Resonance?

 $1^{++}0^+ f_0(980)\pi P$ 




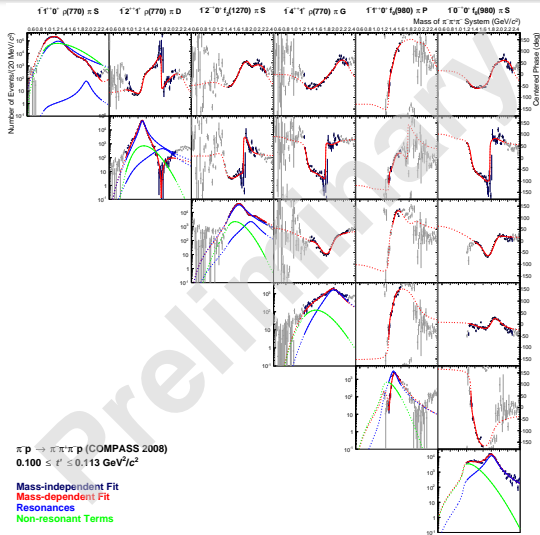
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# Extraction of Resonance Parameters

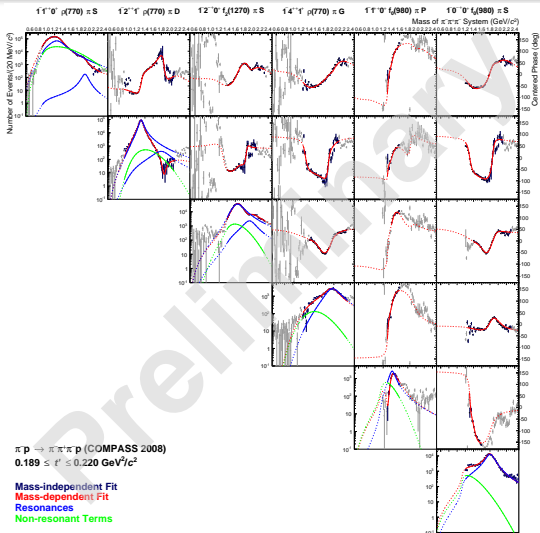
simultaneous fit of 6 partial waves in 11  $t'$  bins





# Extraction of Resonance Parameters

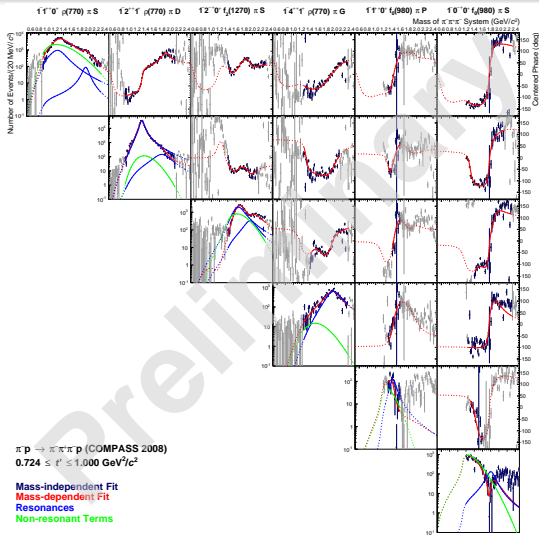
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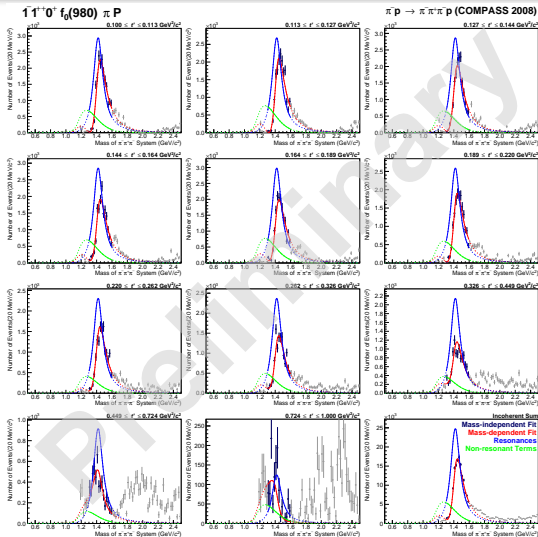






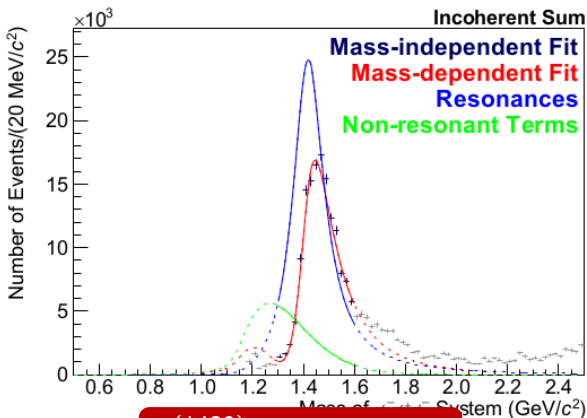
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# The $a_1(1420)$



