

Update on feasibility studies of Time-Like proton form factors at PANDA

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“The annual meeting of the group II of GDR-PH-QCD”



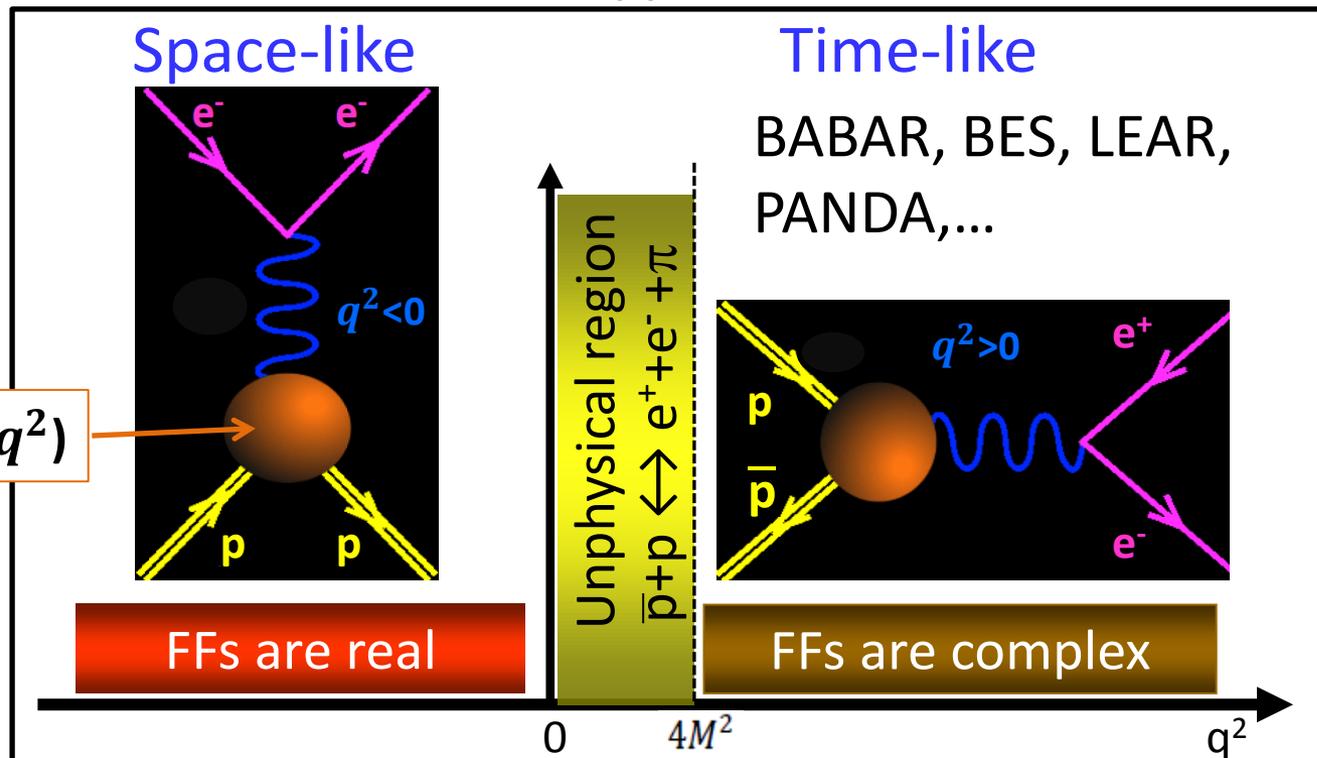
Outline

- I. **Introduction:** Measurements of the proton electromagnetic form factors in the Time-Like (TL) region
- II. Feasibility studies of the $\bar{p}p \rightarrow e^+e^-$ reaction measurement at PANDA at 3 values of total energy
- III. Determination of the **statistical error** on the proton FF ratio
- IV. Conclusions

Electromagnetic form factors

- Parametrize the EM interaction of the hadron (\neq point-like)
- In a P- and T-invariant theory, the EM structure of a particle of spin S is defined by $2S+1$ FFs: **Proton ($S=1/2$) has electric $G_E(q^2)$ and magnetic $G_M(q^2)$ FFs**
- q^2 is a kinematical invariant : $[-\infty, +\infty]$

