

# The $\bar{B} \rightarrow \bar{K} \pi \ell \ell$ distribution at low hadronic recoil.

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*based on*

arXiv: 1406.\*\*\*\*

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- The  $\bar{B} \rightarrow \bar{K}\pi ll$  is  $|\Delta_B| = |\Delta_S| = 1$  Flavour Changing Neutral Current (FCNC) processes and therefore sensitive to New Physics(NP).
- At LHCb with  $3fb^{-1}$  luminosity, significant numbers( $\sim 3K$ ) of  $\bar{B} \rightarrow \bar{K}\pi ll$  events will be produced.
- As far as high precision measurements are concerned,  $\bar{B} \rightarrow \bar{K}\pi ll$  is a significant background to  $\bar{B} \rightarrow \bar{K}^*(\rightarrow \bar{K}\pi)ll$ .

Effective Hamiltonian for  $|\Delta_B| = |\Delta_S| = 1$  decays is

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha_e}{4\pi} \sum_i C_i(\mu) \mathcal{O}_i(\mu).$$

$$\mathcal{O}_7^{(\prime)} = \frac{m_b}{e} \bar{s} \sigma^{\mu\nu} P_R(P_L) b F_{\mu\nu}, \quad \mathcal{O}_9^{(\prime)} = \bar{s} \gamma_\mu P_L(P_R) b \bar{\ell} \gamma^\mu \ell, \quad \mathcal{O}_{10}^{(\prime)} = \bar{s} \gamma_\mu P_L(P_R) b \bar{\ell} \gamma^\mu \gamma_5 \ell,$$

The  $\bar{B}(p_B) \rightarrow \bar{K}(p_K) \pi(p_\pi)$  hadronic matrix element can be parameterized as

$$\langle \bar{K} \pi | \bar{s} \gamma_\mu (1 - \gamma_5) b | \bar{B} \rangle = i \left[ w_+ p_\mu + w_- P_\mu + r q_\mu + i h \epsilon_{\mu\alpha\beta\gamma} p_B^\alpha p^\beta P^\gamma \right],$$

$$\langle \bar{K} \pi | \bar{s} i q^\nu \sigma_{\mu\nu} (1 + \gamma_5) b | \bar{B} \rangle = -i m_B \left[ w'_+ p_\mu + w'_- P_\mu + r' q_\mu + i h' \epsilon_{\mu\alpha\beta\gamma} p_B^\alpha p^\beta P^\gamma \right],$$

where  $q = p_{\ell^-} + p_{\ell^+}$ ,  $p = p_K + p_\pi$ .

[Buchalla and Isidori, Nucl. Phys. B525, 333]

[Lee, Lu and Wise, Phys. Rev. D46, 5040]

The form factors  $w_\pm^{(\prime)}$ ,  $h_\pm^{(\prime)}$  and  $r_\pm^{(\prime)}$  are functions of  $p^2$ ,  $q^2$  and  $\cos \theta_K$ .

$r^{(\prime)}$  does not contribute in vanishing lepton mass limit employed here.

$\theta_K$ : angle between the  $K$  and the  $B$  in the  $K\pi$  rest frame.

Improved Isgur-Wise relations at lowest order in  $1/m_b$  including  $\mathcal{O}(\alpha_s)$  corrections, using QCD equation of motion

$$i\partial^\nu (\bar{s}i\sigma_{\mu\nu}(1 + \gamma_5)b) = -m_b \bar{s}\gamma_\mu(1 - \gamma_5)b + i\partial_\mu(\bar{s}(1 + \gamma_5)b) - 2\bar{s}i\overleftarrow{D}_\mu(1 + \gamma_5)b$$

[Grinstein and Pirjol, Phys. Rev. D 70, 114005 (2004)]

$$w'_\pm = w_\pm \kappa, \quad h' = h\kappa.$$

The lowest order heavy hadron chiral perturbation theory (HH $\chi$ PT) expressions for  $w_\pm(q^2, p^2, \cos\theta_K)$  and  $h(q^2, p^2, \cos\theta_K)$  are