$a_1(1420)$

$M = 1412 - 1422 \text{ MeV}/c^2$

$\Gamma = 130 - 150 \text{ MeV}/c^2$



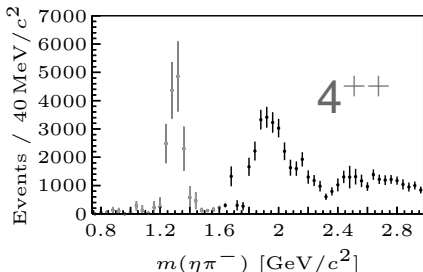
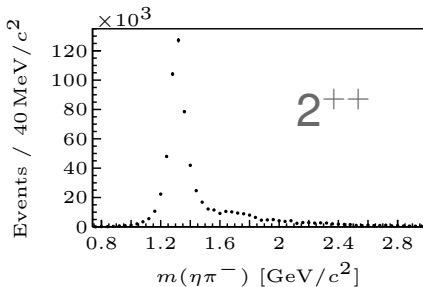
## Partial-wave analysis of

$$\pi^- + p \rightarrow \eta\pi + p$$

$$\pi^- + p \rightarrow \eta'\pi + p$$



$$\pi^- + p \rightarrow \eta\pi + p \quad (2008)$$

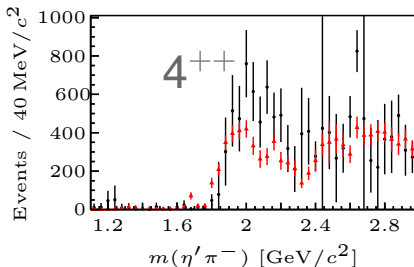
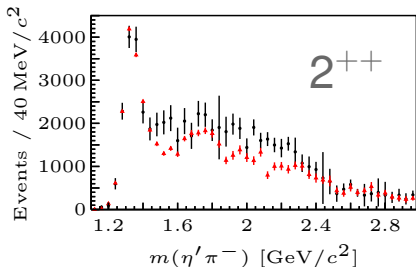
 $D_+ \text{- vs } G_+ \text{-wave}$ 


CERN Preprint CERN-PH-EP-2014-204    subm. to PLB



$$\pi^- + p \rightarrow \eta' \pi + p \quad (2008)$$

Comparison  $\pi^- + p \rightarrow \eta' \pi + p$  vs  $\pi^- + p \rightarrow \eta \pi + p$  (2008)

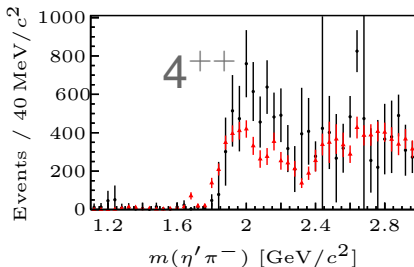
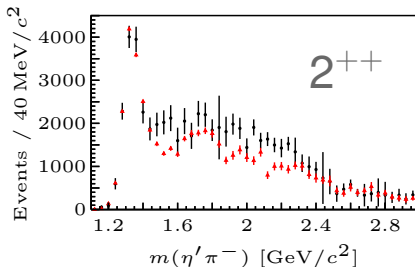


Scaling of  $\eta\pi$ : Adjustment for branching and phase space



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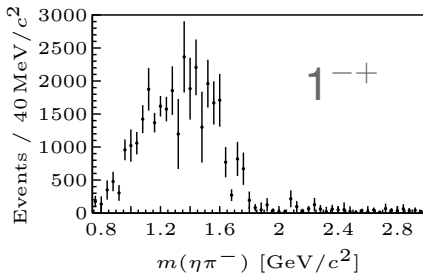


Scaling of  $\eta\pi$ : Adjustment for branching and phase space

Even- $L$  waves have very similar intensity distributions in  $\eta\pi$  and  $\eta'\pi$  (after correction for phase-space effects) over the whole mass range.



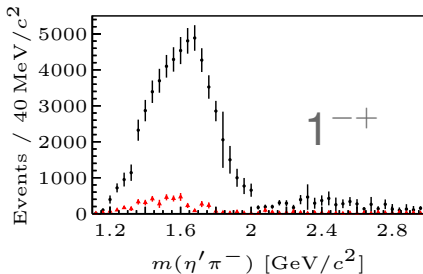
$$\pi^- + p \rightarrow \eta\pi + p \quad (2008)$$

 $P_{+}\text{-wave}$ 



$$\pi^- + p \rightarrow \eta' \pi + p \quad (2008)$$

Comparison  $\pi^- + p \rightarrow \eta' \pi + p$  vs  $\pi^- + p \rightarrow \eta \pi + p$  (2008)



Odd- $L$  waves, in particular the P wave, are suppressed in  $\eta\pi$  by a factor 5 to 10, again over the whole mass range.





# Status of the $J^{PC} = 1^{-+}$ Spin Exotic Partial Wave



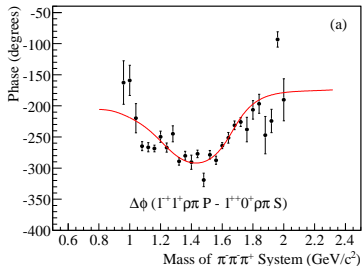
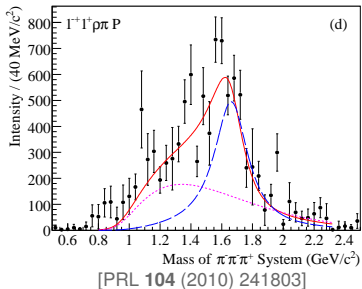
$$\pi^- Pb \rightarrow \pi^- \pi^+ \pi^- Pb \quad (2004)$$