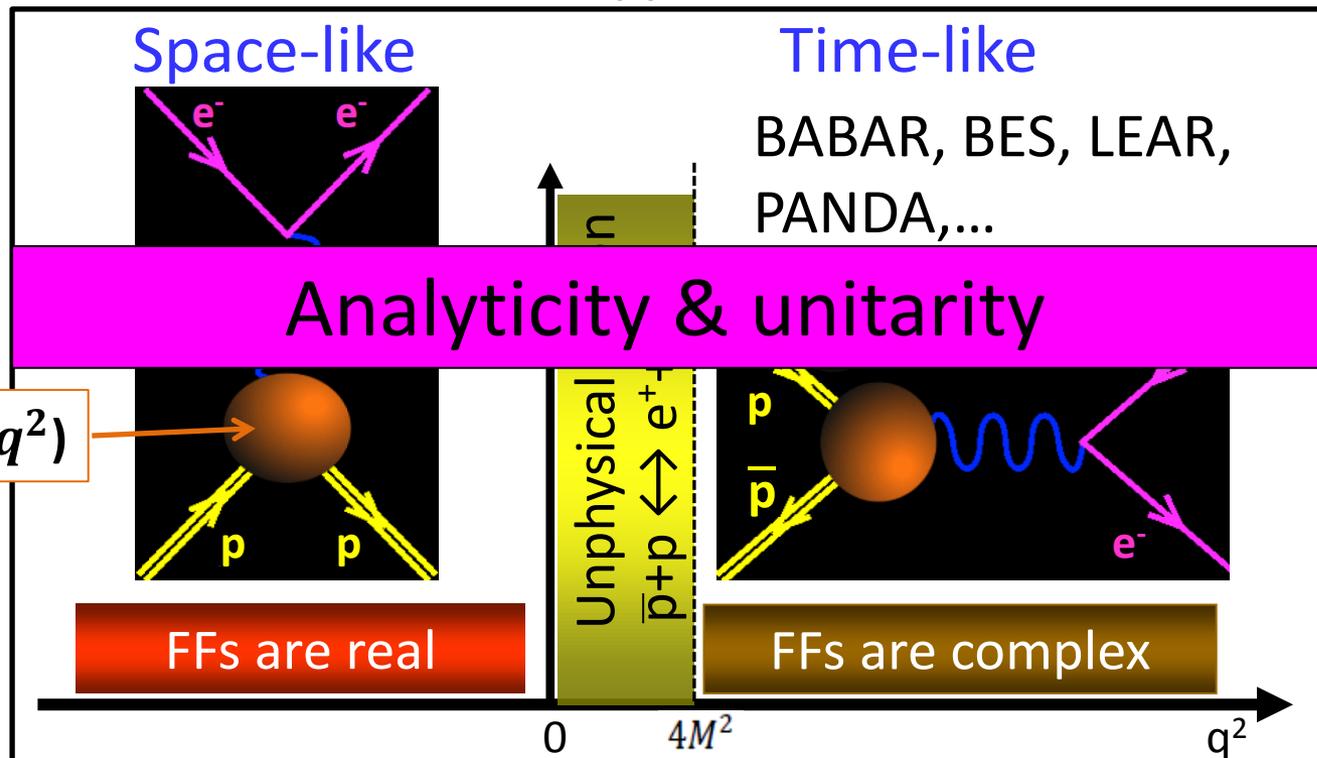
Born approximation



Electromagnetic form factors

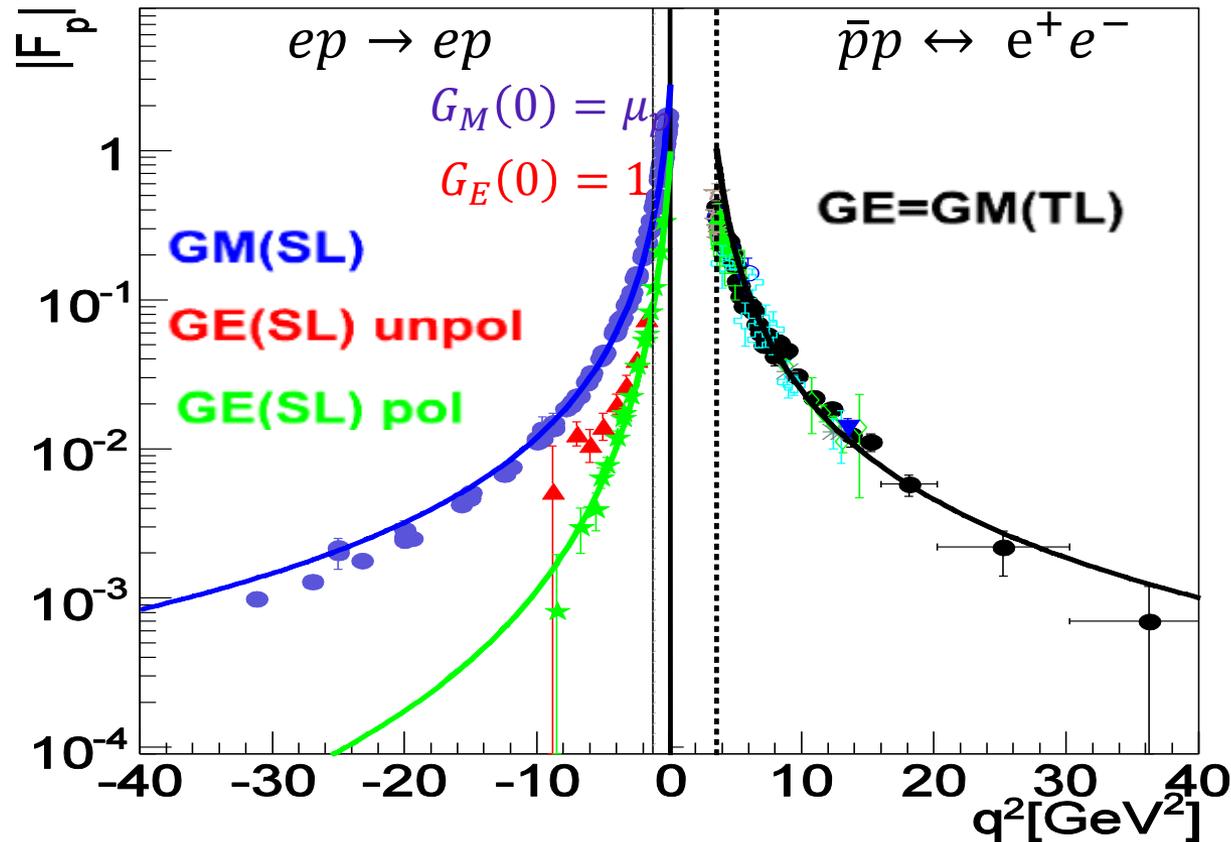
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Born approximation



$G_E(q^2), G_M(q^2)$

Data on proton electromagnetic form factors

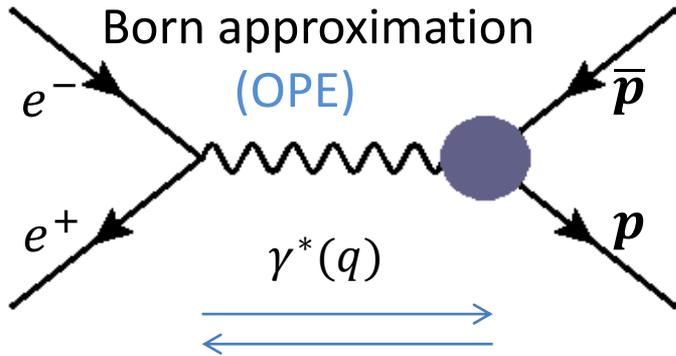


- Space-Like (SL): Discrepancy between the polarized and unpolarized data
- Time-Like (TL):
 - Individual measurement of $|G_E|$ and $|G_M|$
 - Investigation of the unphysical region

Towards a unified description of FFs in all kinematical regions

proton FF measurements in TL region

Energy scan:



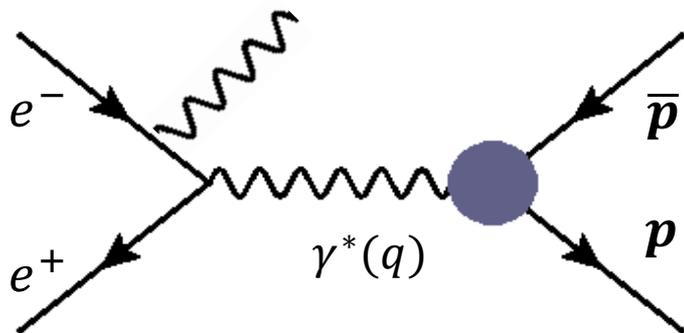
$$\frac{d\sigma}{d\cos\theta} = \mathcal{N} \left[(1 + \cos^2\theta) |G_M|^2 + \frac{4M^2}{s} \sin^2\theta |G_E|^2 \right]$$

$$= \mathcal{N} |G_M|^2 \left[(1 + \cos^2\theta) + \frac{4M^2}{s} \sin^2\theta R^2 \right]$$

$R = |G_E| / |G_M|$, \mathcal{N} is a normalization factor.

