



Top mass standard reconstruction at the Tevatron

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for the D0 and CDF collaborations*

7th International Workshop on Top Quark Physics
September 30, 2013

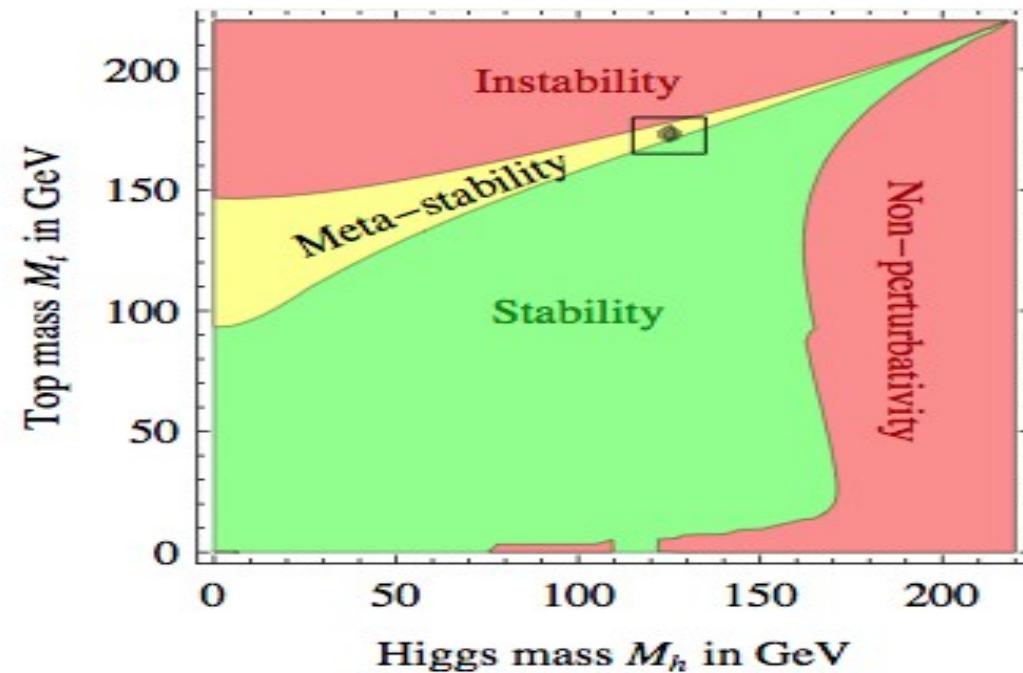
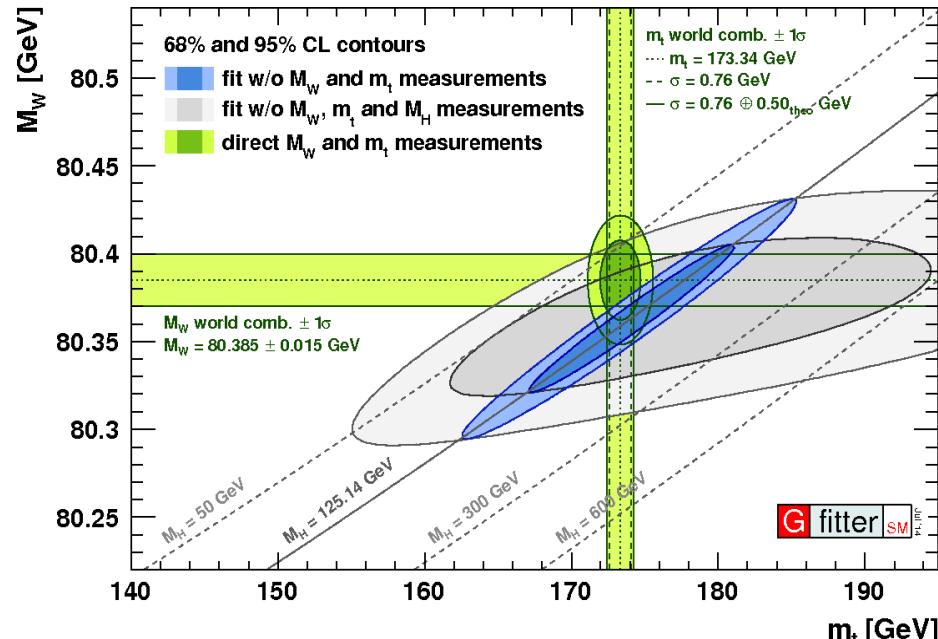
Why?

Theoretician answers:

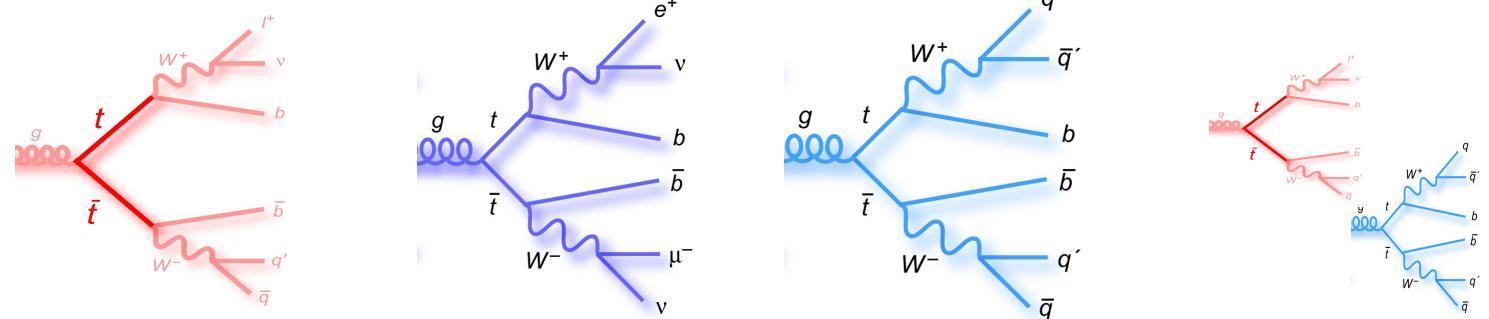
- Standard Model self-consistency
- Higgs potential \Rightarrow Universe Stability

Experimentalist answer

- Because we can measure with high precision!

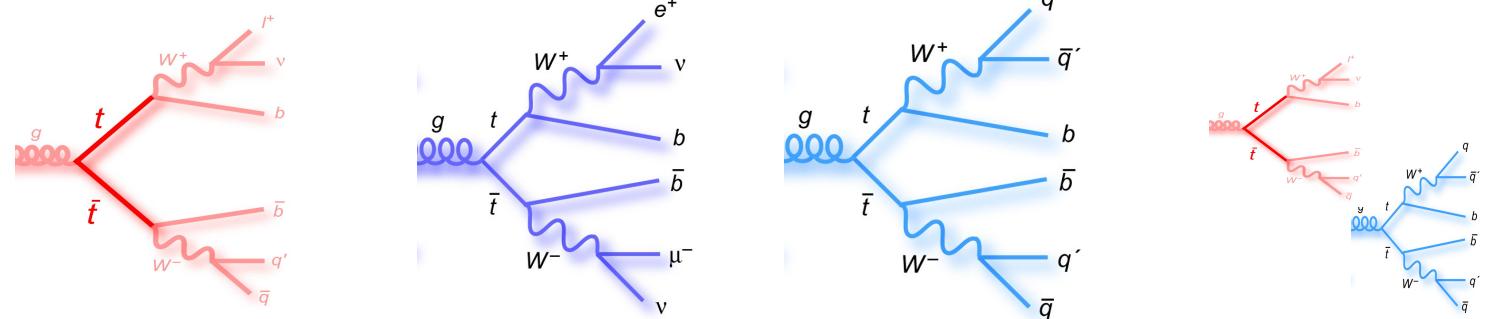


How?