The spin exotic  $J^{PC} = 1^{-+} \rho\pi$  *P*-wave

## Exotic Signatures

- Isospin exotics: “forbidden” decays
- **Spin exotics:**  $J^{PC} = 0^{--}, 0^{+-}, 1^{-+}, 2^{+-} \dots$  forbidden in  $q\bar{q}$
- Proof of existence  $\rightarrow$  strong hint for physics beyond the quark model

COMPASS (2004):  $\pi^- Pb \rightarrow \pi^- \pi^+ \pi^- Pb$   $\sim 400\,000$  events





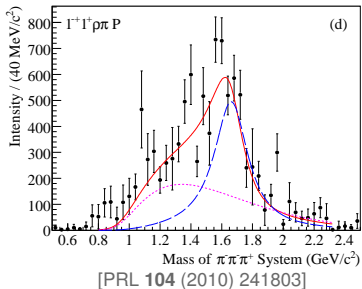
# $\pi^- Pb \rightarrow \pi^- \pi^+ \pi^- Pb$ (2004)

The spin exotic  $J^{PC} = 1^{-+} \rho\pi$  P-wave

## Exotic Signatures

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## Spin Exotic $\pi_1(1600)$

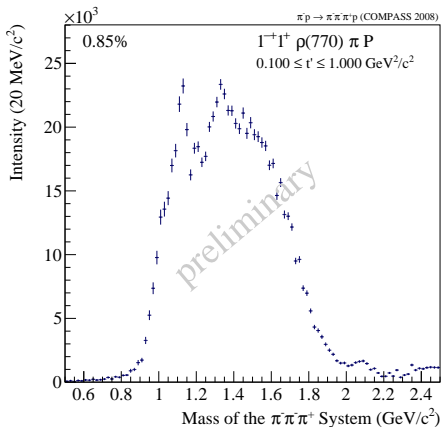
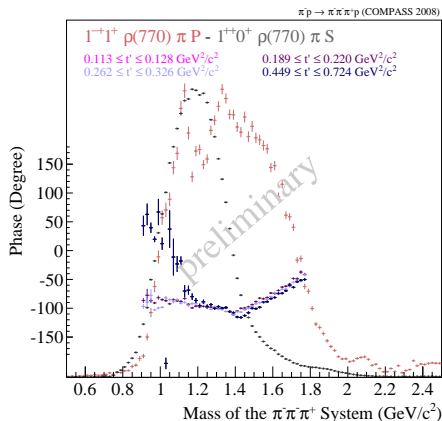
- Significant  $1^{-+}$  amplitude consistent with resonance at  $\sim 1.7$  GeV/c<sup>2</sup>
- No leakage observed ( $< 5\%$ )
- BW for  $\pi_1(1600)$  + background:  
 $M = (1.660 \pm 0.010^{+0.000}_{-0.064})$  GeV/c<sup>2</sup>  
 $\Gamma = (0.269 \pm 0.021^{+0.042}_{-0.064})$  GeV/c<sup>2</sup>



$$\pi^- p \rightarrow \pi^- \pi^+ \pi^- p \quad (2008)$$

The spin exotic  $J^{PC} = 1^{-+} \rho\pi$  P-wave

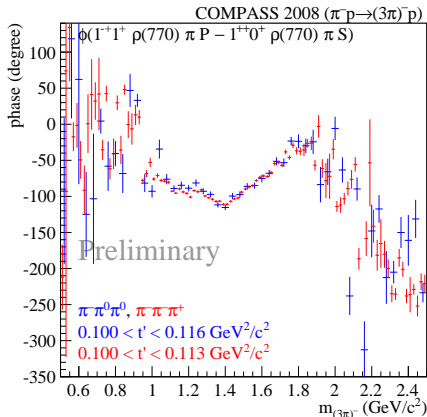
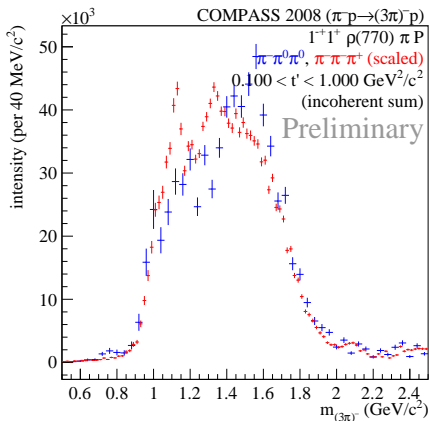
## Intensity

Phase motion vs  $1^{++} \rho\pi$  S-wave



# Comparison $\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$ vs $\pi^- p \rightarrow \pi^- \pi^0 \pi^0 p$ (2008)

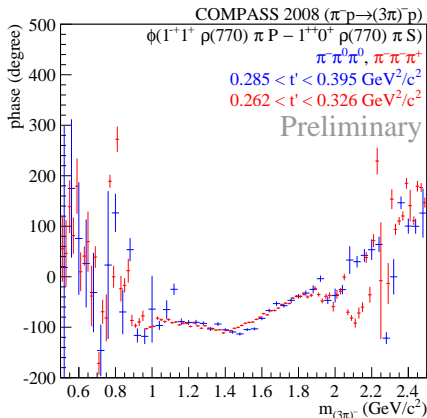
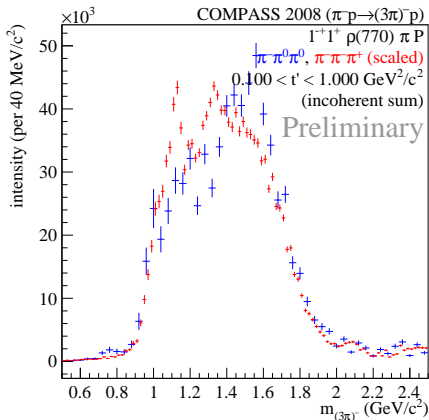
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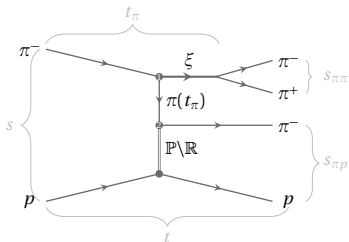