[Lee, Lu and Wise, Phys. Rev. D46, 5040]

$$w_\pm = \pm \frac{gf_B}{2f_\pi^2} \frac{m_B}{v \cdot p_\pi + \Delta},$$

$$h = \frac{g^2 f_B}{2f_\pi^2} \frac{1}{[v \cdot p_\pi + \Delta][v \cdot p + \Delta + \mu_s]},$$

where  $v = p_B/m_B$ ,  $\Delta = m_{B^*} - m_B$  MeV and  $\mu_s = m_{B_s} - m_B$  MeV.

$$g = 0.569 \pm 0.076, \quad [\text{Lattice result on } B^* B \pi \text{ from Flynn } et al., \text{ arXiv:1311.2251}]$$

$$g = 0.59 \pm 0.070 \quad [D^* D \pi \text{ coupling from CLEO Collaboration, PhysRevLett.87.251801}]$$

# Transversity Amplitudes

- The transversity amplitudes at low hadronic recoil with OPE in  $1/m_b$  [Hiller and Zwicky, JHEP 1403 (2014) 042]

$$H_{0,\parallel}^{L/R} = C_-^{L/R}(q^2) F_{0,\parallel}(q^2, p^2, \cos \theta_K), \quad H_{\perp}^{L/R} = C_+^{L/R}(q^2) F_{\perp}(q^2, p^2, \cos \theta_K),$$
$$C_{\pm}^{L/R}(q^2) = C_9^{\text{eff}}(q^2) \pm C_9' \mp (C_{10} \pm C_{10}') + \kappa \frac{2m_b m_B}{q^2} (C_7^{\text{eff}} \pm C_7').$$

- The transversity form factors for  $\bar{B} \rightarrow \bar{K} \pi \ell \ell$  decay are [DD, Hiller, Jung, Shires, arXiv: 1406.\*\*\*\*, DO-TH 14/10] [Lee, Lu and Wise, Phys. Rev. D46, 5040]

$$F_0 = \frac{\mathcal{N}_{nr}}{2} \left[ \lambda^{1/2} w_+ + \frac{1}{p^2} \{ (m_K^2 - m_\pi^2) \lambda^{1/2} - (m_B^2 - q^2 - p^2) \lambda_p^{1/2} \cos \theta_K \} w_- \right],$$

$$F_{\parallel} = \mathcal{N}_{nr} \sqrt{\lambda_p \frac{q^2}{p^2}} w_-, \quad F_{\perp} = \frac{\mathcal{N}_{nr}}{2} \sqrt{\lambda \lambda_p \frac{q^2}{p^2}} h.$$

- Generalized transversity form factors to include resonance (spin  $J_R$ ) contributions.

$$\mathcal{F}_0(q^2, p^2, \cos \theta_K) = F_0(q^2, p^2, \cos \theta_K) + \sum_R P_{J_R}^0(\cos \theta_K) \cdot F_{0J_R}(q^2, p^2),$$

$$\mathcal{F}_i(q^2, p^2, \cos \theta_K) = F_i(q^2, p^2, \cos \theta_K) + \sum_R \frac{P_{J_R}^1(\cos \theta_K)}{\sin \theta_K} \cdot F_{iJ_R}(q^2, p^2), \quad i = \parallel, \perp.$$

[DD, Hiller, Jung, Shires, arXiv: 1406.\*\*\*\*, DO-TH 14/10]

# Kinematics and Angular Distributions: Low recoil

The  $\bar{B} \rightarrow \bar{K}\pi\ell\ell$  angular distribution in terms of angles  $\theta_l, \theta_K, \phi$  [Bobeth, Hiller and Piranishvili, JHEP 0807, 106]

$$d^5\Gamma = \frac{1}{2\pi} \left[ \sum_{i=1}^9 c_i(\theta_l, \phi) I_i(q^2, p^2, \cos\theta_K) \right] dq^2 dp^2 d\cos\theta_K d\cos\theta_l d\phi.$$