	Lepton + jets	Dileptons	All-jets	MET+jets
Templates	CDF, 8.7 fb^{-1}	CDF: 9.1 fb^{-1} D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}	CDF, 9.3 fb^{-1} Soon: D0, 9.7 fb^{-1}	CDF, 8.7 fb^{-1}
Matrix Element	D0, 9.7 fb^{-1}	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}		
From cross-section	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}		
Lepton pT	CDF 2.7 fb^{-1}	CDF 2.8 fb^{-1}		

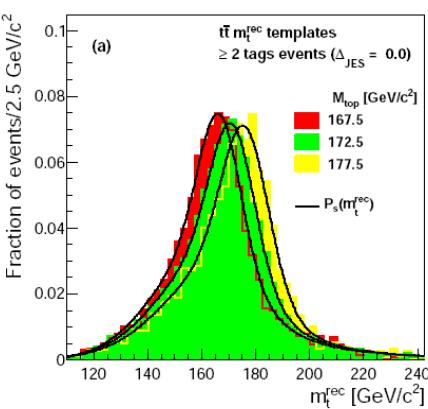
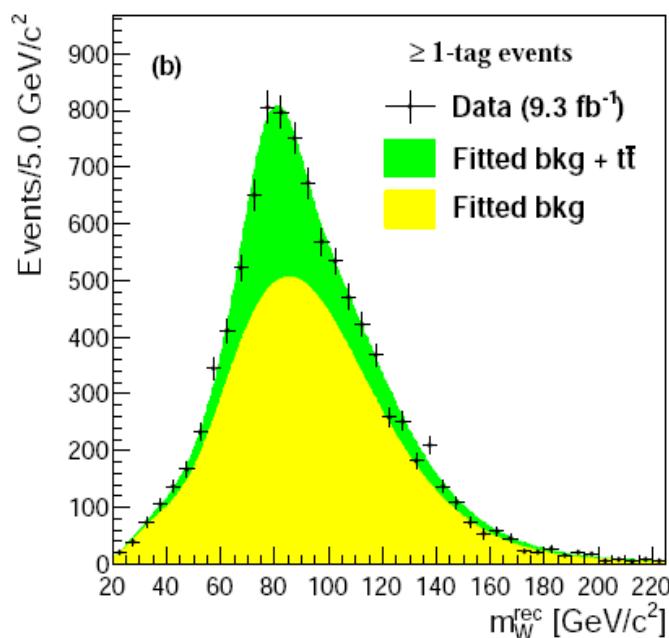
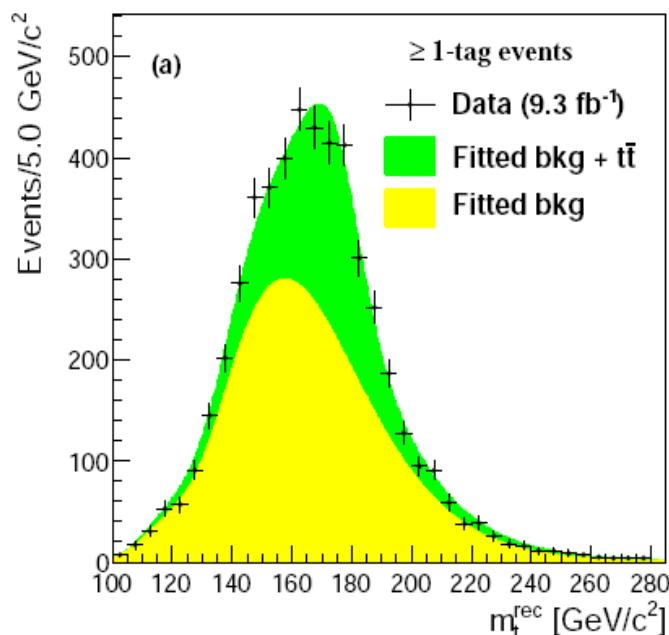
How?



	Lepton + jets	Dileptons	All-jets	MET+jets
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Matrix Element	D0, 9.7 fb^{-1}	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}		
From cross-section	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}		
Lepton pT	CDF 2.7 fb^{-1}	CDF 2.8 fb^{-1}		

For the top mass combinations see Yvon Peter's talk on Wednesday

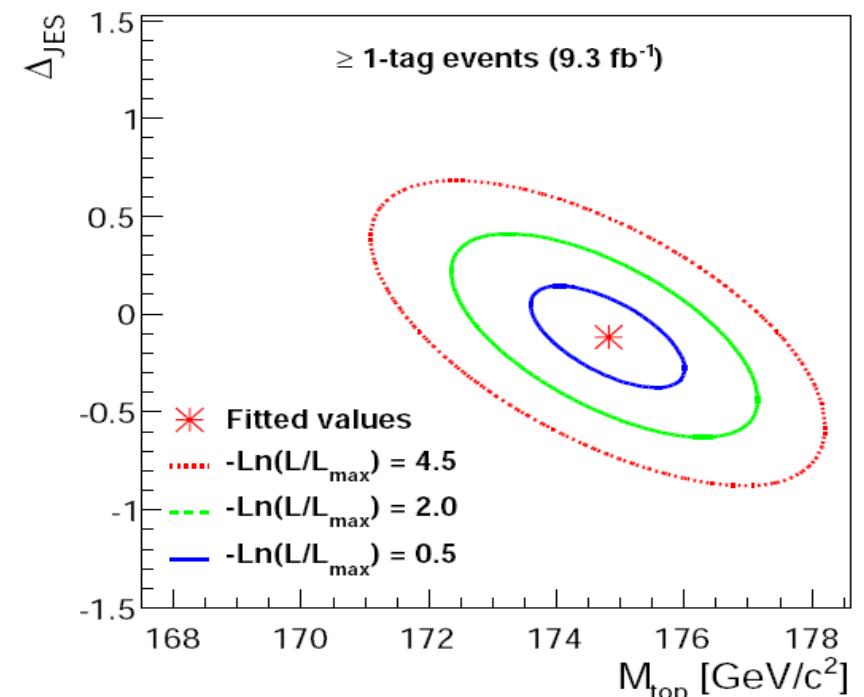
- $t\bar{t}$ simulation: Powgen+Pythia
- Selection
 - 6 – 8 jets with $p_T > 15 \text{ GeV}$, $|\eta| \leq 2.0$
 - MET significance cut + NN discrimination
 - 1—3 b-tags in the event
- Background model:
 - Pre-tag sample times b-tagging rate
 - Evaluate probability to tag background jet from the sample with 5 jets
 - Use correction factors for multiple b-quarks per events from background dominated samples (inverse NN cut)
- All possible combination are taken into account
- m^{rec} and m_W^{rec} are reconstructed by the χ^2 minimization and fitted simultaneously



CDF alljet measurement, 9.3 fb^{-1}

Source	$\sigma_{M_{\text{top}}}$ (GeV/c^2)	$\sigma_{\Delta_{\text{JES}}}$
Generator (hadronization)	0.29	0.273
Parton distribution functions	+0.18 -0.36	+0.096 -0.052
Initial / Final state radiation	0.13	0.232
Color reconnection	0.32	0.101
Δ_{JES} fit	0.97	--
M_{top} fit	--	0.207
Other free parameters of the fit	0.41	0.040
Templates sample size	0.34	0.071
$t\bar{t}$ cross section	0.15	0.034
Integrated luminosity	0.15	0.032
Trigger	0.61	0.188
Background shape	0.15	0.014
b -tagging	0.04	0.018
b -jets energy scale	0.20	0.035
Pileup	0.22	0
Residual JES	0.57	--
Residual bias / Calibration	+0.27 -0.24	+0.077 -0.096
Total	+1.55 -1.58	+0.492 -0.488

→ Herwig – Pythia



$$m_{\text{top}} = 175.07 \pm 1.19 \text{ (stat)} \begin{array}{l} +1.55 \\ -1.58 \end{array} \text{ (syst) GeV}$$

Precision: 1.1%

CDF dilepton measurement, 9.1 fb^{-1}

CDF Public note: 11072

- Selection:
 - 2 x electron or muon with $p_T > 20 \text{ GeV}$
 - 2 or more jets with $p_T > 15 \text{ GeV}$, $|\eta| \leq 2.5$
 - $\text{MET} > 25 \text{ GeV}$, $H_T > 200 \text{ GeV}$
 - Z veto in ee and mumu + topological cuts
- Template based analysis with “hybrid” variable:

$$M_t^{eff} = w \cdot M_t^{reco} + (1 - w) \cdot M_t^{alt}$$

- w is a free parameter (weight) in the range 0 – 1 \Rightarrow choose $w = 0.7$
- M^{reco} is a top quark mass reconstructed with the “neutrino weighting”
- Alternative variable