# Non-Resonant Production

## The Deck Effect

- Additional production mechanism for the same final state  $\rightarrow$  non-resonant contribution
- An incident beam pion dissociates into a  $\rho$  or  $f_2$  and a virtual  $\pi$ . The virtual  $\pi$  scatters diffractively from the target proton (via Pomeron) into a real state.



- Amplitude parametrisation:

$$\Psi(M_{\pi\pi}, t_\pi, t) = \frac{A_{\pi\pi}(M_{\pi\pi}, t_\pi)A_{\pi p}(s_{\pi p}, t)}{m_\pi^2 - t_\pi}$$

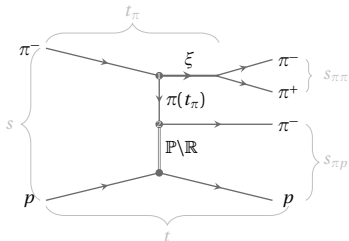
- $A_{\pi\pi}$  scattering amplitude through the  $\rho$  or/and  $f_2$
- $A_{\pi p}$   $\pi^- p$  elastic scattering amplitude



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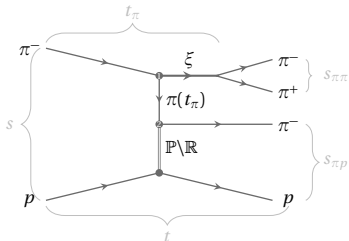




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# Studies of the Deck Contribution to the Data

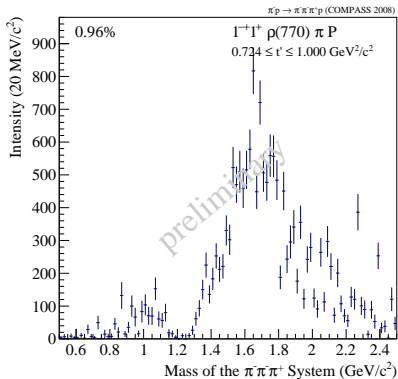
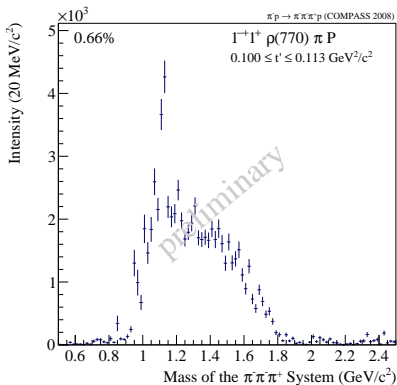
## Procedure

- Generate MC data distributed according to Deck amplitude
- Fit this data with the same model in bins of  $t'$  and  $m_{3\pi}$
- Investigate the contributions of the Deck intensity in the single waves
- Caveat: interference of the simulated Deck amplitude with diffractive production not taken into account



# $\pi^- p \rightarrow \pi^- \pi^+ \pi^- p$ (2008)

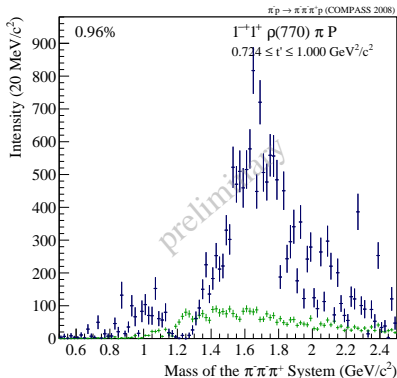
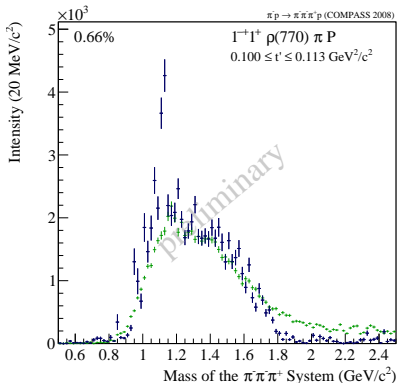
selected  $t'$  bins



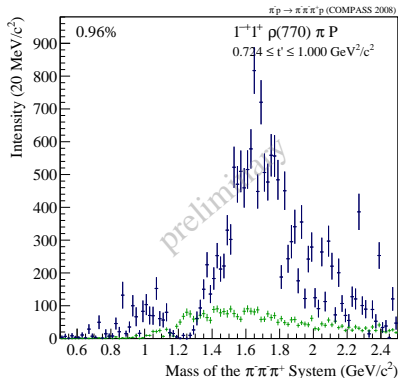
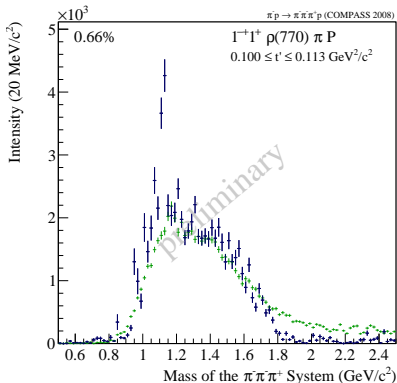


