

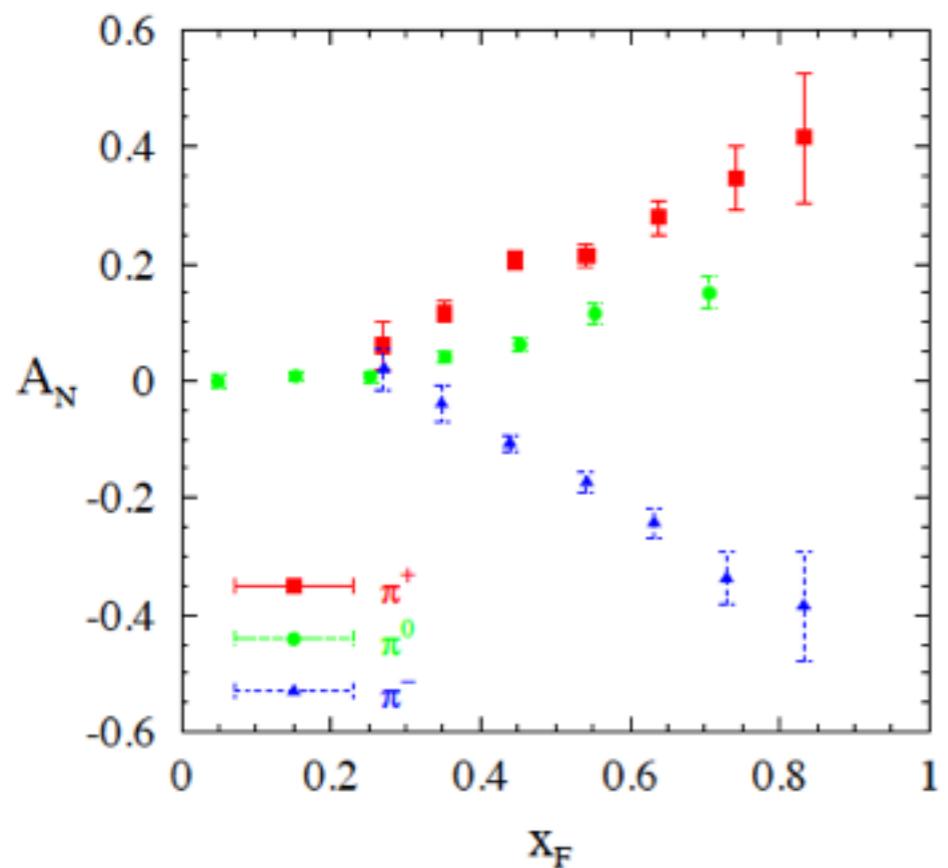
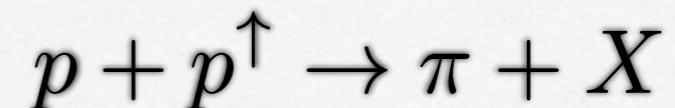
Transverse Spin Asymmetries in Deep- Inelastic Processes

Marc Schlegel
University of Tübingen

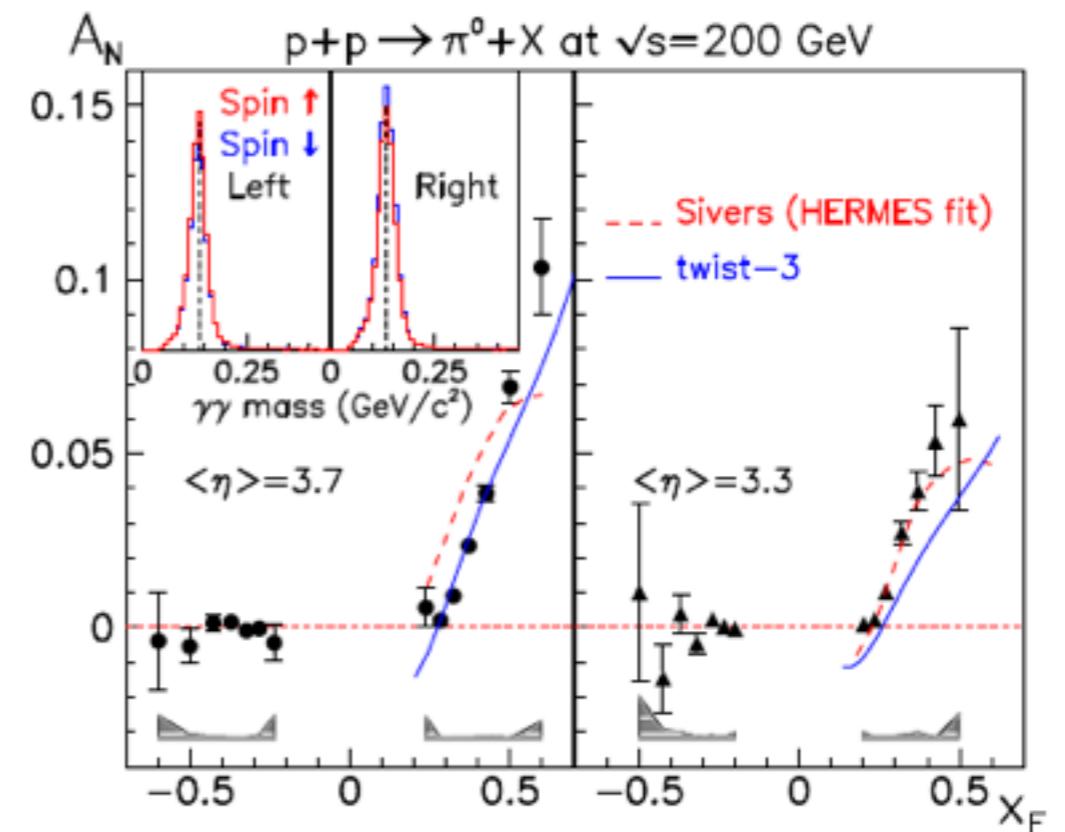
“Spin and Orbital Angular Momentum of Quarks and
Gluons in the Nucleon”, ECT*, Trento, Aug. 28, 2014

Why Transverse Spin Asymmetries?

“Show-off” Transverse SSA



$\sqrt{s} = 20$ GeV [E704 coll. (1991)]



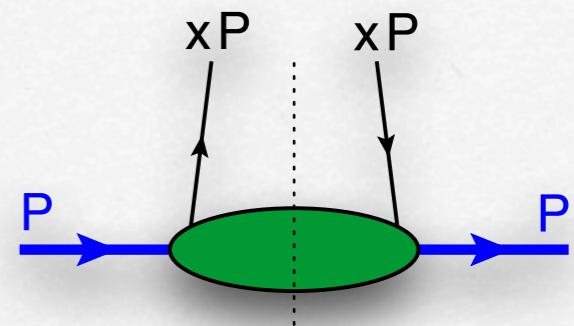
$\sqrt{s} = 200$ GeV [STAR coll. (2008)]

- sizeable effect at large x_F → too large to be left unexplained
- cannot be explained in the naive parton model
→ Twist-3 Formalism (ETQS)!