Angular coefficients can be written in terms of short distance physics  $\rho_1^\pm, \rho_2^\pm, \delta\rho$  and long distance physics  $\mathcal{F}_{0,\parallel,\perp}$ .

$$\rho_1^\pm = \frac{1}{2}(|C_\pm^R|^2 + |C_\pm^L|^2), \quad \delta\rho = \frac{1}{4}(|C_-^R|^2 - |C_-^L|^2), \quad \rho_2^\pm = \frac{1}{4}(C_+^R C_-^{R*} \mp C_-^L C_+^{L*}).$$
$$\rho_1 \equiv \rho_1^\pm = 2\text{Re}\rho_2^-, \quad \rho_2 \equiv \text{Re}\rho_2^+ = \delta\rho, \quad \text{Im}\rho_2^\pm = 0, \quad \text{in SM basis}$$

The coefficients  $\rho_1^\pm$  and  $\rho_2^\pm$  also appear in  $\bar{B} \rightarrow \bar{K}^*\ell\ell$  decay [Bobeth, Hiller and Dyk, JHEP 1007, 098, Phys.Rev. D87 (2013) 034016].

The coefficients  $\delta\rho$  and  $\rho_2^-$  are new.

The strong phase differences between the generalized form factors  $\mathcal{F}_i$  allows us to measure these short distance coefficients.

$$I_7 = \delta\rho \text{Im}(\mathcal{F}_0 \mathcal{F}_\parallel^*) \sin\theta_K,$$

$$\begin{aligned} \frac{d^5\Gamma(S+P+D)}{dq^2 dp^2 d\cos\theta_K d\cos\theta_\ell d\phi} = & \frac{1}{2\pi} \left[ \sum_{i=1,2} c_i (J_{icc} \cos^2\theta_K + J_{iss} \sin^2\theta_K + J_{ic} \cos\theta_K \right. \\ & + J_{issc} \sin^2\theta_K \cos\theta_K + J_{isscc} \sin^2\theta_K \cos^2\theta_K) \\ & + \sum_{i=3,6,9} c_i (J_{icc} \cos^2\theta_K + J_i + J_{ic} \cos\theta_K) \sin^2\theta_K \\ & \left. + \sum_{i=4,5,7,8} c_i (J_{icc} \cos^2\theta_K + J_{iss} \sin^2\theta_K + J_{ic} \cos\theta_K + J_{issc} \sin^2\theta_K \cos\theta_K) \sin\theta_K \right] \end{aligned}$$

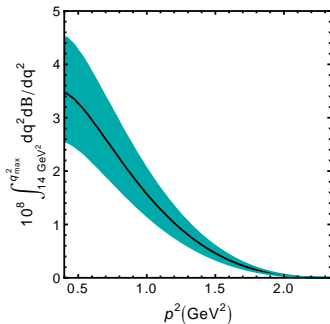
[DD, Hiller, Jung, Shires, arXiv: 1406.\*\*\*\*, DO-TH 14/10]

For pure P-wave, only the coefficients  $J_{1ss}, J_{2ss}, J_{3,6,9}$  and  $J_{4c}, J_{5c}, J_{7c}, J_{8c}$  appear .

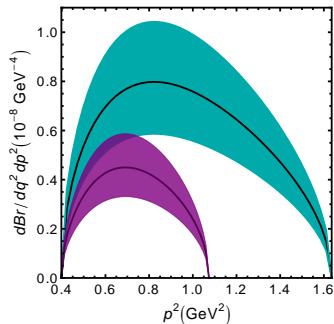
There is no S-wave contribution to  $I_{3,6,9}$ . [Becirevic, et.al 2013, Blake et.al 2013, Matias et.al 2012, Bobeth et.al 2013]

The D-wave contributes to  $I_{3,6,9}$  and can be separated from the pure P-one by angular analysis.

# Phenomenology $\bar{B} \rightarrow \bar{K} \pi \ell \ell$ : $p^2$ distributions



**Figure:** Differential branching fraction in SM, integrated over low recoil region [ $14 \text{ GeV}^2$ - $q_{\text{max}}^2$ ] as a function of lower  $p^2$ -integration boundary.  $q_{\text{max}}^2 = (m_B - \sqrt{p^2})^2$  for given  $p^2$ .