$$\pi^- p \rightarrow \pi^- \pi^+ \pi^- p \quad (2008)$$

selected  $t'$  bins, Deck overlaid



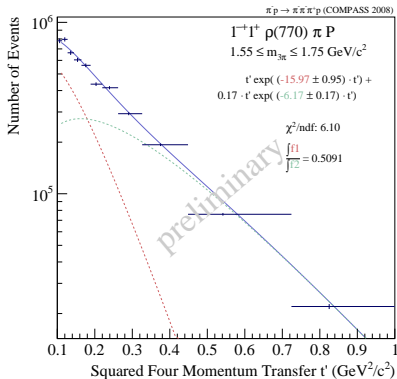


$$\pi^- p \rightarrow \pi^- \pi^+ \pi^- p \quad (2008)$$
selected  $t'$  bins, Deck overlaidDeck contribution suppressed at larger  $t'$



# $\pi^- p \rightarrow \pi^- \pi^+ \pi^- p$ (2008)

$t'$ -Dependence in  $1550 \leq m_{3\pi} \leq 1750$  MeV/ $c^2$

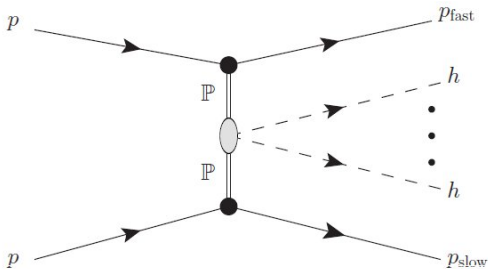


Analysis of  $t'$ -dependencies necessary in order to understand the underlying production processes.



# Isoscalar Scalar Mesons

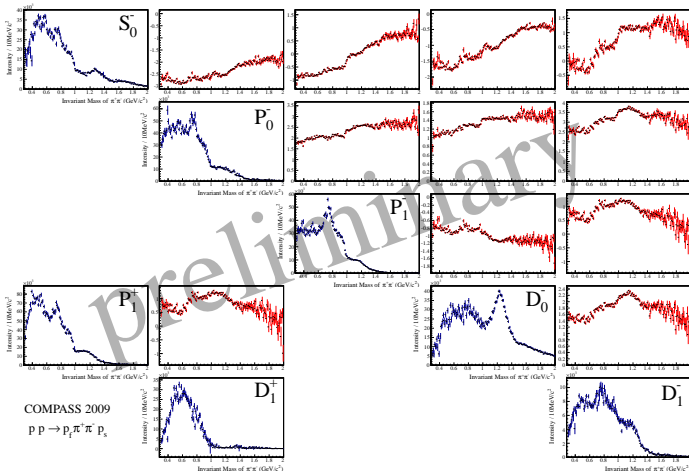
## Meson Production at Central Rapidities in $pp$ Scattering





$$pp \rightarrow p_{\text{fast}} \pi^+ \pi^- + p_{\text{slow}}$$

Amplitude Analysis of  $\pi^+ \pi^-$  System – Physical Solution after Disambiguation

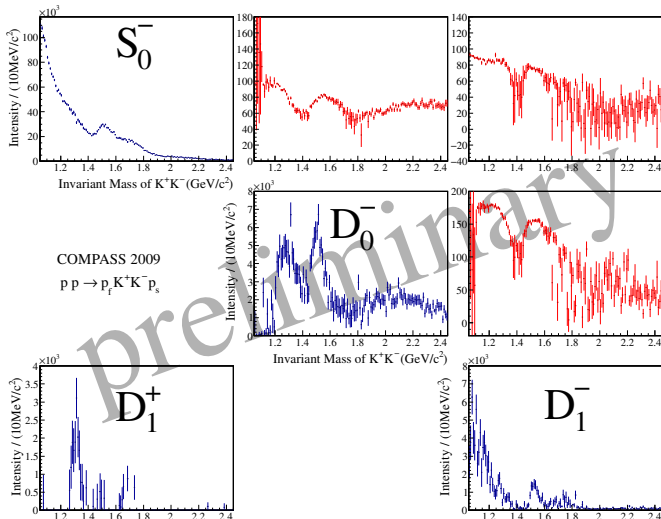






$$pp \rightarrow p_{\text{fast}} K^+ K^- + p_{\text{slow}}$$

Amplitude Analysis of  $K^+ K^-$  System – Physical Solution after Disambiguation

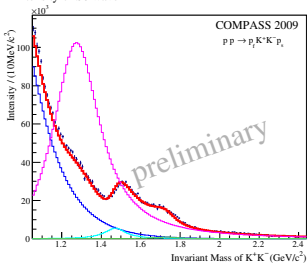




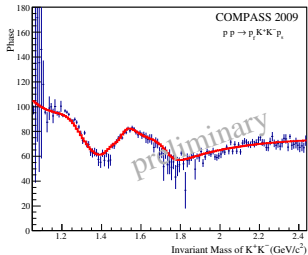
$$pp \rightarrow p_{\text{fast}} K^+ K^- + p_{\text{slow}}$$

Amplitude Analysis of  $K^+ K^-$  System – Fit of the Mass Dependence

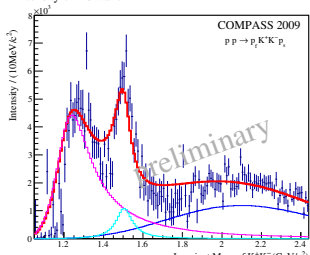
Intensity of S0 wave



Phase(S0 - D0)