Transverse Spin Matrix Elements

1) Transversity distribution

$$h_1^q(x) = \int_{-\infty}^{\infty} \frac{d\lambda}{4\pi} e^{i\lambda x(P \cdot n)} \langle P, S_T | \bar{q}(0) \not{S}_T \not{\gamma} \not{\gamma}_5 [0; \lambda n] q(\lambda n) | P, S_T \rangle$$



"chiral-odd" structure

- in combination with other chiral-odd objects (Collins effect)
- quark mass effects (twist-3)

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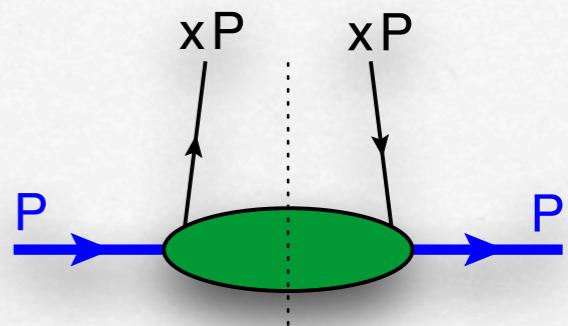
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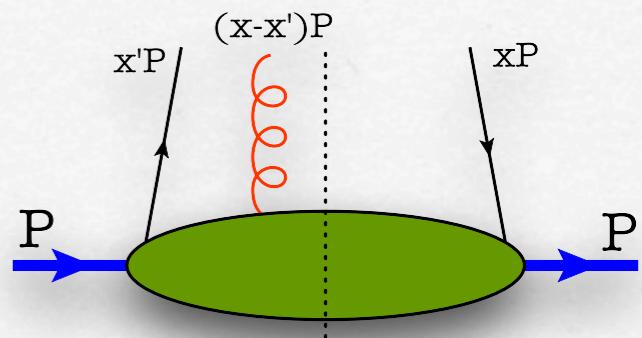
2) 'bad components' → g_T

$$g_T^q(x) = -\frac{(P \cdot n)}{M} \int_{-\infty}^{\infty} \frac{d\lambda}{4\pi} e^{i\lambda x(P \cdot n)} \langle P, S_T | \bar{q}(0) \not{S}_T \not{\gamma}_5 [0; \lambda n] q(\lambda n) | P, S_T \rangle$$

Twist - 3 characteristics hidden in Dirac structure



3) Quark - Gluon - Quark Correlations (ETQS-matrix elements)



$$\frac{M}{2} \epsilon_T^{\alpha\beta} S_{T\beta} G_F^q(x, x') = \int \frac{d\lambda d\eta}{2(2\pi)^2} e^{i(P \cdot n)(x' \lambda + (x - x')\eta)} \langle P, S_T | \bar{q}(0) \gamma^+ g F^{+\alpha}(\eta n) q(\lambda n) | P, S_T \rangle$$

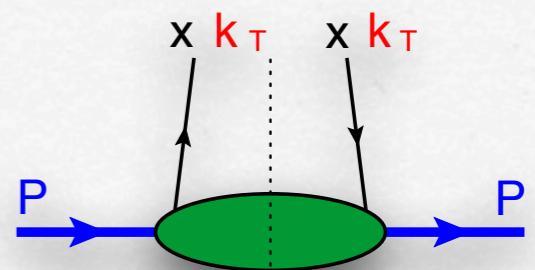
$$\frac{M}{2} S_T^\alpha i \tilde{G}_F^q(x, x') = \int \frac{d\lambda d\eta}{2(2\pi)^2} e^{i(P \cdot n)(x' \lambda + (x - x')\eta)} \langle P, S_T | \bar{q}(0) \gamma^+ \gamma_5 g F^{+\alpha}(\eta n) q(\lambda n) | P, S_T \rangle$$

'dynamical twist - 3'

- 3-parton correlator: suppression by additional propagator
 - dependence on two parton momenta x, x' :
2-dimensional support, richer parton dynamics
- so far: only "diagonal support" $G_F(x, x)$ constraint by data...
- 'integrated' $G_F(x, x')$: average transverse color Lorentz force on struck quark [Burkardt, PRD88, 114502]

$$F^y = [\vec{E} + \vec{v} \times \vec{B}]^y \propto \int dx \int dx' G_F(x, x')$$

4) 'Transverse Parton Momenta k_T '



'Sivers function'

$$f_{1T}^{\perp,(1)}(x) = \int d^2 k_T \frac{k_T^2}{2M^2} f_{1T}^\perp(x, k_T^2)$$

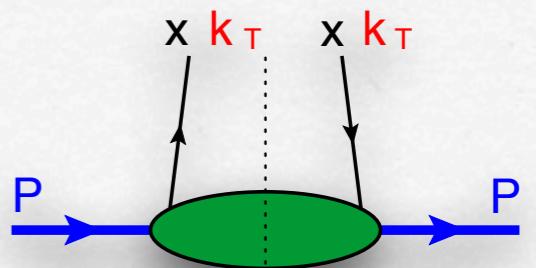
'wormgear function'

$$g_{1T}^{(1)}(x) = \int d^2 k_T \frac{k_T^2}{2M^2} g_{1T}(x, k_T^2)$$

'kinematical twist-3'

→ suppression by small transverse parton momentum k_T

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Relations in collinear factorization

Sivers vs. Gluonic Pole:

$$f_{1T,\text{DIS}}^{\perp(1)}(x) = \frac{\pi}{2} G_F(x, x)$$

'QCD - equation of motion':

$$\begin{aligned} g_{1T}^{(1)}(x) &= x g_T(x) - \frac{m_q}{M} h_1(x) \\ &\quad - \int_0^1 dx' \frac{G_F(x, x') + \tilde{G}_F(x, x')}{2(x' - x)} \end{aligned}$$

→ eliminate TMD moments in twist - 3 formalism

TMD - factorization: 'Fully evolved' form of Sivers function

[Aybat, Collins, Qiu, Rogers, PRD85,034043]

$$\frac{\partial}{\partial b_T} f_{1T}^\perp(x, b_T; \mu, \zeta) \propto \left[\int_x^1 dz dz' C(z, z', \mu_b) G_F(z, z', \mu_b) \right] e^{(S_{\text{pert}} + S_{\text{non-pert}})(b_T)}$$

→ G_F determines x -dependence of Sivers function

→ C at NLO: full support of G_F needed!