- Angular distribution of the proton (electron) $\rightarrow R = |G_E| / |G_M|$
- Angular distribution + normalization $\rightarrow |G_E|$ and $|G_M|$
- Total cross section \rightarrow effective form factor ($|G_E| = |G_M|$)

Initial State Radiation:

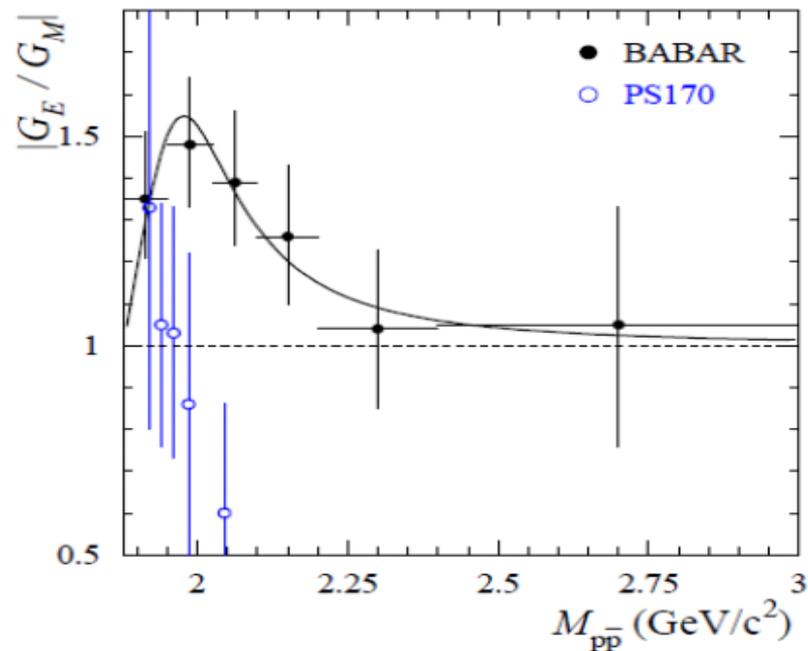


Tagged analysis: proton, antiproton and the photon need to be detected

Untagged analysis: proton and antiproton are detected. 4-momentum of the ISR photon is reconstructed

Data on the ratio of TL proton electromagnetic form factors

- 10%-24% statistical uncertainties
- Inconsistent data between BaBar and PS170
- BaBar: **ISR technique** [1.877, 3.00] GeV
- PS170 (LEAR): Low **energy scan**
- Future Data from:



BES III

- **ISR technique** (tagged+untagged) : XYZ, J/ψ , ψ' , ψ'' , $\psi(4040)$ data
- Proton FF measurement from 2.0-3.1 GeV **energy scan**,
8 energy points, Integrated luminosity = 478 pb^{-1} , $R \sim 10\%$

- PANDA (2019): **Large range of CM energy and high luminosity**



FAIR-High quality antiproton beam

Facility	Years	Momentum range [GeV/c]	Luminosity [$cm^{-2}s^{-1}$]	$\Delta p/p$
CERN-LEAR	1983-1996	0.06 – 1.94	2×10^{29}	10^{-3}
Fermilab (AA) Low energy experiments	1985-2011	< 8.9	2×10^{31}	10^{-4}
FAIR-PANDA	2018-...	1.5 – 15	2×10^{32} (10^{31})	10^{-4} 4×10^{-5}

PANDA will have:

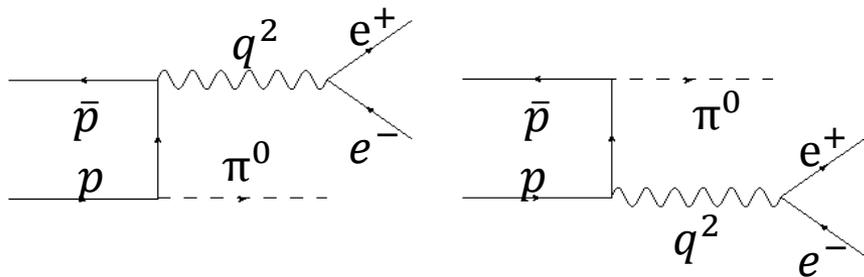
- Larger momentum range of antiproton beam
- Higher luminosity
- Improved beam momentum resolution



Measurement of TL proton FFs at PANDA: Goals

- Measurements of TL proton FFs (effective FF, **ratio**) over a large kinematical region through: $\bar{p}p \rightarrow e^+e^-$
- Individual measurement of $|G_E|$ and $|G_M|$

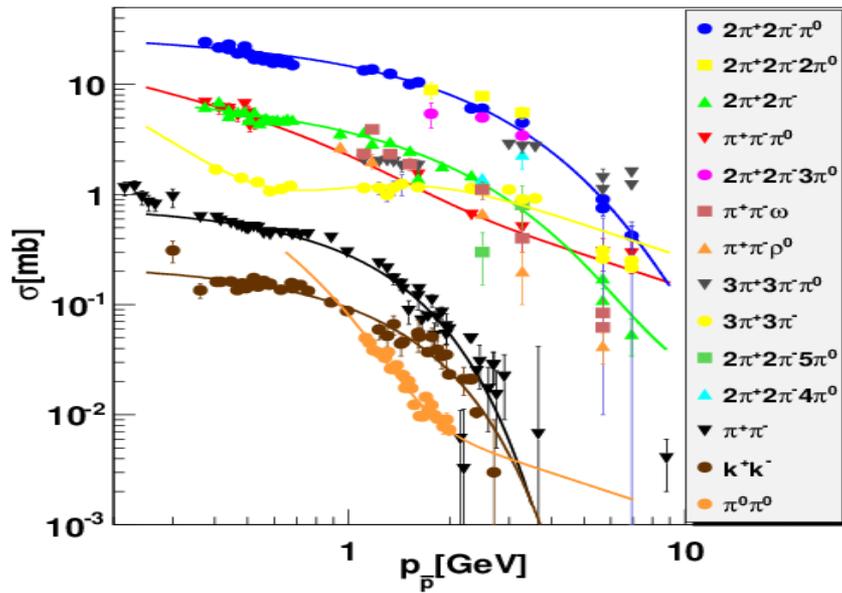
“M. Sudol *et al.* EPJ **A44**, 373 (2010)”
- Possibility to access the relative phase of proton TL FFs
 - Polarization observables (**Born approximation**) give access to $G_E G_M^*$
 - Development of **a transverse polarized proton target for PANDA in Mainz**
- Measurement of proton FFs in the unphysical region: $\bar{p}p \rightarrow e^+e^-\pi^0$



- M.P. Rekalo. *Sov. J. Nucl. Phys.*, 1:760, 1965
- Adamuscin, Kuraev, Tomasi-Gustafsson and F. Maas, *Phys. Rev. C* 75, 045205 (2007)
- C. Adamuscin, E.A. Kuraev, G. I. Gakh, ...
- Feasibility studies (J. Boucher, M. C. Mora-Espi PhD)

TL proton FF measurements at PANDA: background study

- Main issue: signal identification from the huge hadronic background
- The signal is $\bar{p}p \rightarrow e^+e^-$ and the main background is $\bar{p}p \rightarrow \pi^+\pi^-$
 - Channels with more than two charged particles in the final state can be rejected using the kinematics (missing mass)
 - The mass of pion is closer to the electron mass than other hadrons (proton and kaon)



