

# The shape of the universe and cosmological parameters estimation.

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Montpellier, May 28th, 2014



# Inflation

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“The results of Eqs. (68a) and (68b) suggest that our Universe is spatially flat to an accuracy of better than a percent.”

This does not result from a pure **geometrical test** on our 3D space.



## Robertson-Walker metric

$$ds^2 = -c^2 dt^2 + a(t)^2 \left[ r^2 (d\theta^2 + \sin^2 \theta d\phi^2) + \frac{dr^2}{1 - kr^2} \right]$$

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and :

## General Mattig relation

$$r = S_k \left( \int_{t_S}^{t_0} \frac{cdt}{a(t)} \right)$$

# Basics of cosmology

## Dynamic

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General Relativity

$$K = kc^2$$

so

$$\Omega_k = 1 - \sum \Omega_{contents}$$

# Testing GR at cosmological scales

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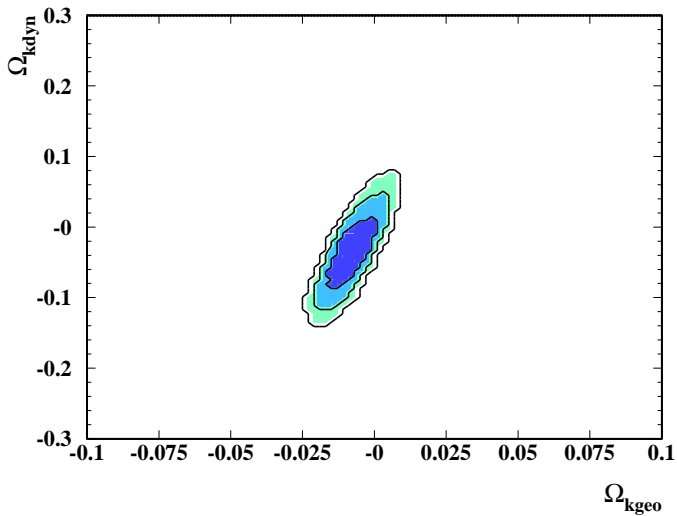
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and

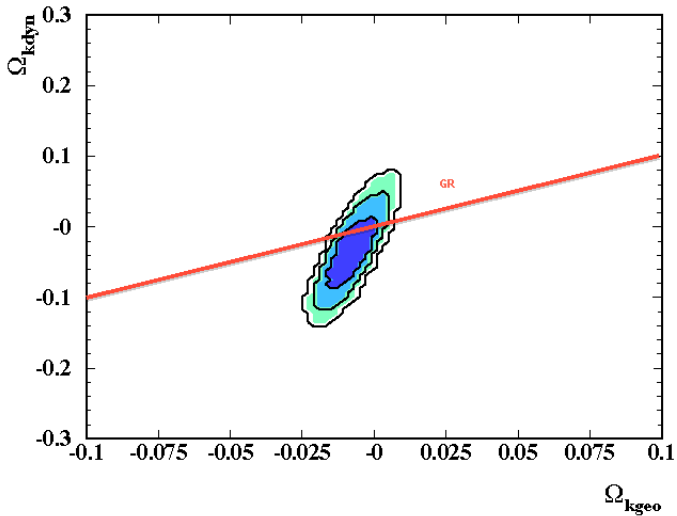
$$\Omega_{kdyn} = 1. - \sum \Omega_{contents}$$

and use SNIa, CMB, BAO to constrain these quantities.

With  $w = -1$

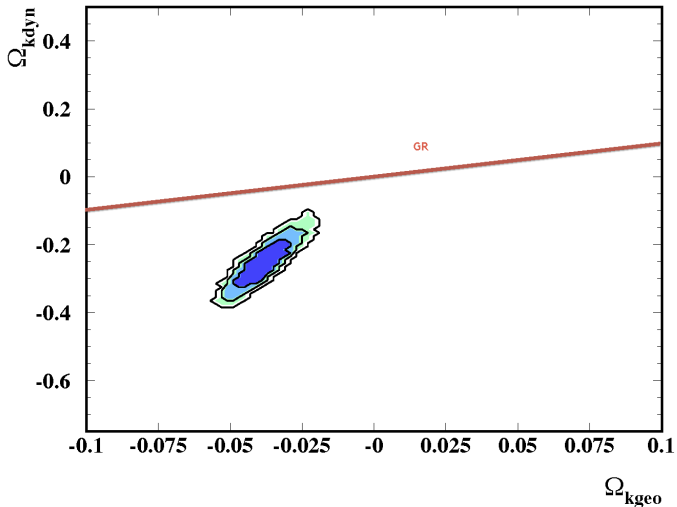


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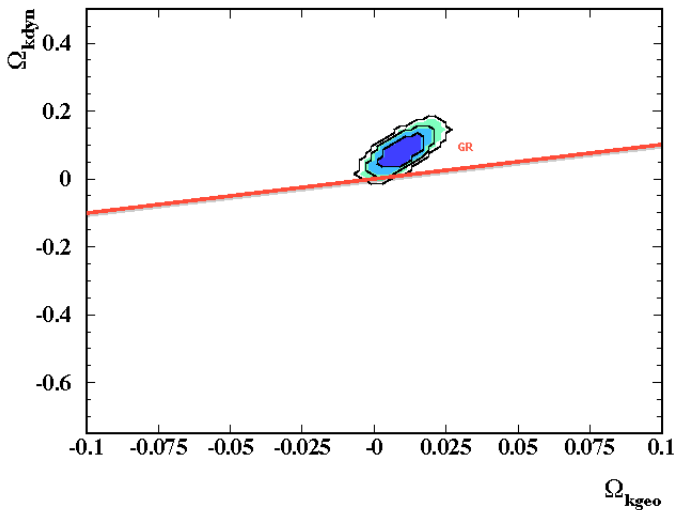
# With different equation of state

$$w = -0.8$$



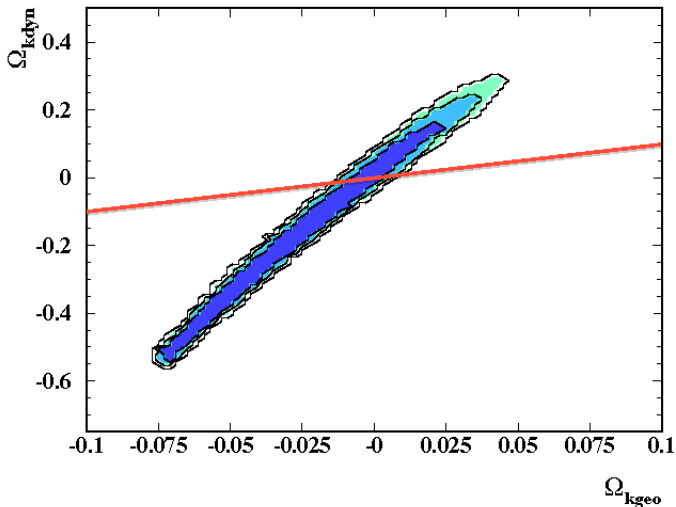
# With different equation of state

$$w = -1.2$$



# With different equation of state

$w = \text{marginalized}$



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Thank You