→ Sivers function \leftrightarrow Spin-Orbit Correlation/OAM (talk by A. Bacchetta)

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back to pion production... $p + p^\uparrow \rightarrow \pi + X$

many competing twist-3 effect:

→ tw-3 transverse spin matrix elements ('Sivers'-like)

→ chiral-odd tw-3 matrix elements of unpolarized proton ('Boer-Mulders'-like)

→ tw-3 matrix elements describing fragmentation ('Collins'-like)

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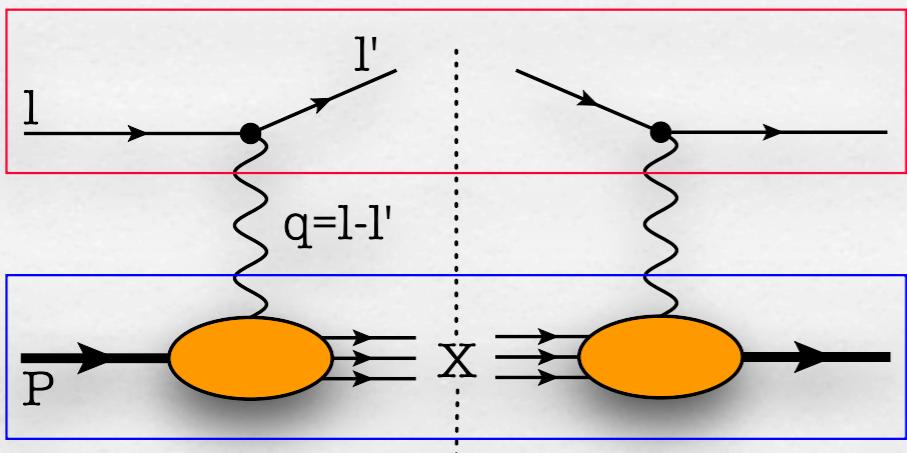
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Fragmentation seems to dominate! [Kanazawa, Koike, Metz, Pitonyak, PRD89, 111501(R)]

⇒ Less complicated processes?

Transverse Spin Asymmetries in deep-inelastic lepton-nucleon processes

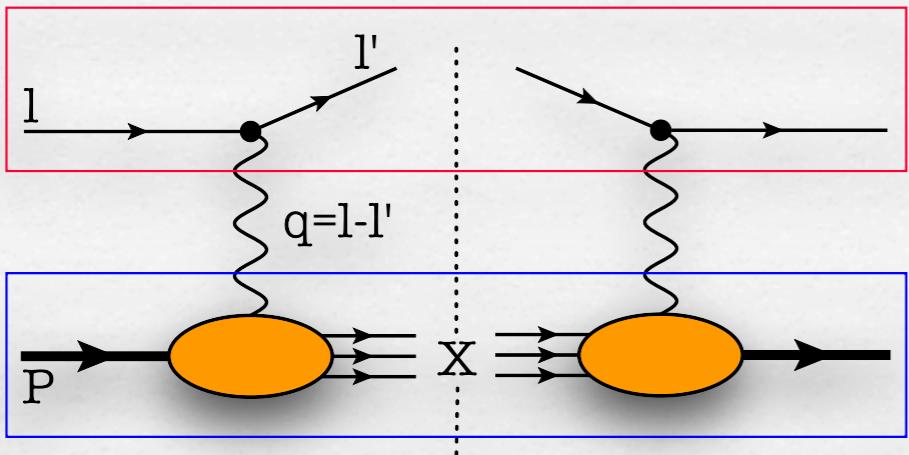
The archetype: g_2 in DIS ($e^+ + p^\uparrow \rightarrow e + X$)



Structure functions

$$\frac{d\sigma}{dx_B dy} \propto (F_1, F_2) + \lambda_e S_L g_1 + \lambda_e S_T \cos \phi_s (g_1 + g_2)$$

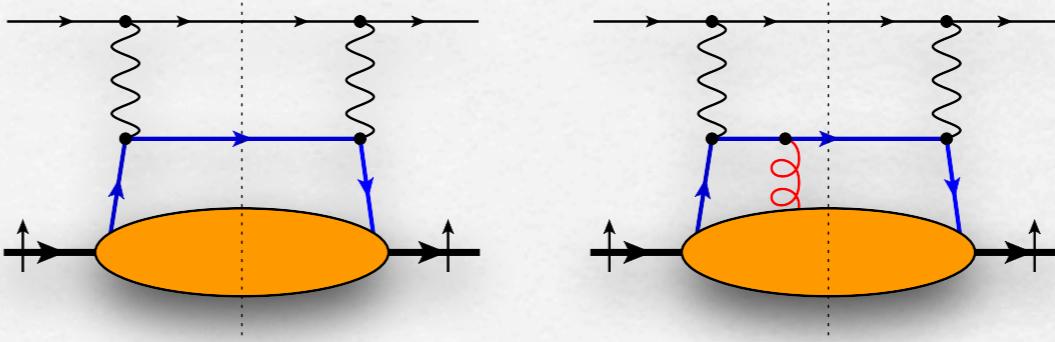
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Twist - 3 formalism



Hard part to LO:

Double-Spin Asymmetry:

$$A_{LT} \propto (g_1 + g_2) \propto x g_T(x) + g_{1T}^{(1)}(x) + \frac{m_q}{M} h_1(x) + \int_0^1 dx' \frac{G_F(x, x') + \tilde{G}_F(x', x)}{2(x' - x)}$$

(QCD – EOM) $\rightarrow 2 x g_T(x)$

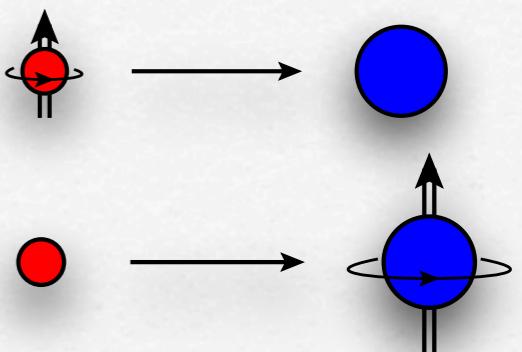
Transverse SSA in DIS

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$A_N = 0$ in $1-\gamma$ exchange [Christ, Lee, 1966]!

⇒ New effects for a Two-Photon Exchange!

$$A_N = \frac{\sigma^{\uparrow} - \sigma^{\downarrow}}{\sigma^{\uparrow} + \sigma^{\downarrow}}$$

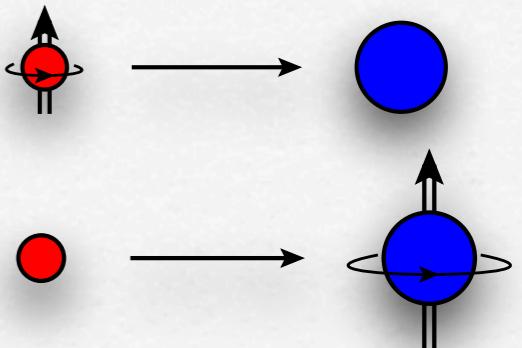


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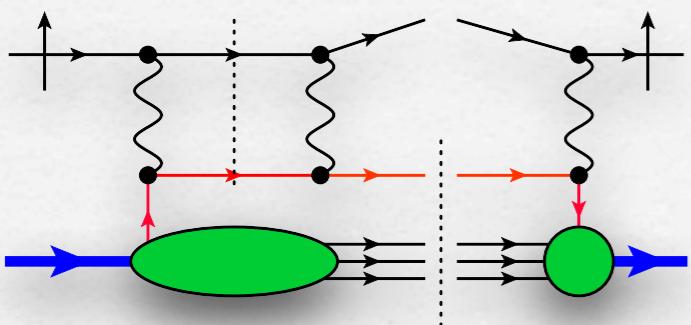
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Transverse Single-Beam Spin Asymmetry in DIS