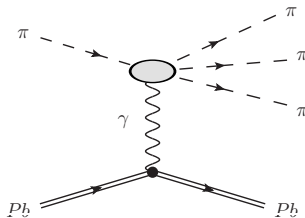
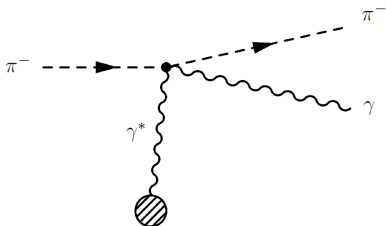


Intensity of D0 wave



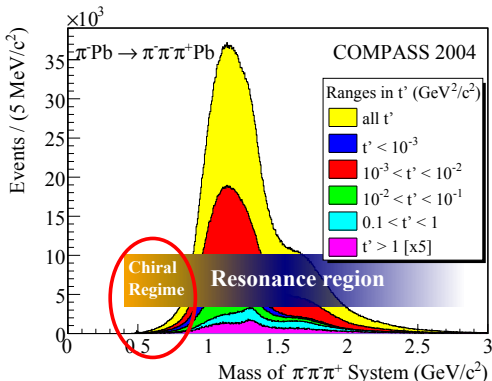
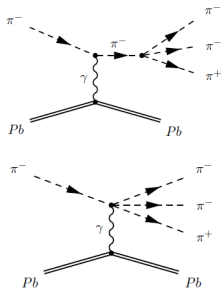


# Tests of Chiral Dynamics



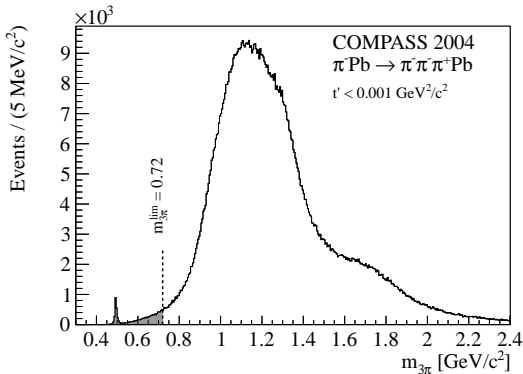
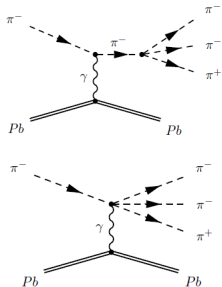


- Chiral regime (low masses,  $t' < 0.001(\text{GeV}/c)^2$ )  
→ fraction of final state events photoproduced
- Heavy nucleus acts as a quasi-real photon source
- Analysis ansatz:  $\chi$ PT amplitude included in PWA
- ⇒  $\gamma\pi^- \rightarrow \pi^-\pi^+\pi^-$  absolute cross section



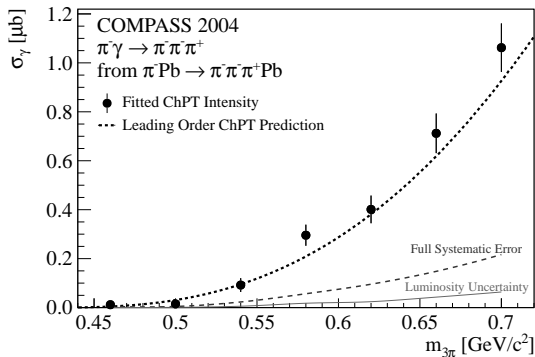
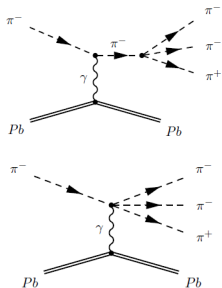


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- $\Rightarrow \gamma\pi^- \rightarrow \pi^-\pi^+\pi^-$  absolute cross section

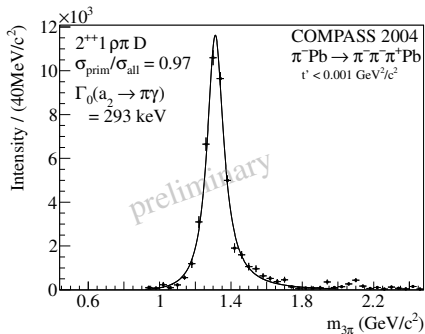




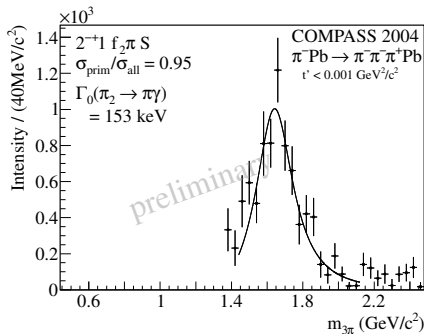
# Radiative Coupling of $a_2(1320)$ and $\pi_2(1670)$