A. Dbeyssi and E. Tomasi Gustafsson
 Prob. Atomic Sci. Technol. 2012N1, 84 (2012)

$$\frac{\sigma(\pi^+\pi^-)}{\sigma(e^+e^-)} \sim [10^5 - 10^6]$$

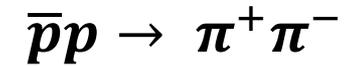
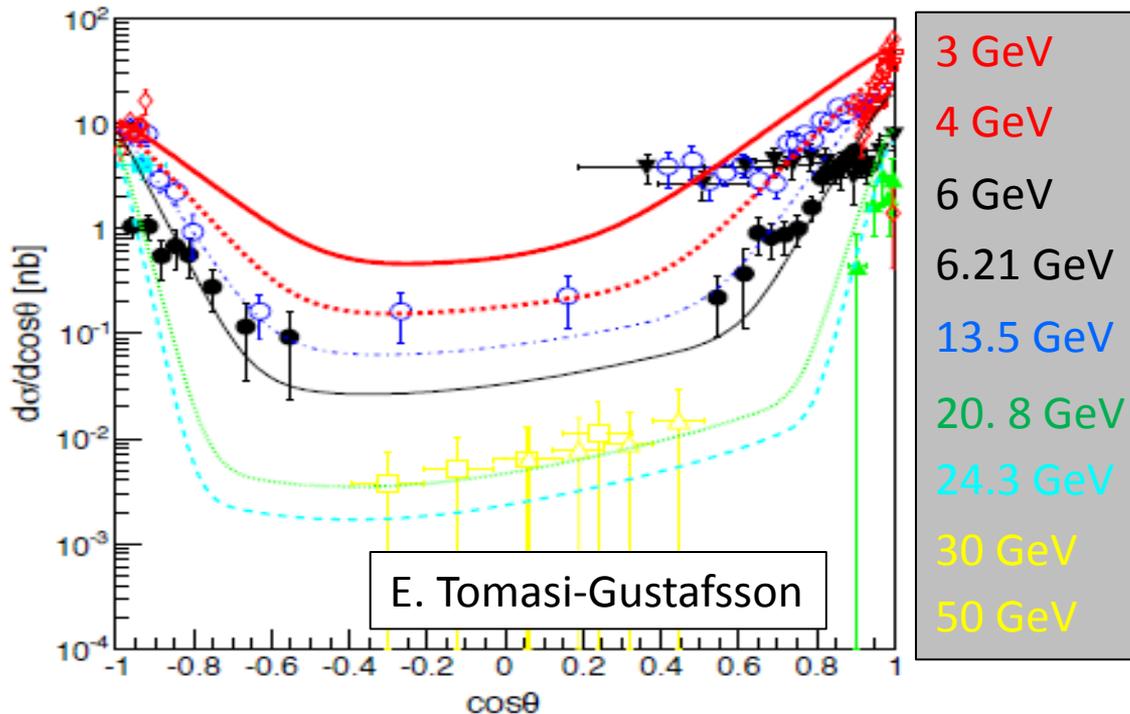
**A background rejection
 at the order of 10^{-8} is needed**

Outline of the simulation studies

- Feasibility studies of $\bar{p}p \rightarrow e^+e^-$ for the measurement of proton FF ratio at PANDA:
 - Study of the **background suppression** versus the **signal ($\bar{p}p \rightarrow e^+e^-$) efficiency**
 - Determination of the statistical error on the extracted proton FF ratio
 $R = |G_E|/|G_M|$

Based on realistic Monte Carlo simulation using **PANDARoot**,
Big amount of data have been handled by the Clusters of HIM

Background angular distribution: Data and modelisation



- Reaction mechanism is changing with the energy and the angle
- Data are very scarce not allowing to constrain parameter model

Monte Carlo event generator:

- Low energy ($p < 5$ GeV): parameters of Legendre polynomials
- High energy ($5 \text{ GeV} \leq p < 12$ GeV) : Regge inspired parametrization

Zambrana et al., "PANDA note - EventGenerators" , HIM Mainz-IPN Orsay, 2011

Description of the simulation

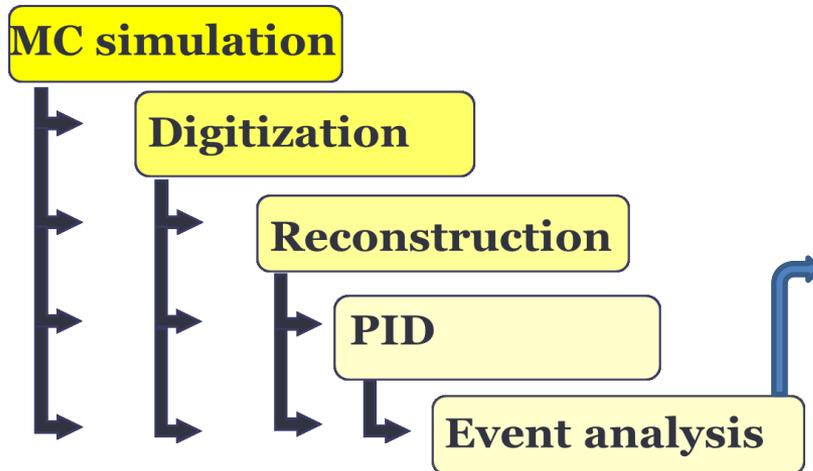
Monte Carlo parameters:

$p_{\bar{p}}$ [GeV]	1.7	3.3	6.4
$s=q^2$ [GeV ²]	5.4	8.2	13.9
Events ($\bar{p}p \rightarrow e^+e^-$)	10^6	10^6	10^6
Events ($\bar{p}p \rightarrow \pi^+\pi^-$)	10^8	10^8	10^8

- PHSP (PHase Space, GEANT4)
 - $\bar{p}p \rightarrow e^+e^-$
 - *PHOTOS* is switched on
- $\bar{p}p \rightarrow \pi^+\pi^-$: $\cos\theta = [-0.8, 0.8]$

PANDARoot version: 25544 (apr13)