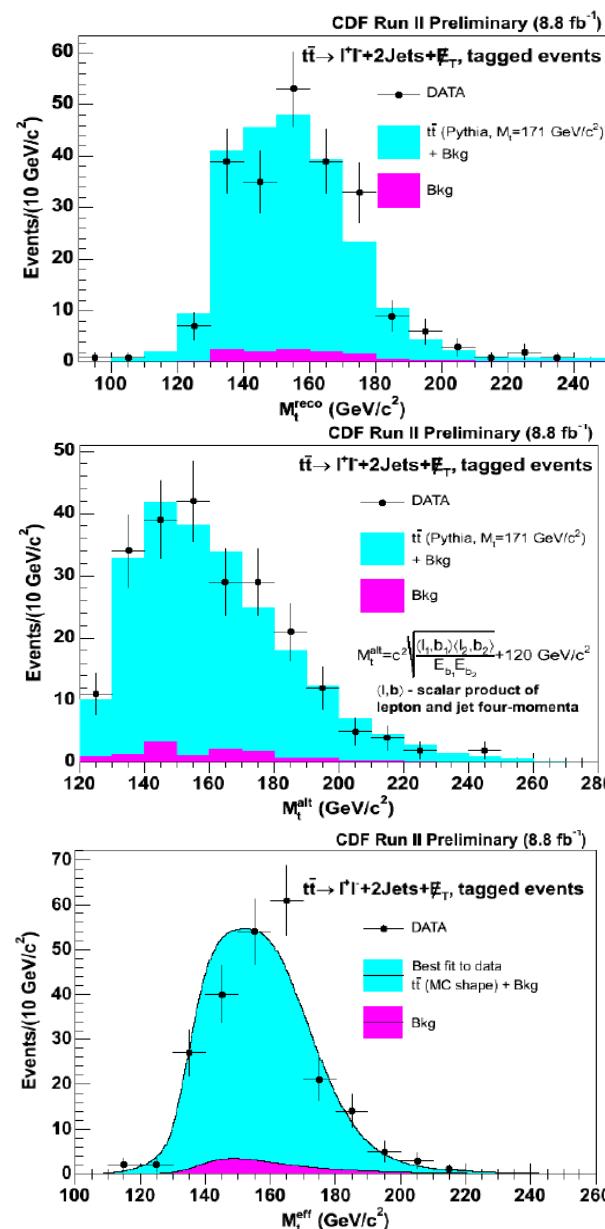
$$M_t^{alt} \equiv \sqrt{\langle l_1, c_{b_1} \rangle \cdot \langle l_2, c_{b_2} \rangle} + 120 \text{ GeV}$$

Lepton 4-momenta, jet directions

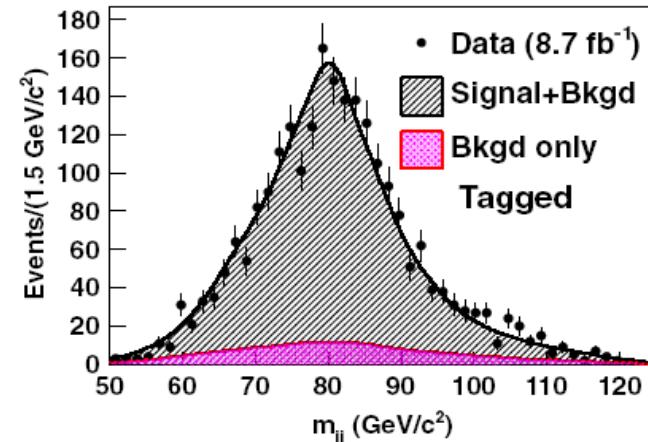
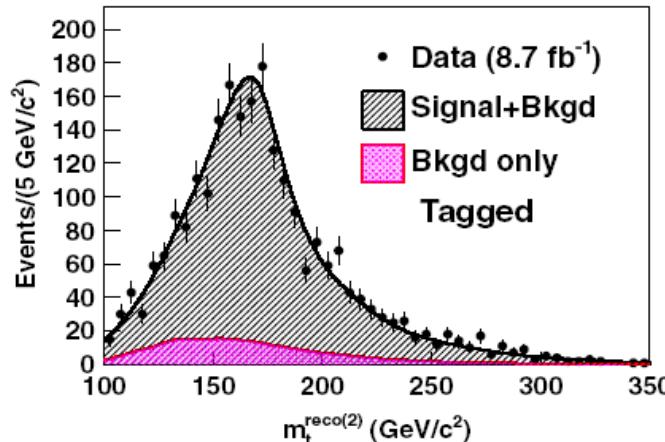
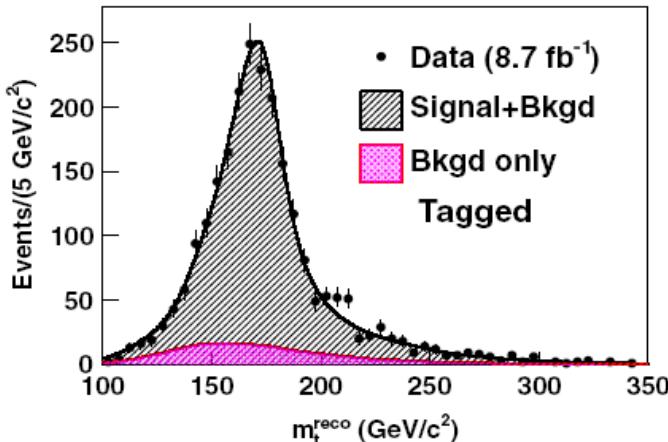
JES dominated

$$m_{top} = 170.80 \pm 1.83(\text{stat.}) \pm 2.69(\text{syst.}) \text{ GeV}$$

Precision: 1.9%



D0, 5.3 fb^{-1} , PRD(R) 86, 051103 (2012)
 $173.9 \pm 1.9 \text{ (stat)} \pm 1.6 \text{ (syst)} \text{ GeV}$



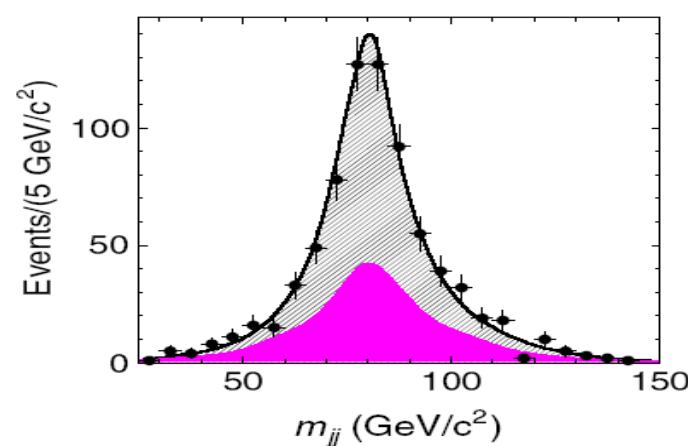
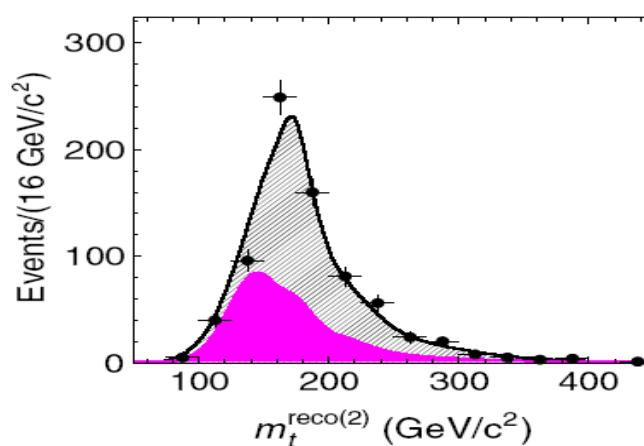
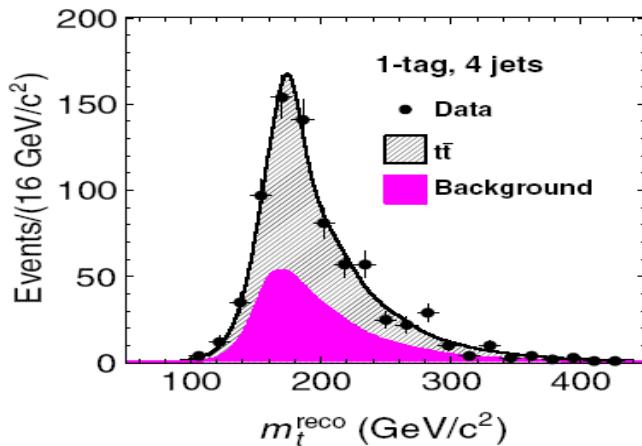
- $t\bar{t}$ simulation: Pythia
- Selection: electron or muon with $p_T > 20 \text{ GeV}$, $|\eta| < 1.1$, 4 and more jets $p_T > 20 \text{ GeV}$, $|\eta| < 2.0$, MET $> 20 \text{ GeV}$
- Separate in n b-tag samples
- Use kernel density estimation method for three variables: m^{reco} for the best and next-to-best assignment + m_{jj} – inv. mass for the W jets.

$$m_{\text{top}} = 172.85 \pm 0.71 \text{ (stat+JES)} \pm 0.84 \text{ (syst) GeV}$$