Technische Universität München

EPJ A50 (2014) 79



$$\Gamma_0(a_2(1320) \rightarrow \gamma\pi) M2$$

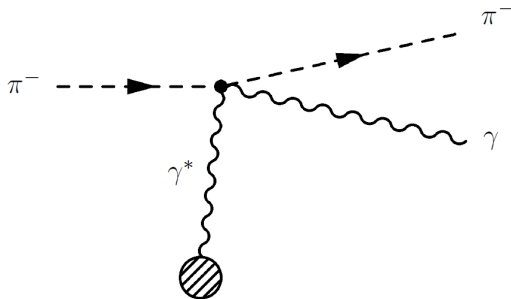


$$\Gamma_0(\pi_2(1670) \rightarrow \gamma\pi) E2$$



# Pion Polarizability

## in Primakoff–Compton Scattering



## Primakoff Compton Reaction

$$\gamma^{(*)}\pi \rightarrow \pi\gamma$$

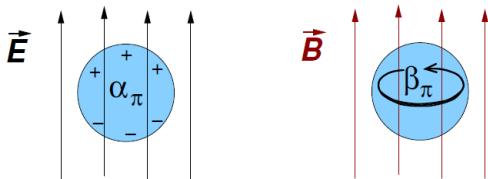
tiny extrapolation  $\gamma^* \rightarrow \gamma \quad \mathcal{O}(10^{-3}m_\pi^2)$





$$\pi + \gamma \rightarrow \pi + \gamma$$

Compton cross-section contains information about e.m. polarizability  
(as deviation from the expectation for a pointlike particle)



$\chi$ PT (2-loop) prediction by  $\chi$ PT:  $2\alpha_\pi = \alpha_\pi - \beta_\pi = (5.7 \pm 1.0)10^{-4} \text{ fm}^3$  but contradicts experimental observations (4 - 14)

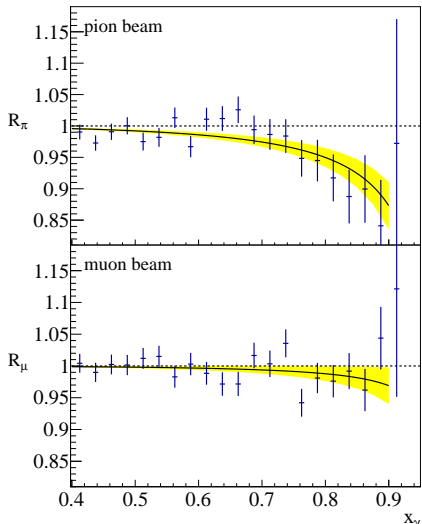
## Measurement :

- COMPASS: use pion and muon beam
- Experimentally demanding, systematics precisely to be controlled
- Assumption:  $\alpha_\pi = -\beta_\pi$



# Pion Polarizability

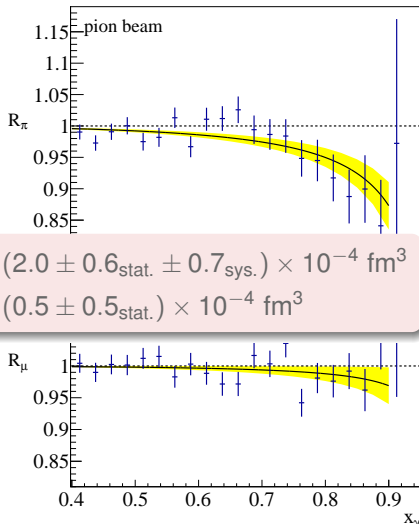
Fit to Muon and Pion Data, CERN-PH-EP-2014-109, subm. to PRL





# Pion Polarizability

Fit to Muon and Pion Data, CERN-PH-EP-2014-109, subm. to PRL





## Conclusions

- COMPASS 2008/2009: **large data sets** in
  - diffractive  $\pi^-/K^-/p$  dissociation (up to 2 orders of magnitude improvement)
- Meson Spectroscopy
  - $\pi^-\pi^+\pi^-$ ,  $\pi^-\pi^0\pi^0$ ,  $\eta\pi^-$ ,  $\eta'\pi^-$ ,  $K^-\pi^+\pi^-$ ,  $5\pi$ ,  $\pi^-\pi_{\text{isobar}}^+$
  - Central production in  $pp$  and  $\pi p$
- Baryon Spectroscopy
  - $p\pi^0$ ,  $p\pi^+\pi^-$ ,  $pK^+K^-$ ,  $p\omega$ , ...
- **Chiral dynamics:**
  - $3\pi$ -amplitude
  - Pion polarizability
- Spin alignment and violation of the OZI rule



## Outlook – Deisobared Fit of the $\pi^-\pi^+\pi^-$ Final State

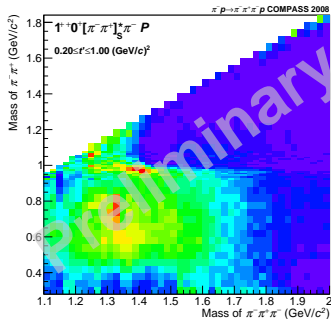
Idea: Reducing the model systematics by a simultaneous fit of the  $2\pi$  subsystem and the  $3\pi$  final state

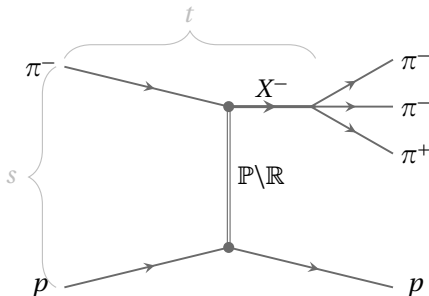


## Outlook – Deisobared Fit of the $\pi^- \pi^+ \pi^-$ Final State

Idea: Reducing the model systematics by a simultaneous fit of the  $2\pi$  subsystem and the  $3\pi$  final state