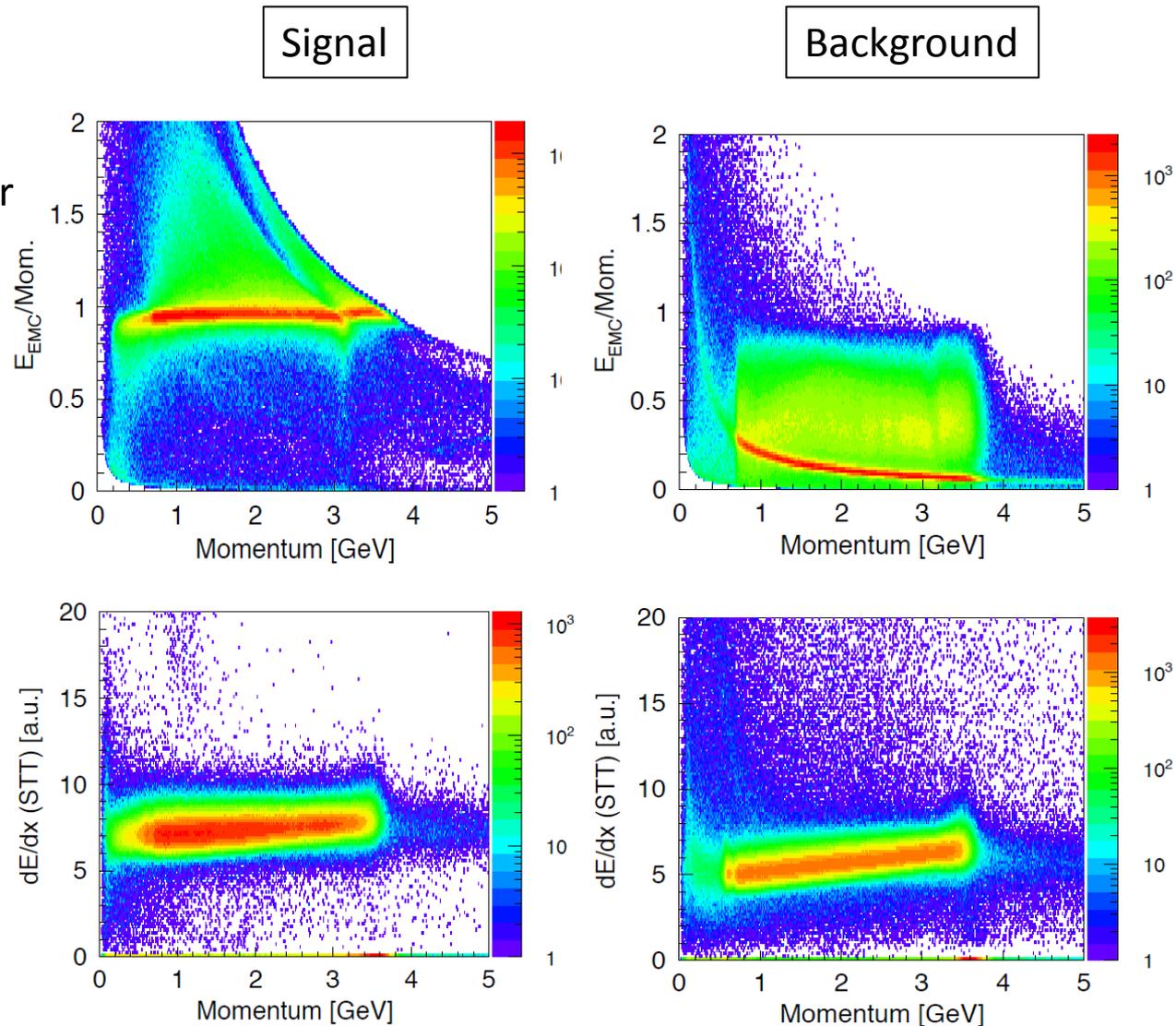
Standard chain of simulation and analysis in PANDARoot:



- One positive and one negative particle per event
- Best **back to back pair** in the CM is selected among all possible pairs (positive and negative particles) per event
- PID probabilities and kinematics cuts are applied to the selected events

Reconstructed PID variables

- Energy deposit , shower shape, ... in the **ElectroMagnetic Calorimeter**
- Energy loss in the **Straw Tube Tracker** and **Micro Vertex Detector**
- Cherenkov angles (Cherenkov detectors DIRC)
- Other kinematical and PID variables



PID and kinematical Cuts

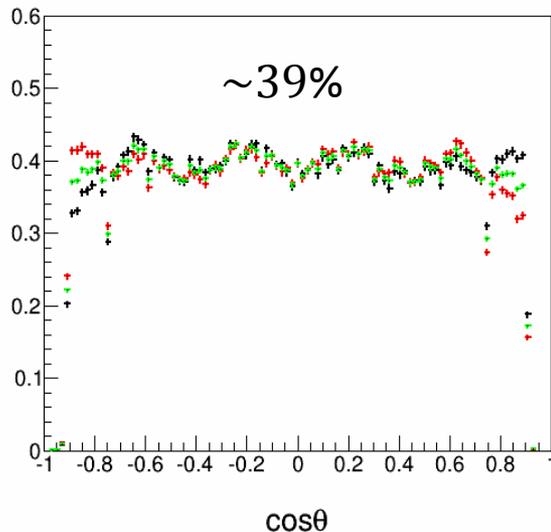
s [GeV ²]	5.4	8.2	13.9
Total PID prob.	>99%	>99%	>99.9%
Individual PID _{<i>i</i>} prob.	EMC >0.3 STT >0.33 MVD>0.05	EMC >0.63 STT >0.37	EMC >0.06 STT >0.11
$ \phi - \phi' $		[178°-185°]	[175°-185°]
Invariant mass [GeV]	>1.5		> 2.7
Background rejection factor	10^{-8}	10^{-8}	10^{-8}

- PID --> probability for the detected particle to be identified as the signal.
- PID information are taken from **EMC**, **STT**, **DIRC** and **MVD** subdetectors.

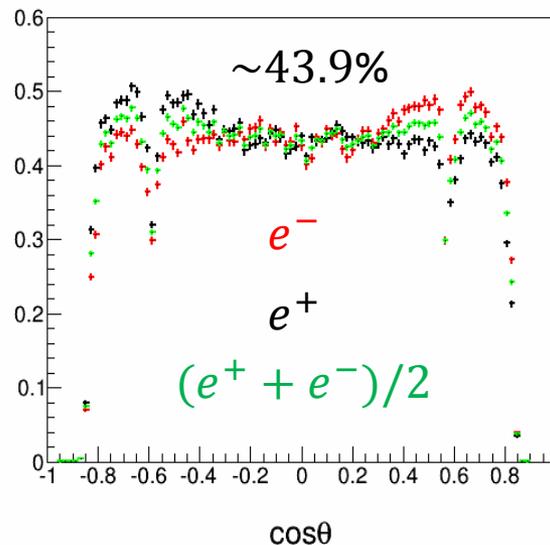
Signal efficiency after background suppression

ϵ = Selected events (e^+e^-) after the cuts/MC events (e^+e^-)

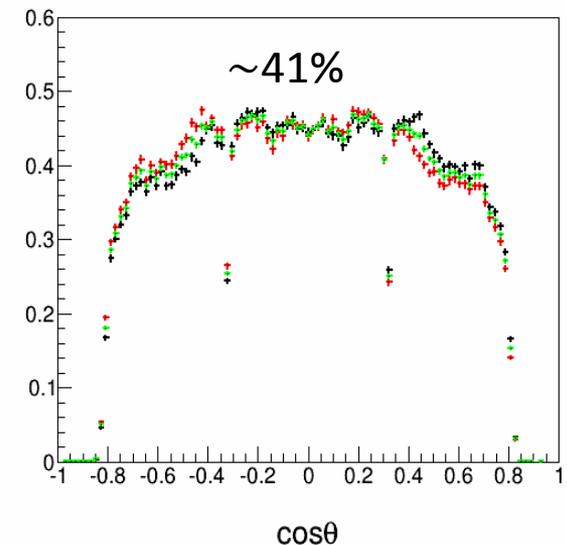
$s = 5.4 \text{ GeV}^2$



$s = 8.2 \text{ GeV}^2$



$s = 13.9 \text{ GeV}^2$



Analysis for proton FF measurements is limited to the region
 $\cos\theta = [-0.8, 0.8]$ in the CM