[Metz, M.S., Goeke, PLB 643 (2006) 319]



Transversely polarized lepton → lepton mass effect

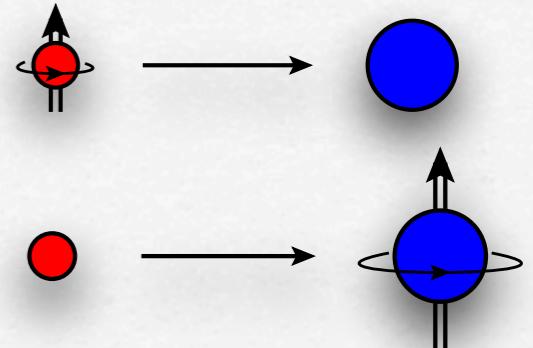
$$A_{TU} = \frac{d\sigma^{\uparrow} - d\sigma^{\downarrow}}{d\sigma^{\uparrow} + d\sigma^{\downarrow}} \propto \alpha_{\text{em}} \frac{m_l}{Q} \sum_q e_q^3 f_1^q(x_B)$$

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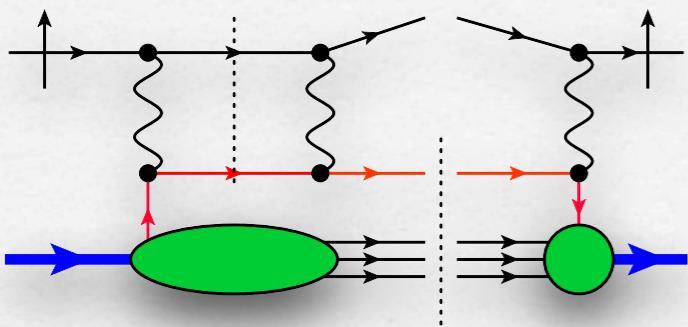
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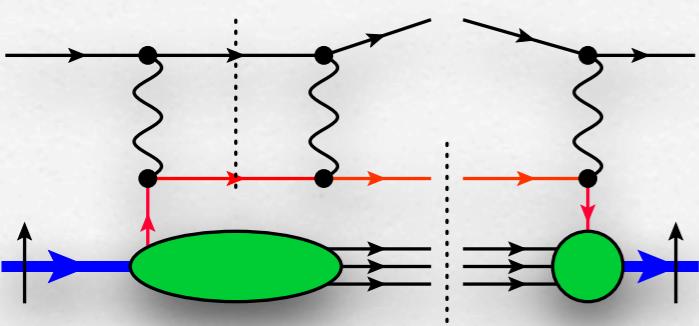


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Transverse Target Single Spin Asymmetry in DIS

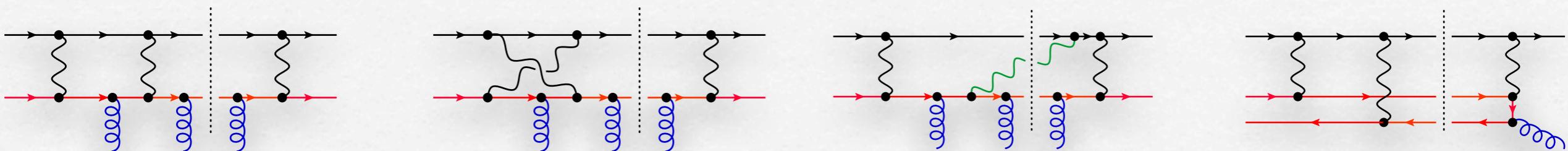
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$$A_{UT} \propto \alpha_{\text{em}} \frac{M}{Q} \left(\frac{a}{\varepsilon} + b \right) \sum_q e_q^3 x_B g_T^q(x_B)$$

QED NLO soft singularities ⇔ higher twist effects

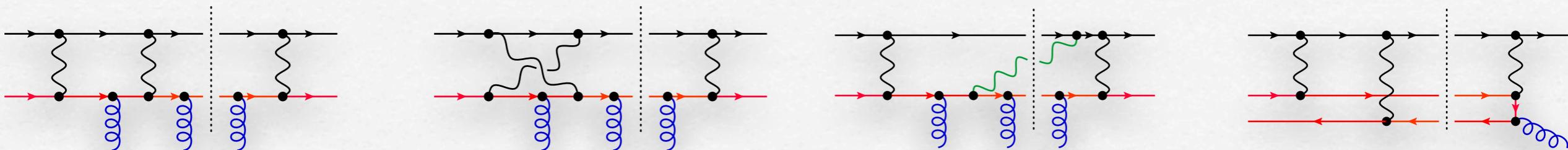
Inclusion of 'Quark - Gluon Correlations'



→ Sum of all twist-3 Two-Photon effects finite!

[MS, PRD 87, 034006 (2013)]

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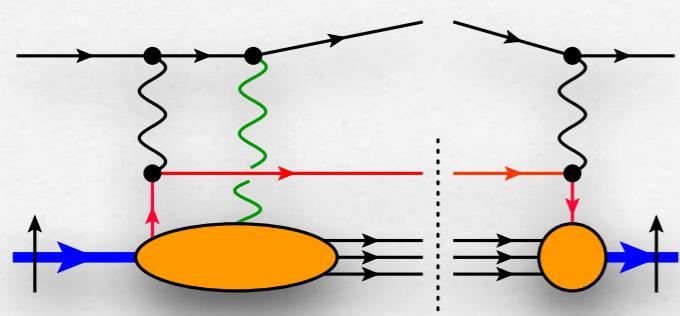


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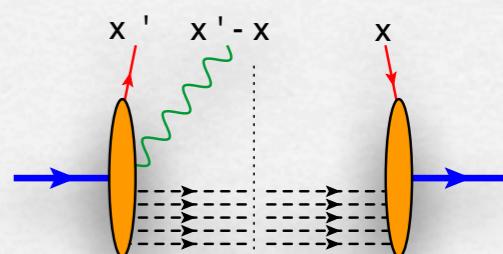
Complementary effect: Soft photon from nucleon wave function

[Metz, Pitonyak, Schäfer, MS, Vogelsang, Zhou, PRD86, 094039 (2012)]