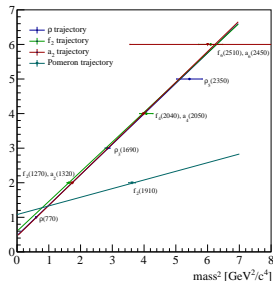
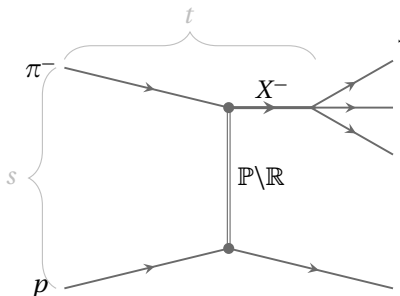
Example:  $1^{++}$  partial waves decaying via scalar isobars





$$A(s, t) \sim g_{\lambda_a \lambda_c}(t) \left( \frac{s}{m^2} \right)^{\alpha(t)} \frac{S + \exp(-i\pi\alpha(t))}{2\sin\pi\alpha(t)} g_{\lambda_b \lambda_d}(t)$$

- at COMPASS:  $s$  is fixed
- $t$  is the running variable in order to describe diffraction



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# Decay Amplitudes and Isobar Parametrizations

## 2-body Decay Amplitude

$$A(\tau) = \sum_{\lambda} D_{M,\lambda}^J(\phi, \theta, 0) f_{\lambda}(m, m_1, m_2)$$

$$f_{\lambda}(m, m_1, m_2) =$$

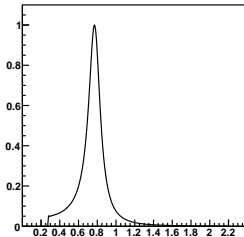
$$\underbrace{\sqrt{2I+1}}_{\text{normalization}} \underbrace{(I_1 I_{1z} I_2 I_{2z} | I I_z)(I 0 s \lambda | J \lambda)(s_1 \lambda_1 s_2 - \lambda_2 | s \lambda)}_{\text{Clebsch-Gordon coeff.}} \underbrace{F_I \Delta(m)}_{\text{dyn. func.}}$$

- Rotation functions  $D_{M,\lambda}^J(\phi, \theta, 0)$ , describing the angular part
- Clebsch-Gordan coefficients:
  - $(I_1 I_{1z} I_2 I_{2z} | I I_z)$ : Isospin coupling
  - $(I 0 s \lambda | J \lambda)$ :  $l - s$ -coupling
  - $(s_1 \lambda_1 s_2 - \lambda_2 | s \lambda)$ : spin coupling
- $F_I$ : Angular momentum barrier factors
- $\Delta(m)$ : Dynamic description of the mother state. Parametrized by:
  - Breit-Wigner forms
  - fit to the data

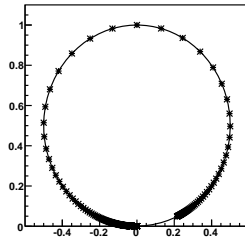


# How to parametrize the Isobar Resonances?

intensity of simple\_rho\_BW



Argand plot of simple\_rho\_BW

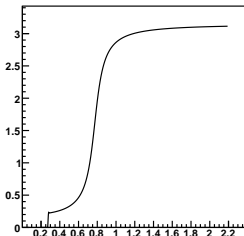


$$\Delta m = \frac{m_0 \tau_0}{m_0^2 - m^2 - i m_0 \tau_0}$$

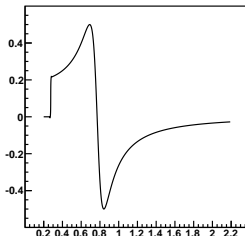
$$\text{RE} : \frac{m_0 \tau_0 (m_0^2 - m^2)}{(m_0^2 - m^2)^2 + (m_0 \tau_0)^2}$$

$$\text{IM} : \frac{m_0 \tau_0 (m_0 \tau_0)}{(m_0^2 - m^2)^2 + (m_0 \tau_0)^2}$$

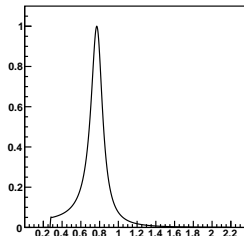
phase of simple\_rho\_BW

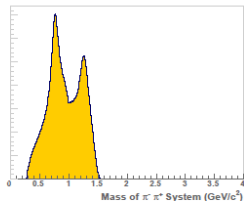
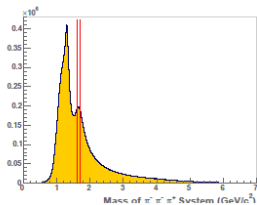


real part of simple\_rho\_BW

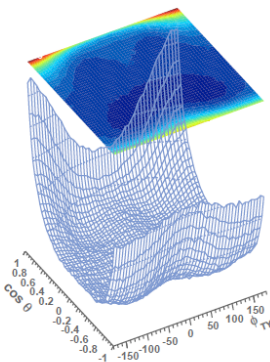


imaginary part of simple\_rho\_BW

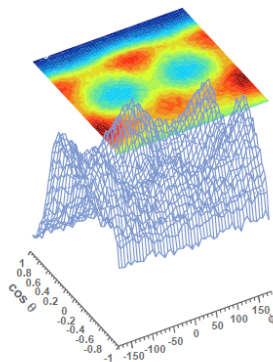




Gottfried-Jackson Reference System



Helicity Reference System





# Deck-like Monte Carlo Kinematic Distributions