Precision: 0.6%

Source

Residual jet energy scale	0.52
Signal modeling	0.56
Higher-order corrections	0.09
b jet energy scale	0.18
b -tagging efficiency	0.03
Initial and final state radiation	0.06
Parton distribution functions	0.08
Gluon fusion fraction	0.03
Lepton energy scale	0.03
Background shape	0.20
Multiple hadron interaction	0.07
Color reconnection	0.21
MC statistics	0.05



- $t\bar{t}$ simulation: Pythia
- Selection $\sim l+jets$:
 - NO identified leptons, MET significance $> 3 \text{ GeV}^{1/2}$
 - 4 – 6 jets with $p_T > 15 \text{ GeV}$, $|\eta| < 2.0$
 - topological cuts + NN discriminant cut
 - Use b-tagging to classify events
- Reconstruction procedure is similar to the $l+jets$

Source	Uncertainty (GeV/c^2)
Residual jet-energy scale	0.44
MC generator	0.36
Color reconnection	0.28
gg fraction	0.27
Radiation	0.28
PDFs	0.16
b -jet energy scale	0.19
Background	0.15
Calibration	0.21
Multiple hadron interaction	0.18
Trigger modeling	0.13

$$M_{top} = 173.93 \pm 1.64 \text{ (stat+JES)} \pm 0.87 \text{ (syst) GeV}$$

Precision: 1.1%

D0 ℓ +jet measurements, 9.7 fb^{-1}

- Full D0 data set.
- Selections
 - Exactly one electron or muon with $p_T > 20$ GeV, $|\eta_e| < 1.1$, $|\eta_\mu| < 2.0$
 - Exactly four jets $p_T^{\text{leading}} > 40$ GeV, $p_T > 20$ GeV
 - One or more b-tagged jets (efficiency $\sim 65\%$, mistag rate $\sim 5\%$)
 - MET < 20 GeV + topological cuts

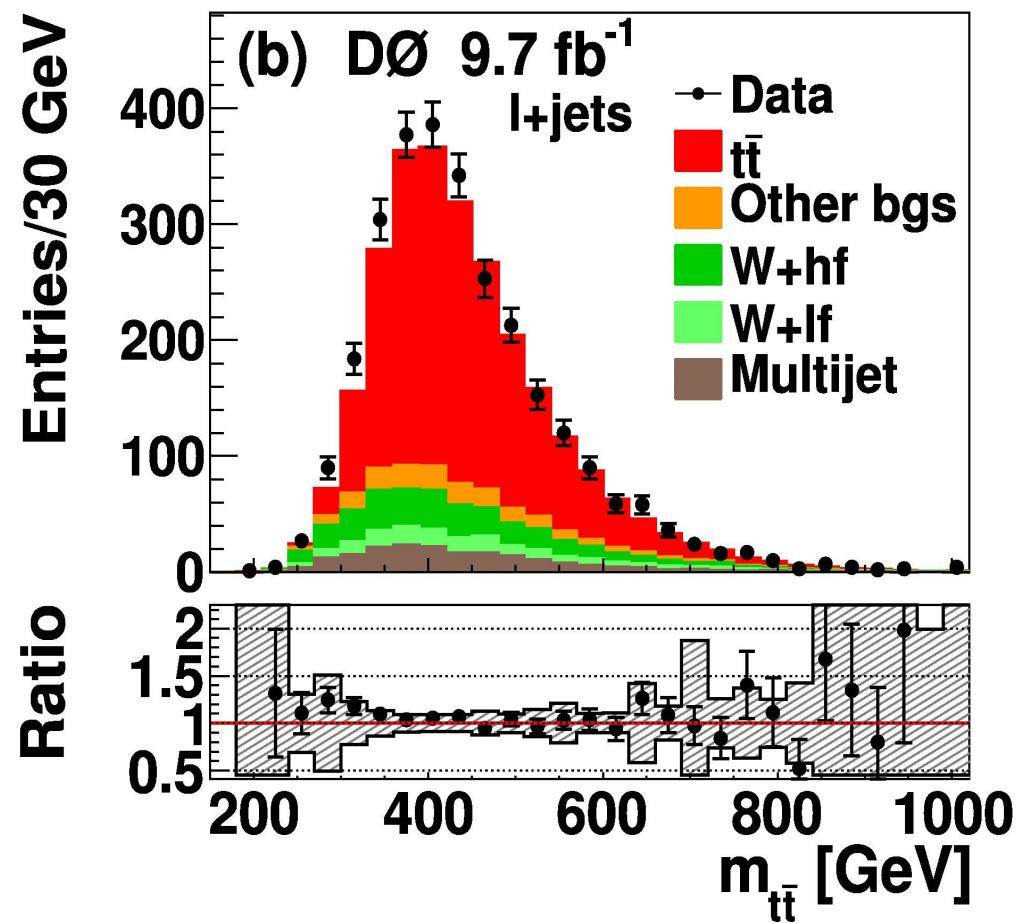
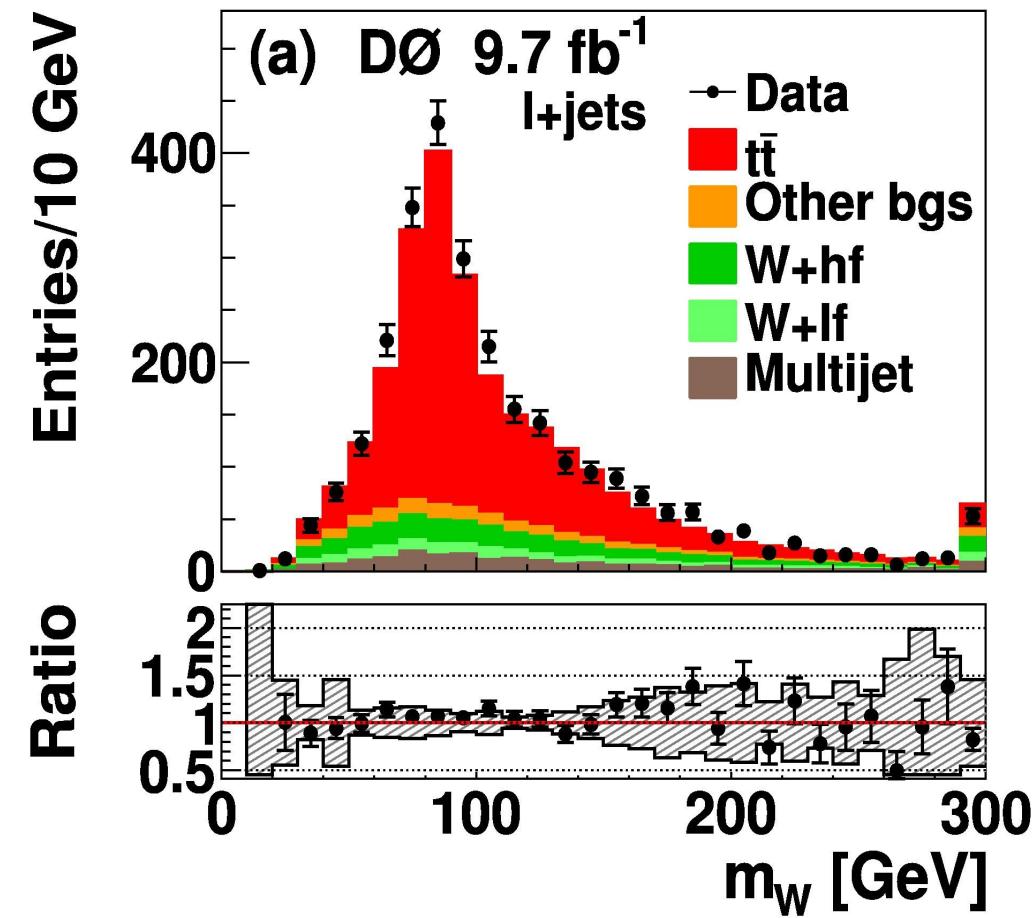
• Simulation

- $t\bar{t}$: Alpgen + Pythia (D0 modified tune A), CTEQ 6L1 PDFs
- W+jets : Alpgen+Pythia
- W+cc, W+bb: Alpgen+Pythia
- Multijets events : from data

Contribution	e +jets		μ +jets			
$t\bar{t}$	918.11	\pm	3.63	824.88	\pm	3.48
W +jets	77.85	\pm	2.13	101.03	\pm	2.93
W +HF	125.98	\pm	2.12	162.21	\pm	2.81
Multijet	144.41	\pm	24.19	48.17	\pm	16.11
Other backgrounds	97.75	\pm	0.51	79.24	\pm	0.94
Expected	1364.10	\pm	24.65	1215.53	\pm	17.00
Observed	1502		1286			