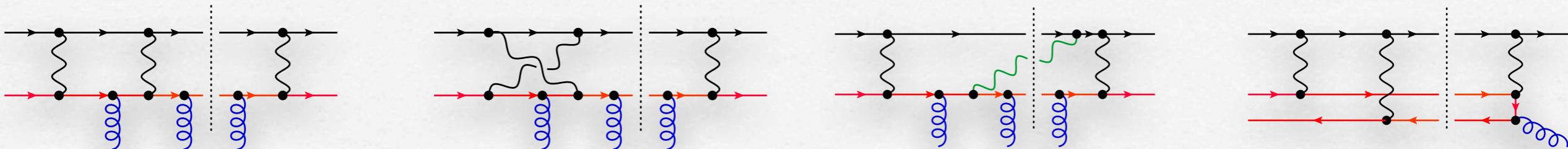


Contributions from Quark - Photon - Quark Correlations

$$G_F^\gamma(x, x') \sim \langle \bar{q} F_{\text{em}} q \rangle$$



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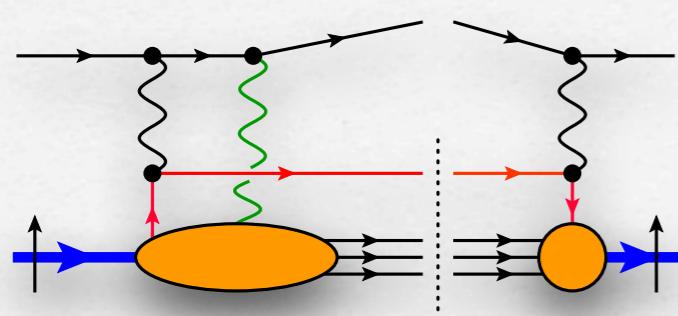


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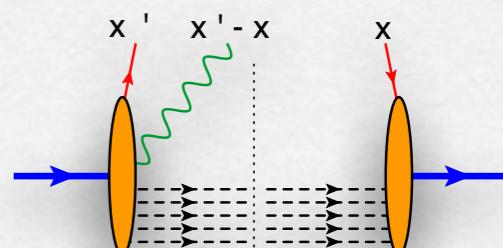
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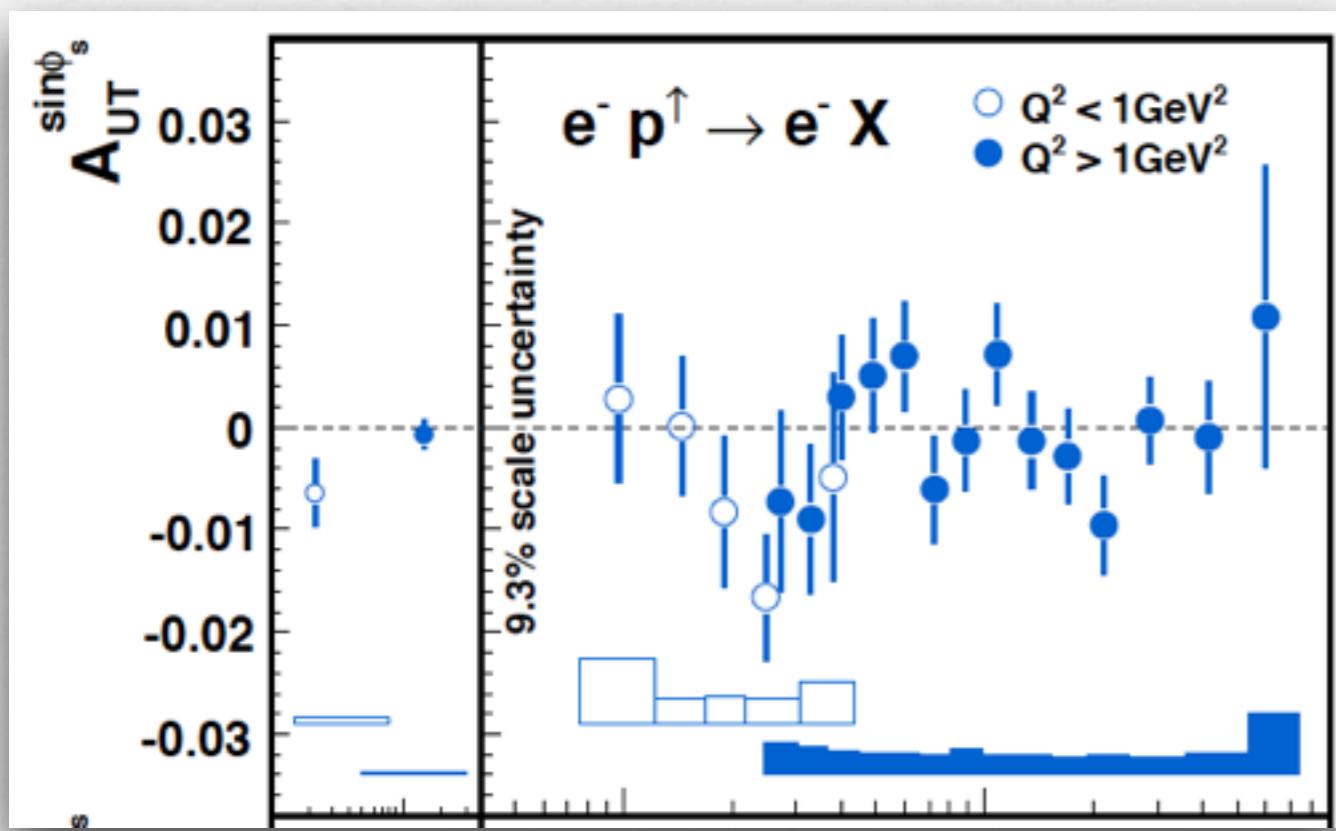


Final result [MS, PRD 87, 034006 (2013)]

$$\begin{aligned} A_{UT} \propto & \alpha_{\text{em}} \frac{M}{Q} \left[\int_0^1 dx \left(\hat{\sigma}_+ \left(\frac{x_B}{x}, y \right) G_F(x_B, x) + \hat{\sigma}_- \left(\frac{x_B}{x}, y \right) \tilde{G}_F(x_B, x) \right) \right. \\ & \left. + f(y) \left(1 - x_B \frac{d}{dx_B} \right) G_F^\gamma(x_B, x_B) + g(y) \frac{m_q}{M} h_1(x_B) \right] \end{aligned}$$