From PHSP to physical angular distributions

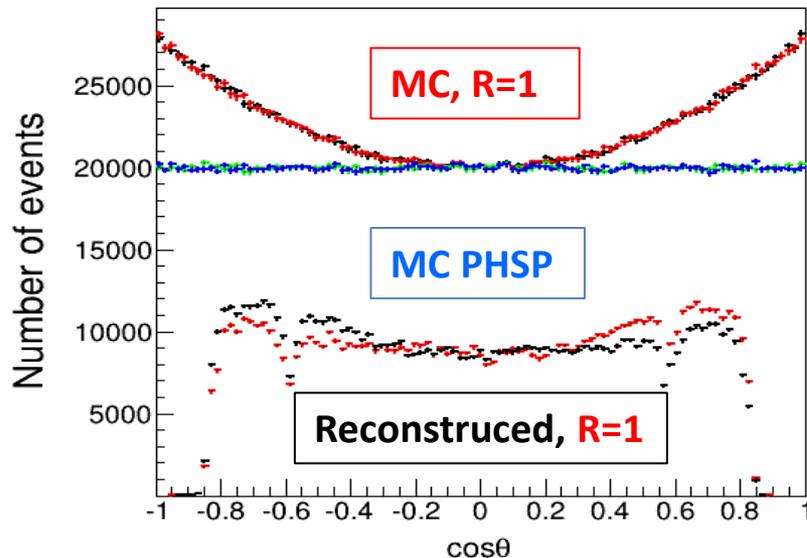
The differential cross section in the CM for $\bar{p}p \rightarrow e^+e^-$ is:

$$\frac{d\sigma}{d\cos\theta} = \sigma_0(1 + \mathcal{A} \cos^2\theta)$$

$$\left\{ \begin{array}{l} \sigma_0 = \frac{d\sigma}{d\cos\theta} \left(\theta = \frac{\pi}{2} \right) \\ \mathcal{A} = \frac{\tau - R^2}{\tau + R^2}, R = |G_E|/|G_M|, \tau = \frac{s}{4M^2} \end{array} \right.$$

A. Zichichi et al., Nuovo Cim. 24 (1962) 170

E. Tomasi-Gustafsson and M.P. Rekalo, Phys.Lett. B504 (2001) 291-295



Monte Carlo events, PHSP

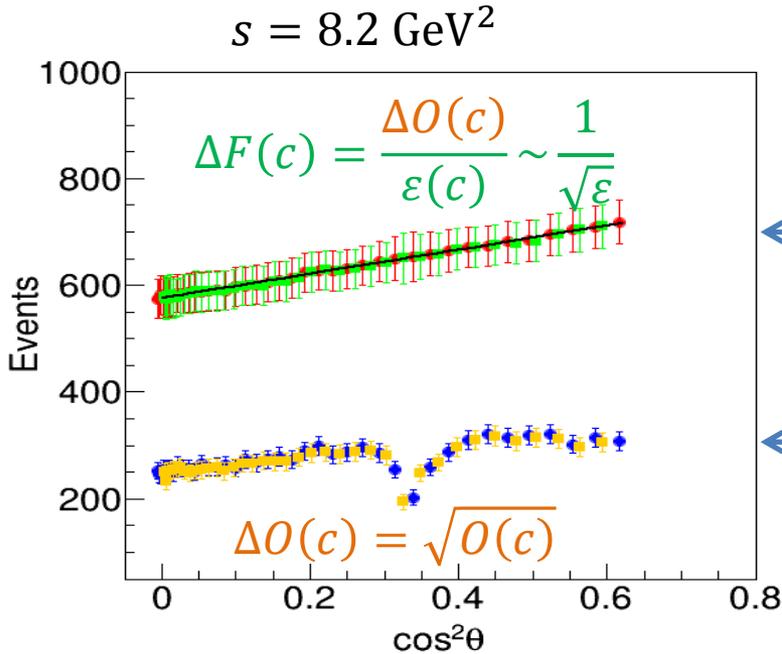
× Weight: $1 + \mathcal{A} \cos^2\theta$

Physical Monte Carlo events

× Efficiency $\epsilon(c)$

Physical reconstructed events

Efficiency correction and linear fit



- The observed events are **corrected** by the efficiency: $F(c) = \frac{O(c)}{\epsilon(c)}$

- The events are normalized according to the expected counting rate: $O(c)$

➤ Linear fit to the signal (e^+e^-) events as a function of $\cos^2\theta$

- Fit function: $y = a_0 + a_1 x$, $x = \cos^2\theta$

$$\frac{d\sigma}{d\cos\theta} = \sigma_0(1 + \mathcal{A} \cos^2\theta)$$

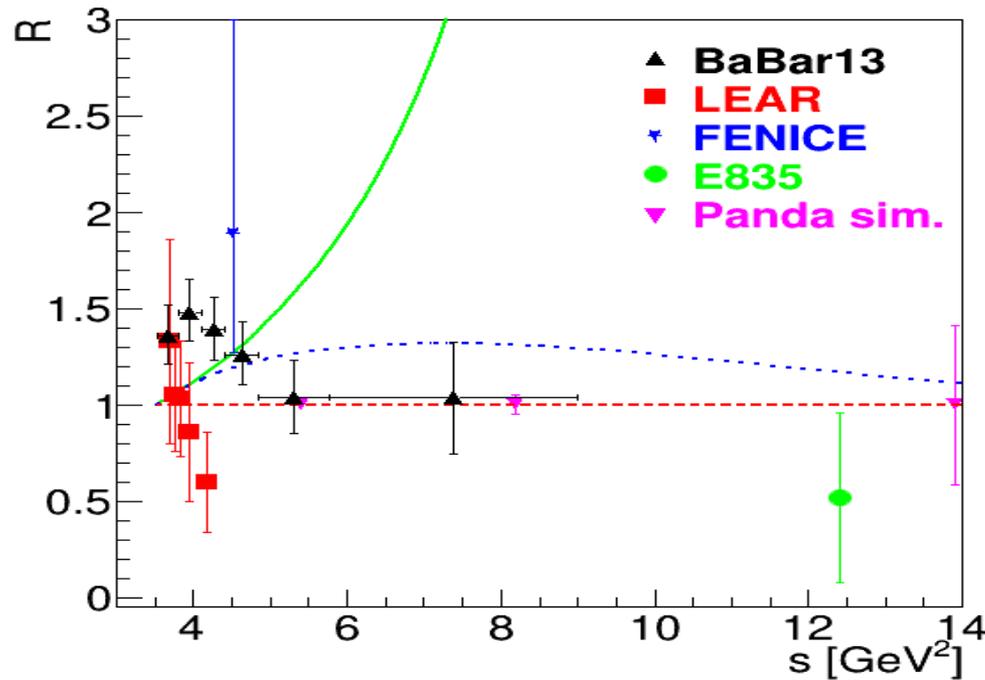
- The slope a_1 is related to \mathcal{A}