Expected signal fraction $\sim 68\%$

$\mathcal{D}\mathcal{O}$ $l+jet$ measurements, 9.7 fb^{-1}



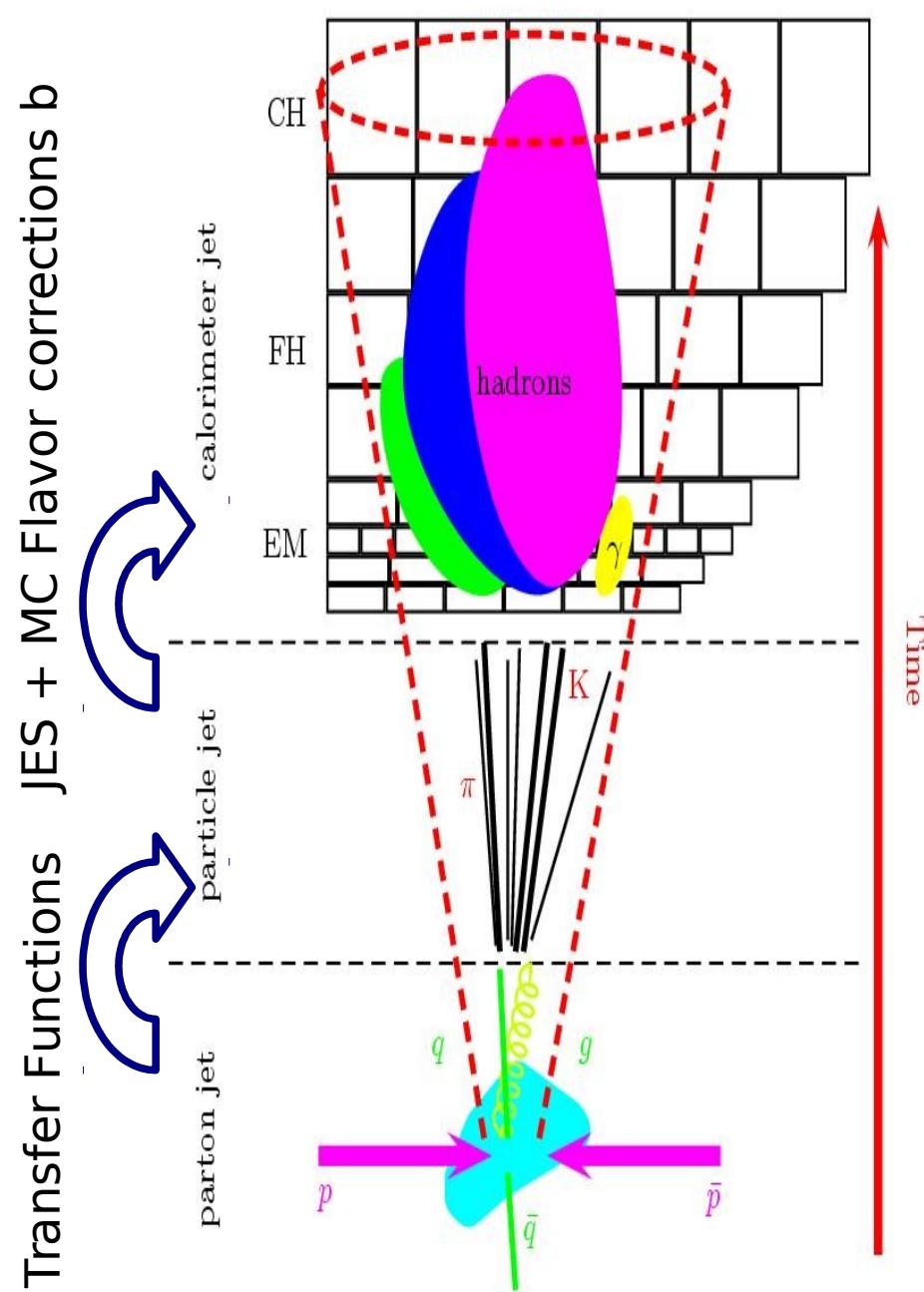
JES at D0

- Jet Energy Scale: correct reconstructed jet energy to the particle level
 - Absolute JES
 - Separately measured for data and MC

$$E_{jet} = \frac{E_{meas} - E_{offset}}{R_{response} \cdot S_{showring}}$$

- Flavor dependent correction : different response correction for gluon, light quark, b-quarks (b-JES)
 - Tune the single particle response difference between data and MC in $\gamma + \text{jets}$ and dijets events

$$F_{corr} = \frac{1}{\langle F \rangle_{\gamma+jet}} \frac{\sum_i E_i R_i^{data}}{\sum_i E_i R_i^{MC}}$$



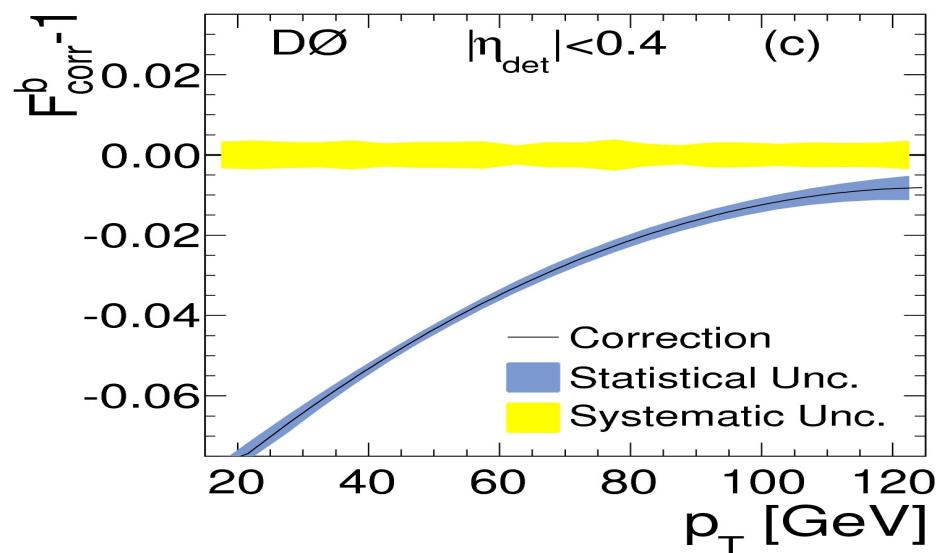
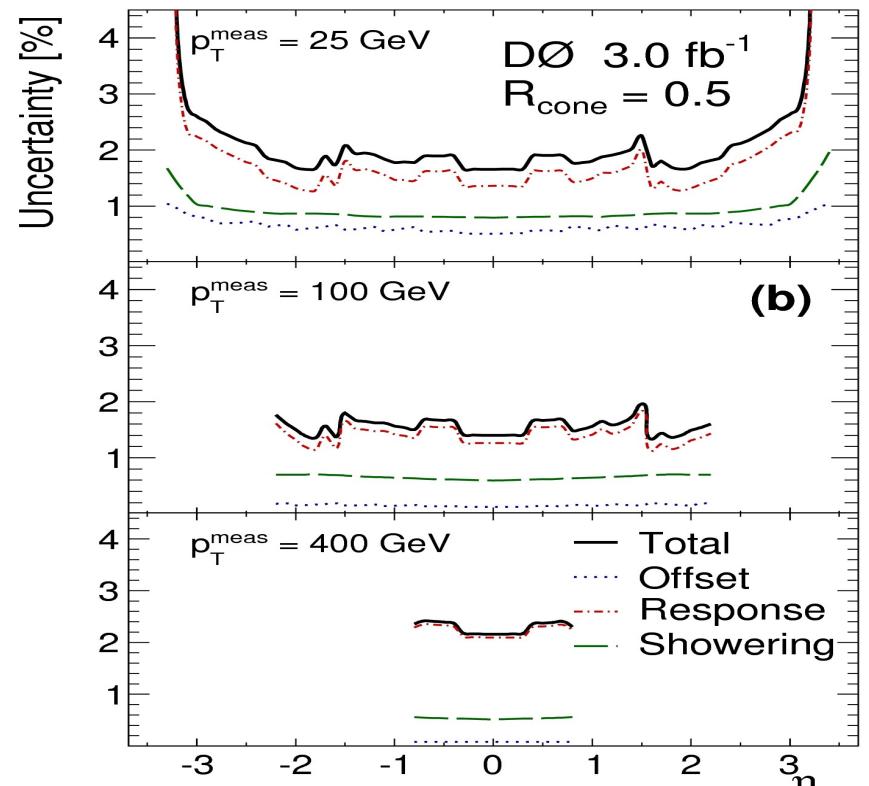
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Matrix Element Technique

$$P(x, H) \sim \int d^6\sigma(y, H) W(x, y) f_{PDF}(q_1) f_{PDF}(q_2) dq_1 dq_2$$