**Figure:**  $d\mathcal{B}(\bar{B} \rightarrow \bar{K} \pi \ell \ell)/dq^2 dp^2$  in SM for fixed  $q^2 = 16 \text{ GeV}^2$  (outer curve) and  $q^2 = 18 \text{ GeV}^2$  (inner curve).

[DD, Hiller, Jung, Shires, arXiv: 1406.\*\*\*\*, DO-TH 14/10]



# Phenomenology of $\bar{B} \rightarrow \bar{K} \pi \ell \ell$ : $p^2$ cuts

- full non-resonant phase space:  $p_{min}^2 \equiv (m_K + m_\pi)^2 \leq p^2 < (m_B - \sqrt{q^2})^2$
- P-wave 'signal' window:  $0.64 \text{ GeV}^2 \leq p^2 < 1 \text{ GeV}^2$
- S+P-wave 'total' window:  $p_{min}^2 \leq p^2 < 1.44 \text{ GeV}^2$

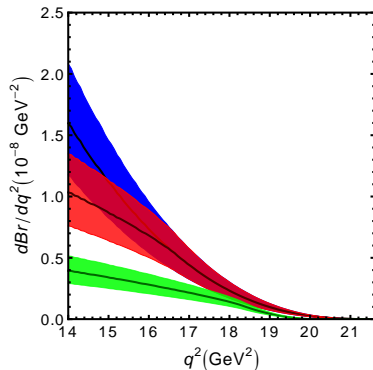


Figure:  $d\mathcal{B}(\bar{B} \rightarrow \bar{K} \pi \ell \ell)/dq^2$  in SM without any  $p^2$  cut (blue), in the S+P wave window (red) and in the P wave signal window (green).

$\bar{B} \rightarrow \bar{K} \pi \ell \ell$  as background to  $\bar{B} \rightarrow \bar{K}^* \ell \ell$

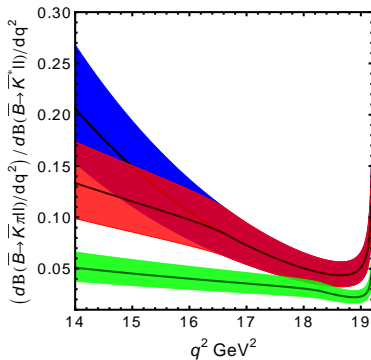


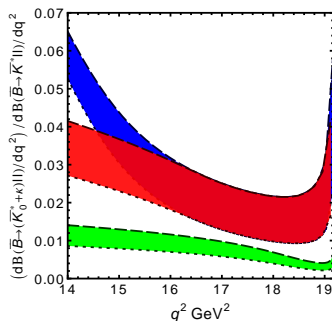
Figure:  $[dB(\bar{B} \rightarrow \bar{K} \pi \ell \ell)/dq^2]/[dB(\bar{B} \rightarrow \bar{K}^* \ell \ell)/dq^2]$  in SM without any  $p^2$  cut (blue), in S+P-wave total window (red) and P wave signal window (green).

[DD, Hiller, Jung, Shires, arXiv: 1406.\*\*\*\*, DO-TH 14/10]

# S-wave as background to $\bar{B} \rightarrow \bar{K}^* \ell \ell$

$$BW_S(p^2) = \mathcal{N}_S \left[ \frac{-g_\kappa}{(m_\kappa - i\Gamma_\kappa/2)^2 - p^2} + \frac{1}{(m_{K_0^*} - i\Gamma_{K_0^*}/2)^2 - p^2} \right]$$

$$|g_\kappa| = 0.2, \quad \text{Arg}(g_\kappa) = \pi/2, \quad [\text{Becirevic and Tayduganov, Nucl. Phys. B868, 368}]$$



**Figure:**  $[d\mathcal{B}(\bar{B} \rightarrow (\bar{K}_0^*(1430) + \kappa)\ell\ell)/dq^2]/[d\mathcal{B}(\bar{B} \rightarrow \bar{K}^*\ell\ell)/dq^2]$  in SM without  $p^2$  cut (blue), in S+P wave window (red) and in P-wave signal window (green). The bands are obtained by varying  $|g_\kappa| \in [0, 0.2]$  and  $\text{Arg}(g_\kappa) \in [\pi/2, \pi]$ . The maximum contribution is obtained for  $|g_\kappa| = 0.2$ ,  $\text{Arg}(g_\kappa) = \pi/2$  (dashed lines). For  $g_\kappa = 0$  the lower edge of the band (dotted lines) is obtained.