- Error on R through: $\mathcal{A} = \frac{\tau - R^2}{\tau + R^2} \rightarrow \Delta R = \frac{1}{R} \frac{\tau}{(1 + \mathcal{A})^2} \Delta \mathcal{A}$

Results ($R=1$)

s [GeV ²]	\mathcal{A}	$\mathcal{A} \pm \Delta\mathcal{A}$	R	$R \pm \Delta R$
5.4	0.21	0.217 ± 0.011	1	0.993 ± 0.011
8.2	0.4	0.393 ± 0.041	1	1.007 ± 0.049
13.9	0.59	0.588 ± 0.268	1	1.01 ± 0.415

The **extracted values** are compatible with the **Monte Carlo input**



F. Iachello et al., Phys. Rev. C 69 (2004) 055204

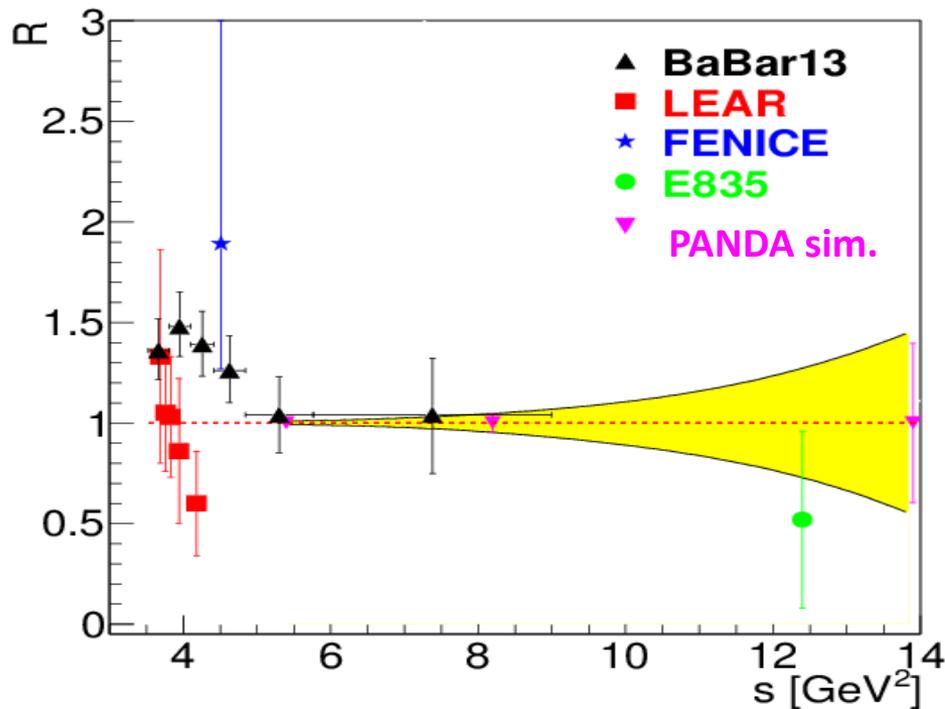
E. L. Lomon, Phys. Rev. C 66 (2002) 045501

E. Tomasi-Gustafsson et al., Eur. Phys. J. A 24, 419 (2005)

V. A. Matveev, S. J. Brodsky, D. V. Shirkov....

Comparison with previous simulations

s [GeV ²]	$R \pm \Delta R$	$R \pm \Delta R$ (new simulation)
5.4	0.992 ± 0.009	0.993 ± 0.011
8.2	0.997 ± 0.045	1.007 ± 0.049
13.9	1 ± 0.396	1.01 ± 0.415



- New version of PANDARoot
- More background events have been generated

Expected statistical precision using the **BaBar** framework for $R=1$.
 [M. Sudol *et al.* EPJ A44, 373 (2010)]

Points under investigation

- Determination of the statistical errors on the individual proton form factors
- Efficiency extrapolation and effective form factor determination at large energies
- Second analysis done by Dmitry Khanef (HIM Mainz) :
 - Different event generator for the signal
 - Different PID and kinematical cuts
 - Different fit functions (study of the correlation matrix elements)
- Radiative corrections to the annihilation reactions $\bar{p}p \rightarrow e^+e^-$
 - Event generator for PANDA
 - Simulation and analysis studies:
effect of radiative correction on the proton form factors

Conclusions

- Feasibility studies (PANDARoot) for measuring proton TL EM FFs at PANDA:
 - Three values of the momentum transfer squared are considered $q^2 = s = \mathbf{5.4, 8.2}$ and $\mathbf{13.9}$ GeV²
 - The suppression of the main background at the order of $\mathbf{10^{-8}}$ is achieved keeping sufficient signal efficiency
 - The proton FF ratio can be measured at PANDA with unprecedented statistical accuracy

Thank you for your attention

PID and kinematical Cuts

Previous simulations

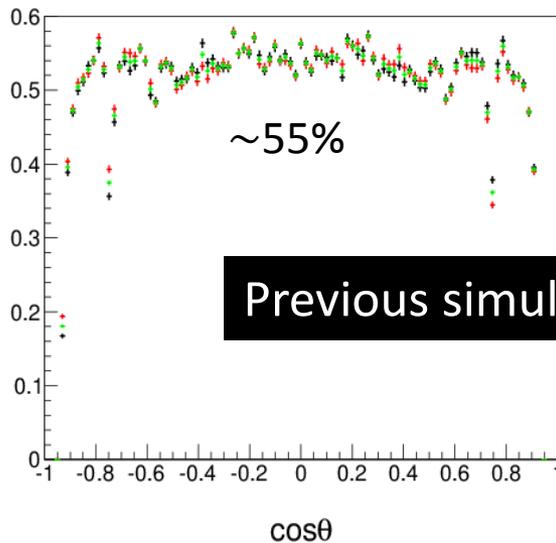
s [GeV ²]	5.4	8.2	13.9
Total PID prob.	>99%	>99%	>99.9%
Individual PID _{<i>i</i>} prob.	>5%	>5%	>6%
Number of fired crystals in the EMC	>5	>5	>5
$(\theta + \theta')$ [CMS]	[178°-182°]	[178°-182°]	[175°-185°]
$ \phi - \phi' $	[178°-182°]	[178°-182°]	[175°-185°]
Invariant mass [GeV]	No cut	> 2.14 GeV	> 2.5 GeV
Background [Events]	0	0	0