Diff. xsection Detector response
with LO ME (Transfer Function) PDFs

- Sum over 24 possible jet-parton assignments with b-tag dependent weights
- Integrate over 10 variables using MC integration
- Use W-boson mass as an additional constrains for the JES correction factor
- Multiply probabilities for all events \rightarrow likelihood as a function of top quark mass and JES correction. $P_{\text{evt}}(m_{\text{top}}) \propto f P_{\text{sig}}(m_{\text{top}}) + (1 - f) P_{\text{bgr}}$
- Improvement since previous publication (*PRD 84, 032004, 2011*):

Accelerate
integration by a
factor of ~ 100

- {
- low-discrepancy sequences for the MC integration
 - Factorise the JES correction factor from the ME calculation



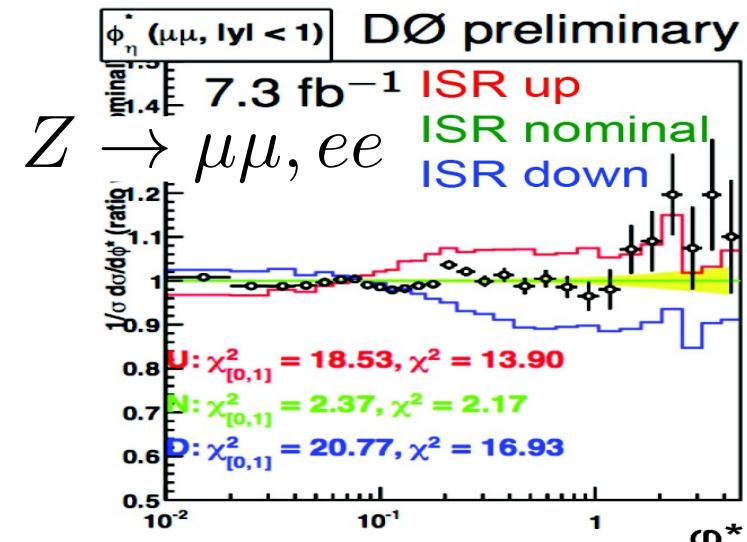
Integrate many more MC events \Rightarrow reduce statistical component
in the systematic uncertainties estimation from ~ 0.25 GeV to **0.05 GeV**

Systematic Uncertainties Estimation

Source of uncertainty	Effect on m_t (GeV)
<i>Signal and background modeling:</i>	
Higher order corrections	+0.15
Initial/final state radiation	±0.09
Hadronization and underlying event	+0.26
Color reconnection	+0.10
Multiple $p\bar{p}$ interactions	-0.06
Heavy flavor scale factor	±0.06
b quark jet modeling	+0.09
Parton distribution functions	±0.11
<i>Detector modeling:</i>	
Residual jet energy scale	±0.21
Flavor-dependent response to jets	±0.16
b tagging	±0.10
Trigger	±0.01
Lepton momentum scale	±0.01
Jet energy resolution	±0.07
Jet identification efficiency	-0.01
<i>Method:</i>	
Modeling of multijet events	+0.04
Signal fraction	±0.08
MC calibration	±0.07
<i>Total systematic uncertainty</i>	±0.49
<i>Total statistical uncertainty</i>	±0.58
<i>Total uncertainty</i>	±0.76