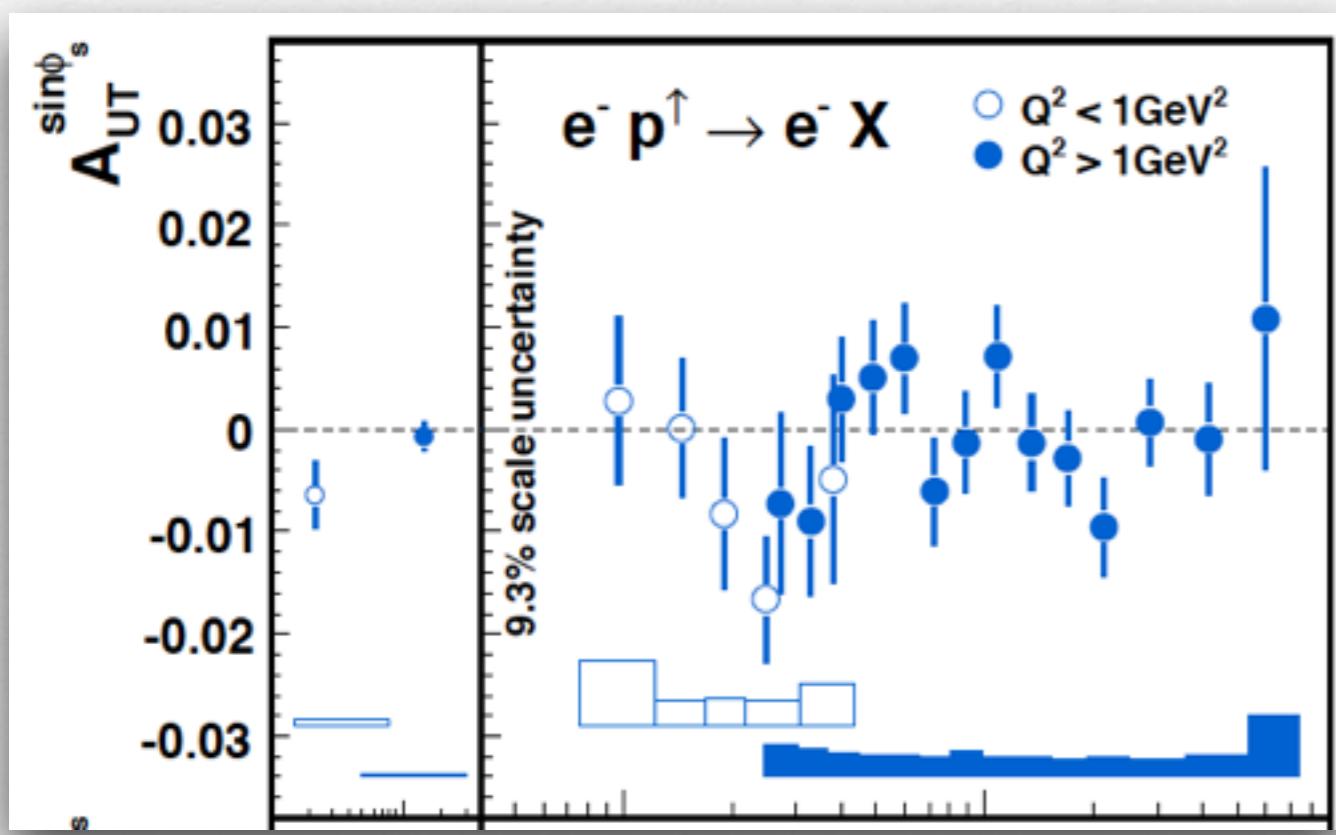
Experimental situation

HERMES [PLB682, 351 (2010)]
polarized proton target

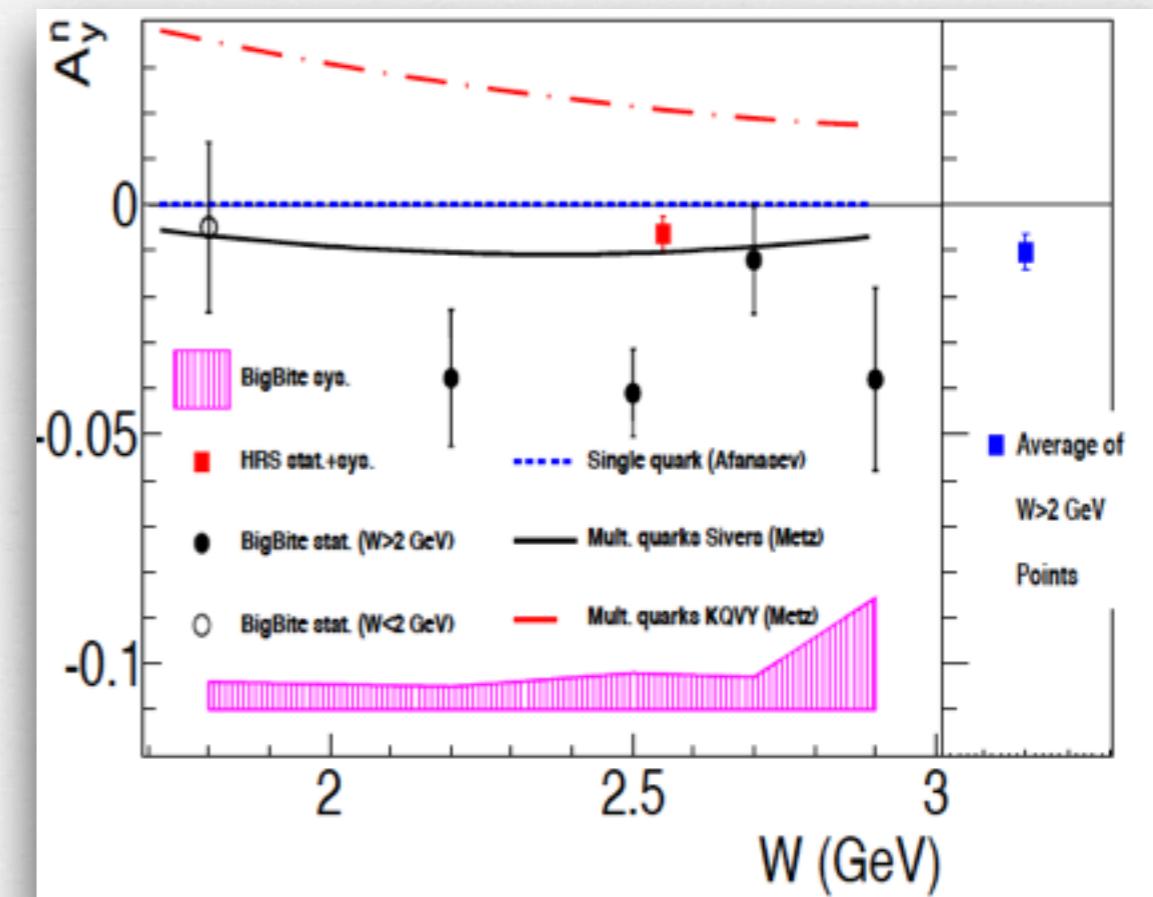


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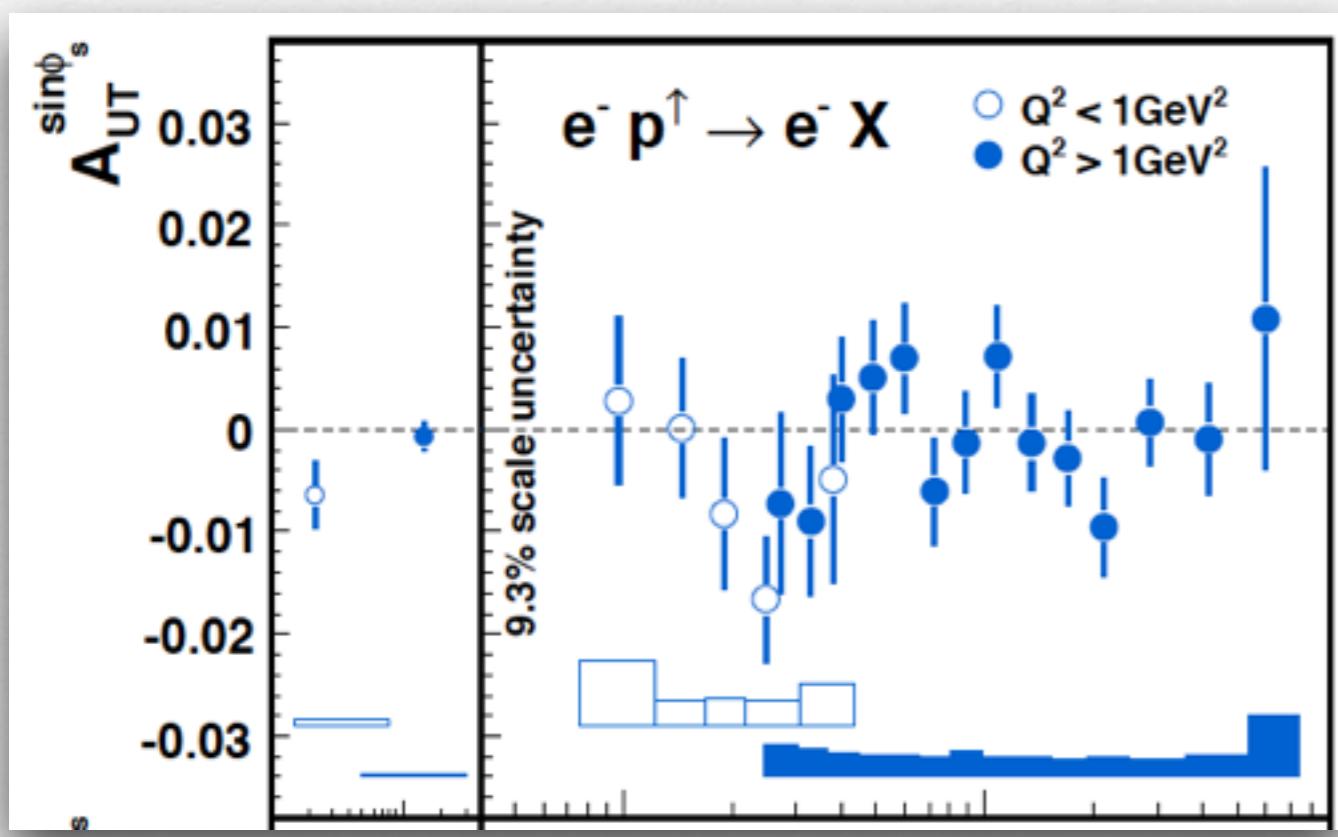


JLab [PRL113, 022502]