- Kinematic endpoint correspond to  $q^2 = q_{max}^2 = (m_B - \sqrt{p^2})^2$  at fixed  $p^2$
- Only  $F_0$  and  $F_{\parallel}$  survive and dominated by P-wave amplitudes

$$I_3 = -\frac{I_1 + I_2}{2}, \quad I_4 = -\sqrt{\frac{(I_1 + I_2)(I_1 - 3I_2)}{2}}, \quad I_{5,6,7,8,9} = 0$$

$$\frac{d^3\Gamma}{dp^2 dq^2 d\cos\theta_K} / \left( \frac{d^2\Gamma}{dp^2 dq^2} \right) |_{endpoint} = \frac{1}{2},$$

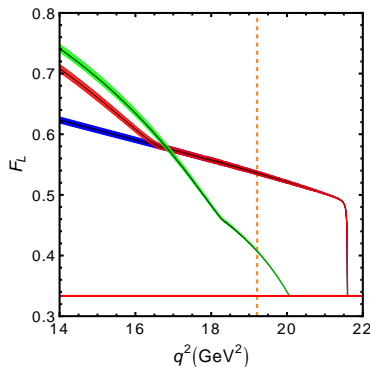
$$\frac{d^3\Gamma}{dp^2 dq^2 d\cos\theta_l} / \left( \frac{d^2\Gamma}{dp^2 dq^2} \right) |_{endpoint} = \frac{1}{2},$$

$$\frac{d^3\Gamma}{dp^2 dq^2 d\cos\phi} / \left( \frac{d^2\Gamma}{dp^2 dq^2} \right) |_{endpoint} = \frac{1}{2\pi} \left( 1 - \frac{1}{3} \cos 2\phi \right),$$

[DD, Hiller, Jung, Shires, arXiv: 1406.\*\*\*\*, DO-TH 14/10]

# Phenomenology of $\bar{B} \rightarrow \bar{K} \pi \ell \ell$ : $F_L$

$$F_L \Big|_{\text{endpoint}} = \frac{1}{3}, \text{ [Hiller and Zwicky, JHEP 1403 (2014) 042]}$$



**Figure:** Angular observable  $F_L$  in SM for  $\bar{B} \rightarrow \bar{K} \pi \ell \ell$  in the P-wave signal window (green), S+P window (red) and without any  $p^2$ -cut (blue). The vertical dashed line corresponds to  $K^*(892)$  endpoint and the horizontal line is  $1/3$ . Uncertainties cancel to a large extent in ratio.

[DD, Hiller, Jung, Shires, arXiv: 1406.\*\*\*\*, DO-TH 14/10]

- Non-resonant  $\bar{B} \rightarrow \bar{K}\pi\ell\ell$  is dominant background to  $\bar{B} \rightarrow \bar{K}^*\ell\ell$ .
- $\bar{B} \rightarrow \bar{K}\pi\ell\ell$  could be a viable rare signal.
- Phenomenological results for  $\bar{B} \rightarrow \bar{K}\pi\ell\ell$  decay at low hadronic recoil are presented.
- Improved Isgur-Wise relations between the vector and tensor current.
- Endpoint relations for  $\bar{B} \rightarrow \bar{K}\pi\ell\ell$  decay.

Ongoing analysis for  $\bar{B} \rightarrow \bar{K}K\ell\ell$  corresponding to  $B_s \rightarrow \phi(\rightarrow \bar{K}K)\ell\ell$ .

*thank you*