MC@NLO + Herwig – Alpgen + Herwig

Vary renormalisation scale in Alpgen by 1.5

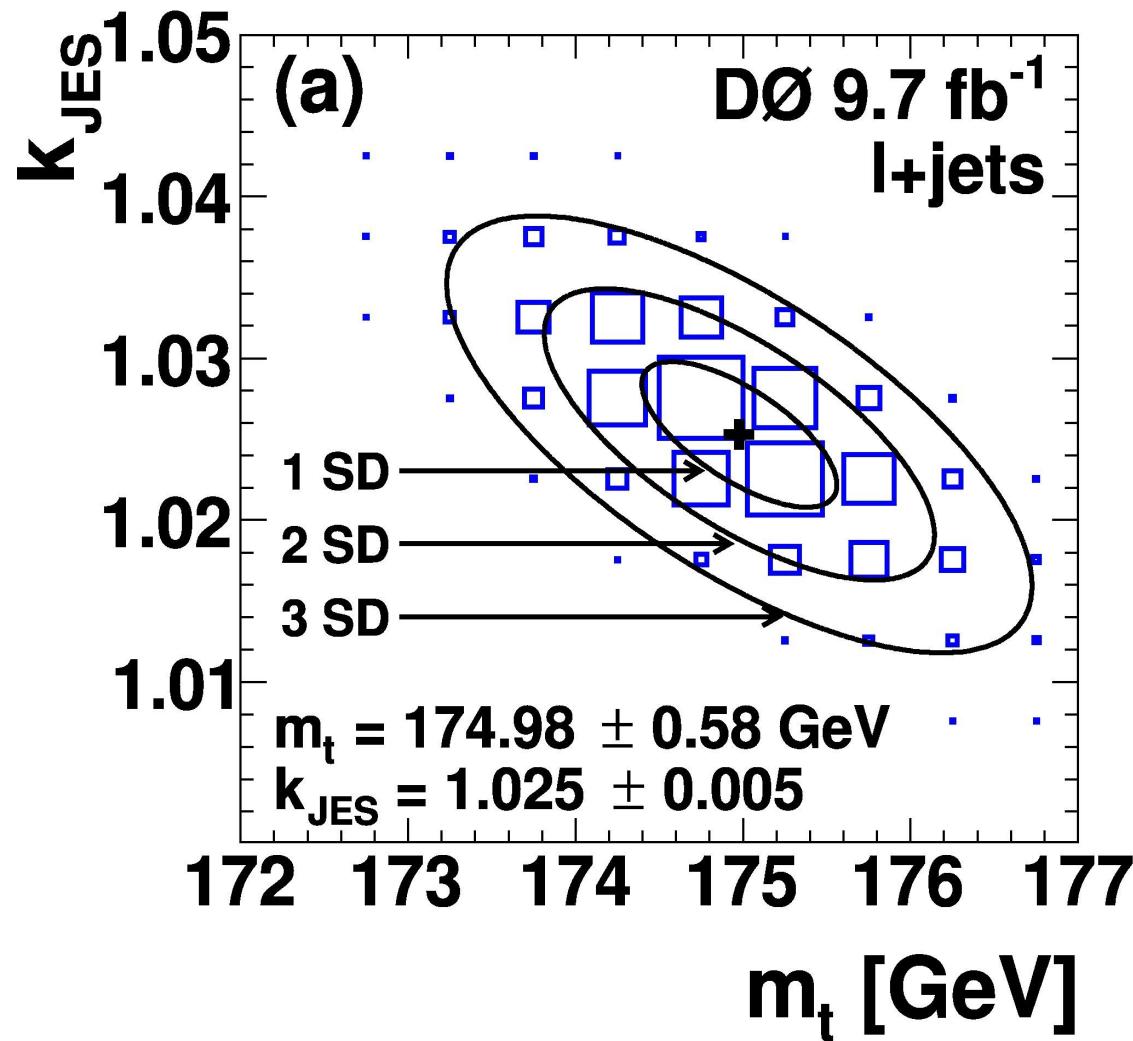


Alpgen + Herwig – Alpgen + Pythia
for particle-level jets

Pythia, Perugia 2011 – Perugia 2001NOCR

Phys. Rev. Lett. 113, 032002 (2014)
PRD with more details is in preparation

Results

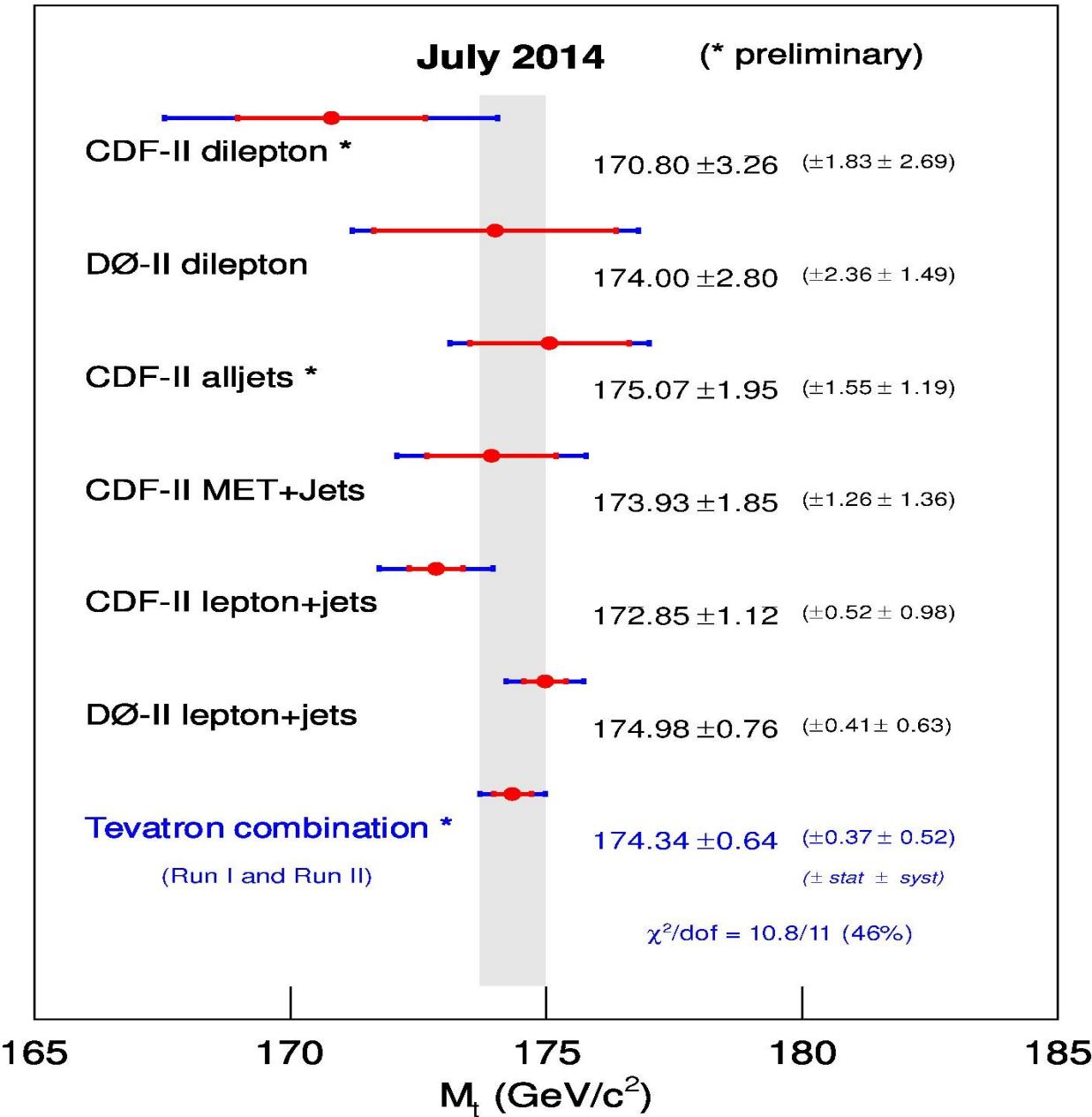


$$m_{\text{top}} = 174.98 \pm 0.41(\text{stat}) \pm 0.41(\text{JES}) \pm 0.49(\text{syst}) \text{ GeV}$$