polarized He^3 (~neutron) target

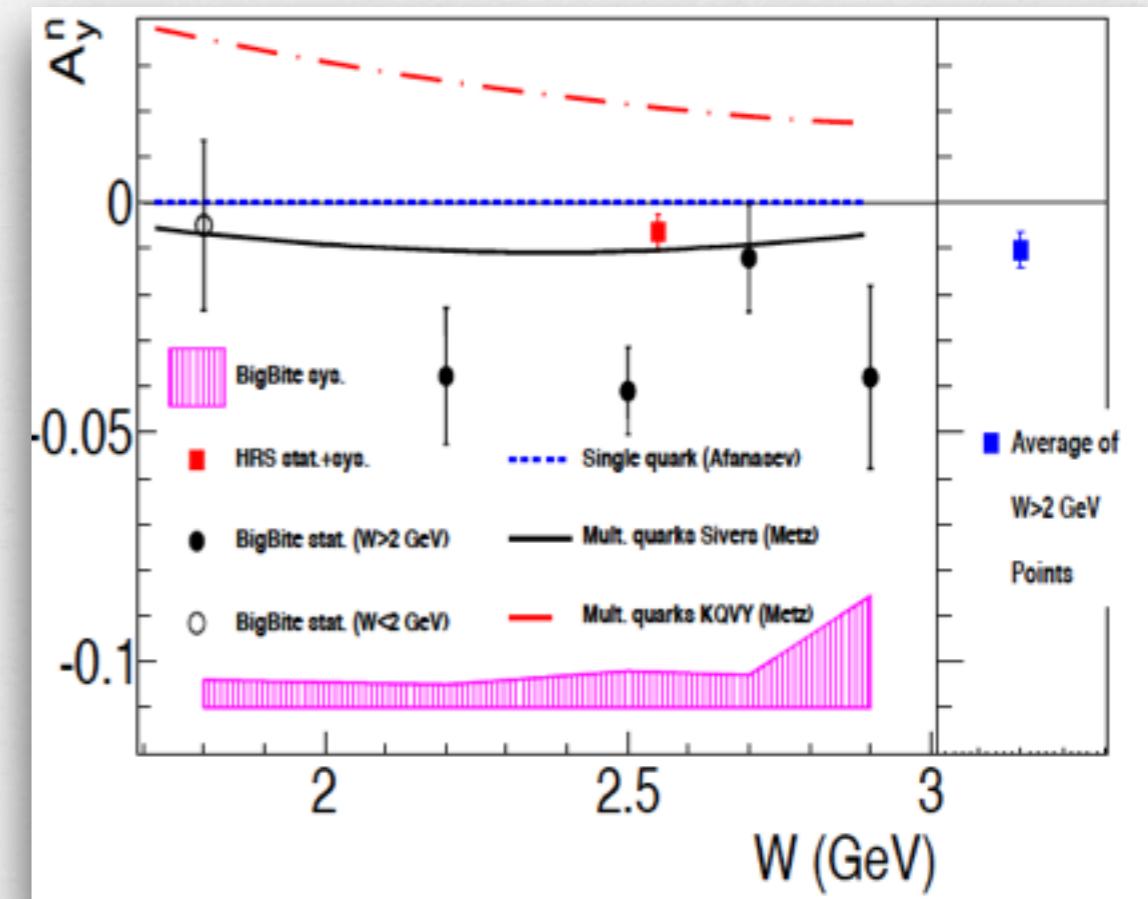


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Models \rightarrow quark-photon-quark correlations seem to dominate for He^3
Measurements to be continued at JLab12 for He^3 and proton target