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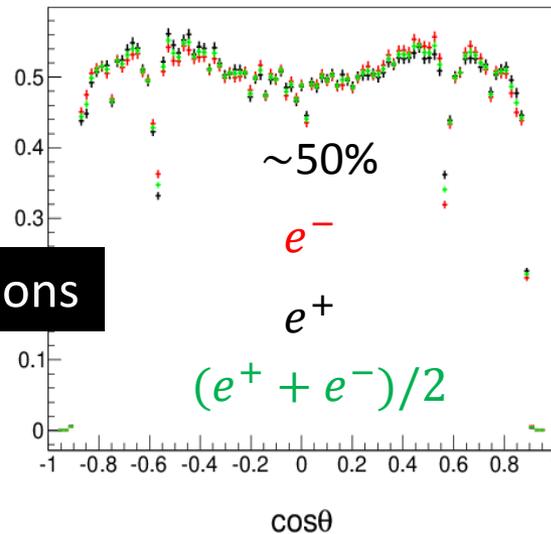
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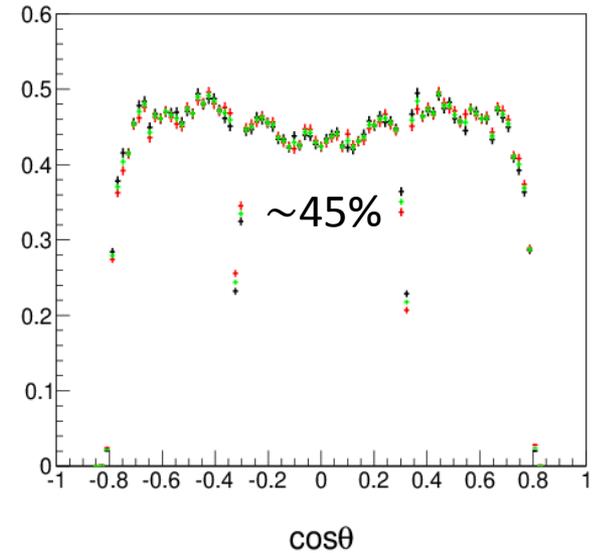
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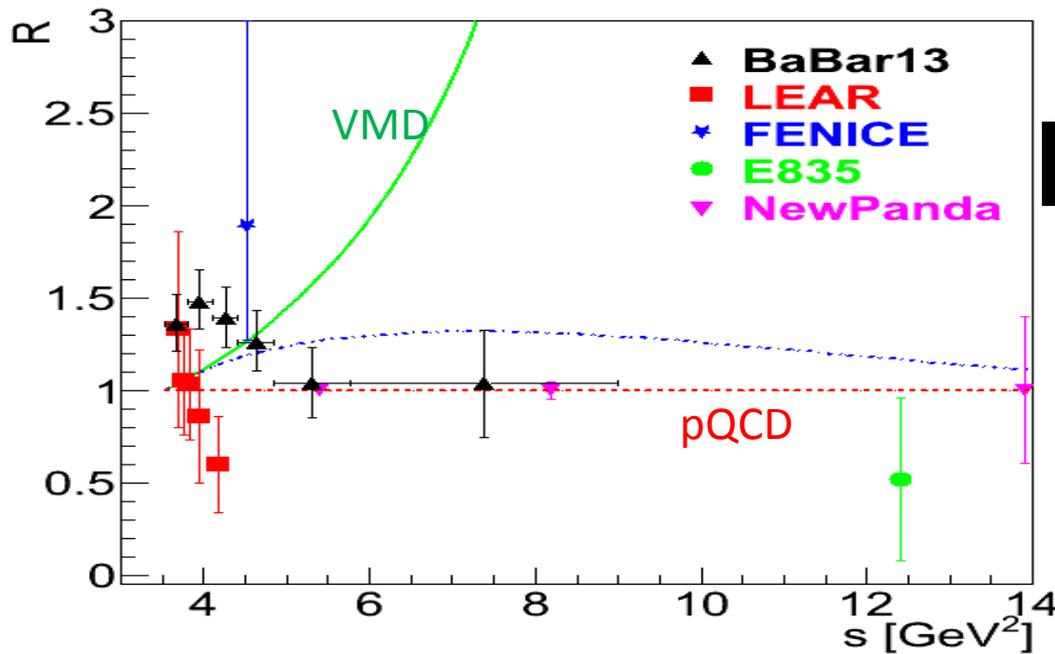
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 $\cos\theta = [-0.8, 0.8]$ in the CM

Results:

s [GeV ²]	\mathcal{A}	$\mathcal{A} \pm \Delta\mathcal{A}$	R	$R \pm \Delta R$
5.4	0.21	0.218 ± 0.009	1	0.992 ± 0.009
8.2	0.4	0.401 ± 0.038	1	0.997 ± 0.045
13.9	0.59	0.595 ± 0.255	1	1 ± 0.396

The **extracted values** are compatible with the **Monte Carlo input**



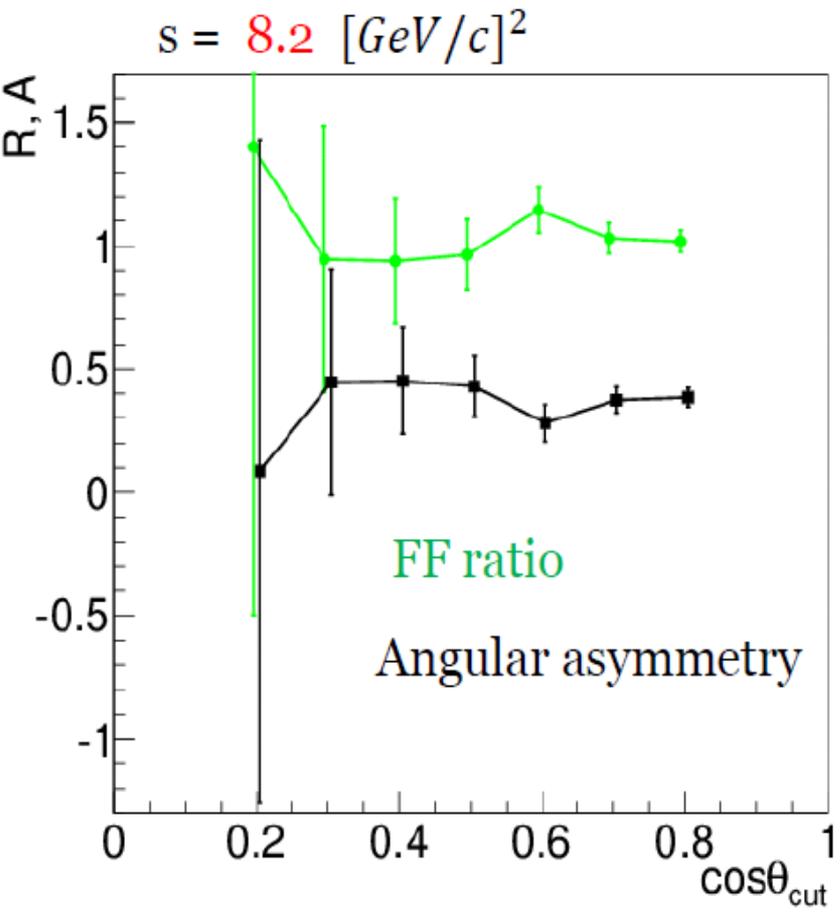
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 V. A. Matveev, S. J. Brodsky, D. V. Shirkov....

Effect of the angular cut

Previous simulations



Experimental data on \mathbf{R} have been extracted in the region of $|\cos\theta| < 0.8$:

Small effect of the angular cut

M. Ambrogiani et al., PRD 60 (1999)
Bardin NPB 411 (1994)

$\cos\theta_{cut}$	0.8	0.6
ΔR	0.045	0.092