Precision: 0.44%

Summary of the results

Mass of the Top Quark

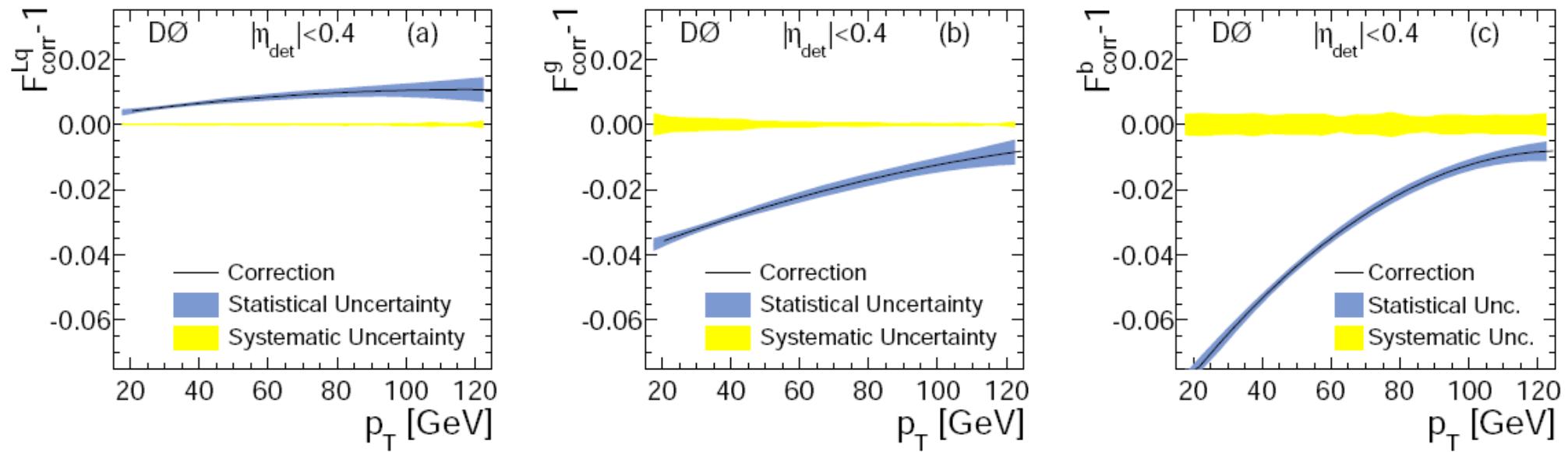


Conclusion

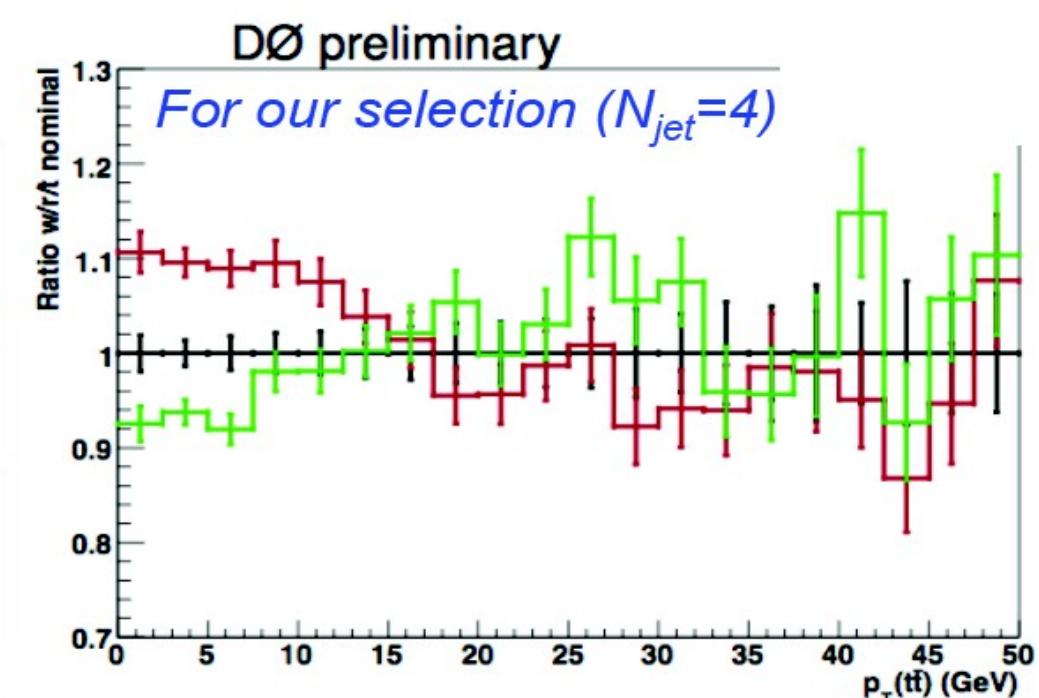
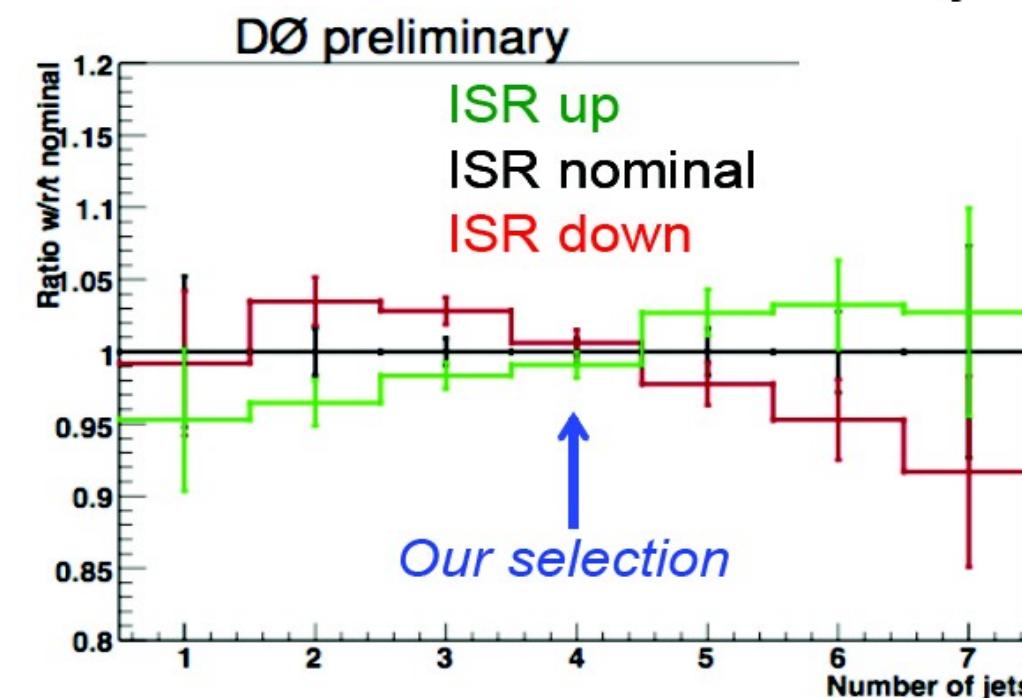
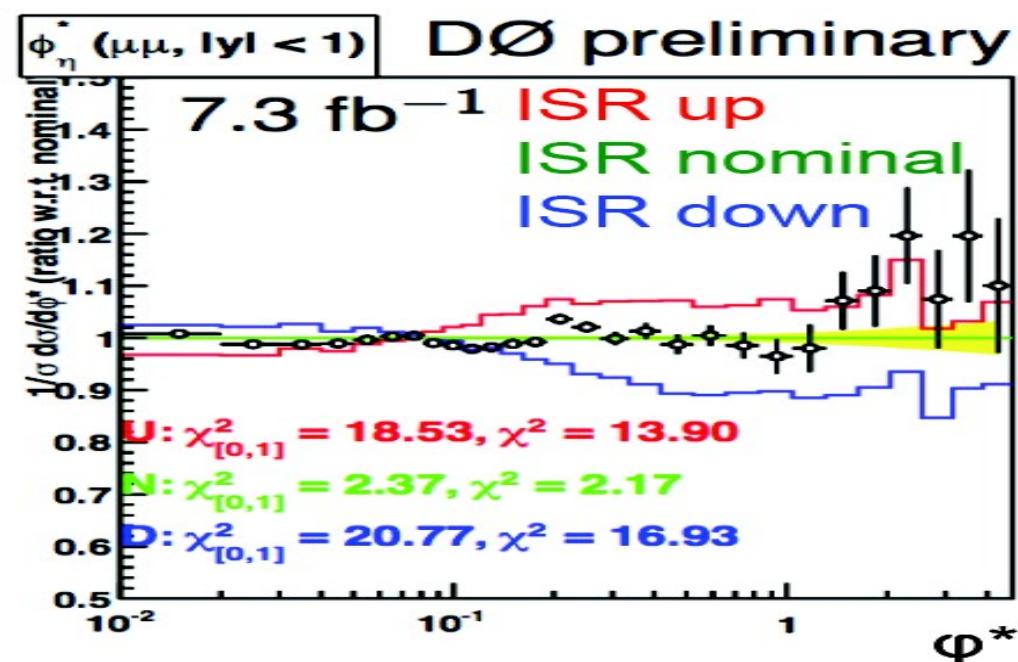
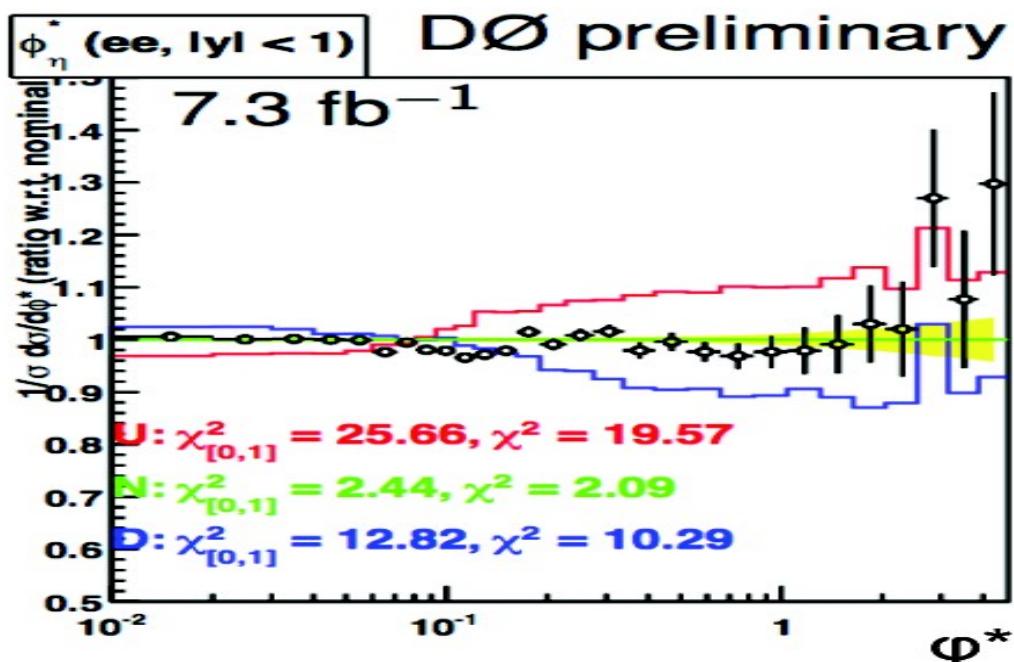
- The most precise channels from the Tevatron with all statistics are done.
- Several more results are coming in dilepton and alljets channels

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Matrix Element	D0, 9.7 fb^{-1}	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}		
From cross-section	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}	D0, 5.4 fb^{-1} Soon: D0, 9.7 fb^{-1}		
Lepton pT	CDF 2.7 fb^{-1}	CDF 2.8 fb^{-1}		

Additional Materials



$D\bar{O}$ ISR/FSR variation



$\mathcal{D}0$ measurement: systematic uncertainties comparison

Source	Uncertainty (GeV)	Source of uncertainty	Effect on m_t (GeV)
<i>Modeling of production:</i>		<i>Signal and background modeling:</i>	9.7 fb^{-1}
<i>Modeling of signal:</i>	3.6 fb^{-1}	Higher order corrections	+0.15
Higher-order effects	±0.25	Initial/final state radiation	±0.09
ISR/FSR	±0.26	Hadronization and underlying event	+0.26
Hadronization and UE	±0.58	Color reconnection	+0.10
Color reconnection	±0.28	Multiple $p\bar{p}$ interactions	-0.06
Multiple $p\bar{p}$ interactions	±0.07	Heavy flavor scale factor	±0.06
Modeling of background	±0.16	b quark jet modeling	+0.09
$W+\text{jets}$ heavy-flavor scale factor	±0.07	Parton distribution functions	±0.11
Modeling of b jets	±0.09	<i>Detector modeling:</i>	
Choice of PDF	±0.24	Residual jet energy scale	±0.21
<i>Modeling of detector:</i>		Flavor-dependent response to jets	±0.16
Residual jet energy scale	±0.21	b tagging	±0.10
Data-MC jet response difference	±0.28	Trigger	±0.01
b -tagging efficiency	±0.08	Lepton momentum scale	±0.01
Trigger efficiency	±0.01	Jet energy resolution	±0.07
Lepton momentum scale	±0.17	Jet identification efficiency	-0.01
Jet energy resolution	±0.32	<i>Method:</i>	
Jet ID efficiency	±0.26	Modeling of multijet events	+0.04
<i>Method:</i>		Signal fraction	±0.08
Multijet contamination	±0.14	MC calibration	±0.07
Signal fraction	±0.10	<i>Total systematic uncertainty</i>	±0.49
MC calibration	±0.20	<i>Total statistical uncertainty</i>	±0.58
Total	±1.02	<i>Total uncertainty</i>	±0.76