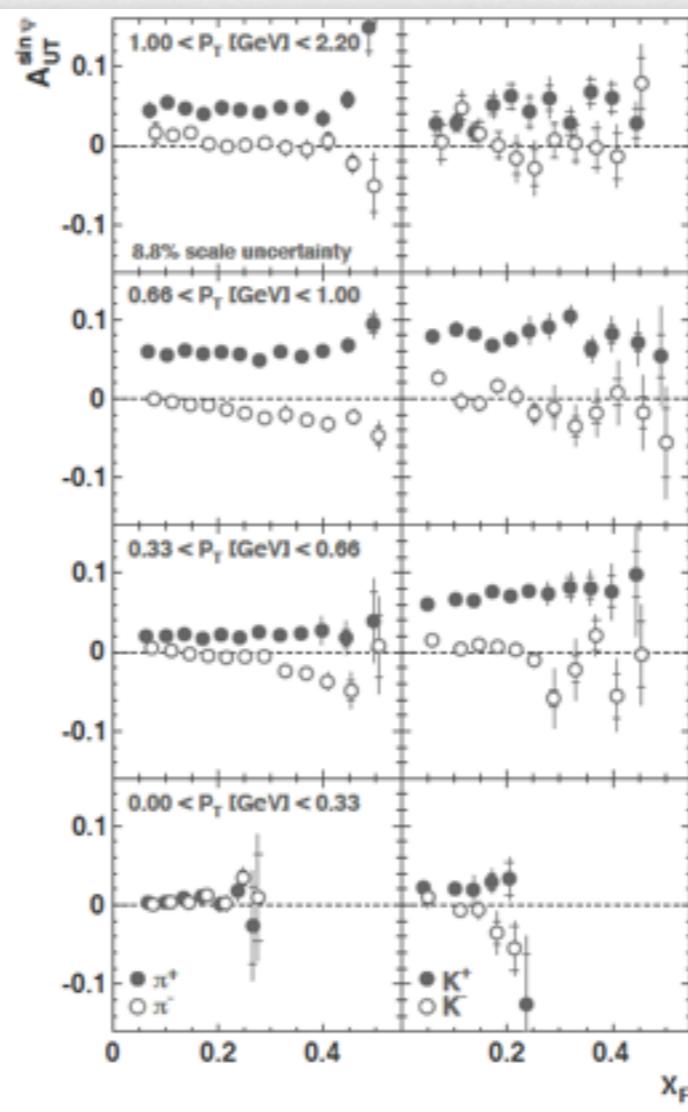
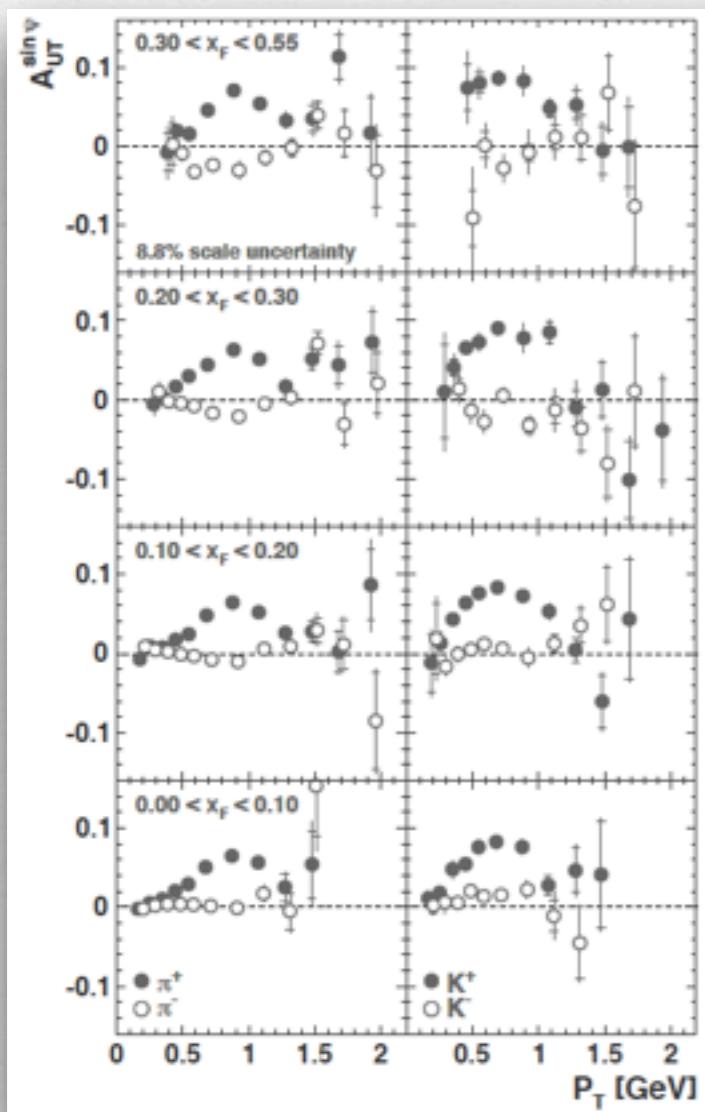
Hadron production in lepton - hadron collisions

$$(e + p^\uparrow \rightarrow h + X)$$

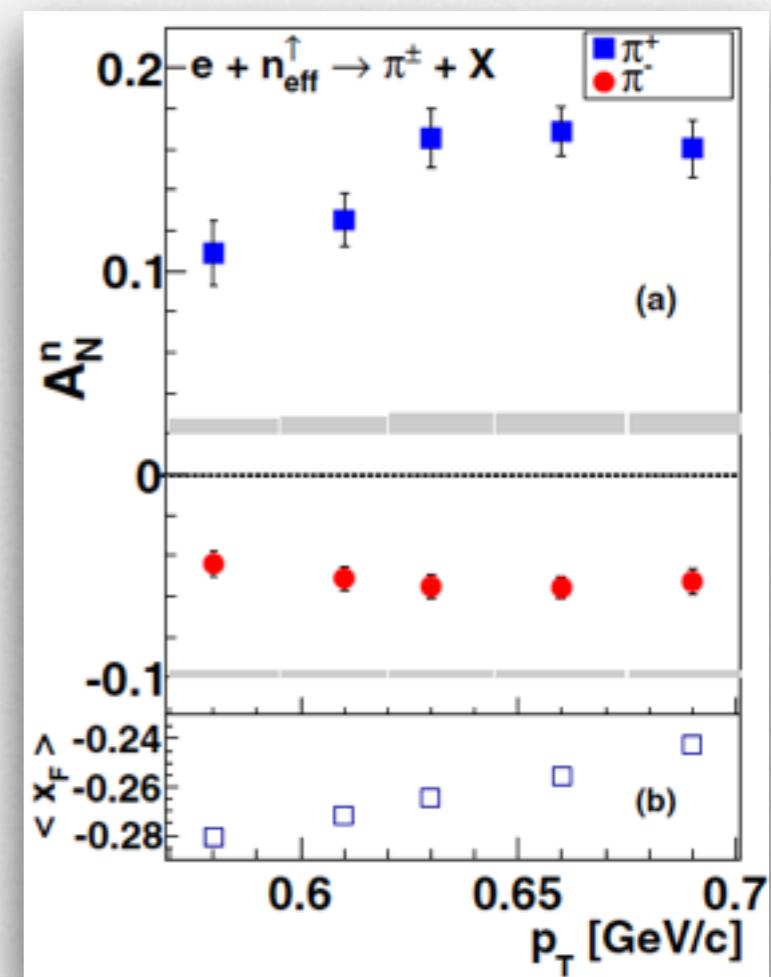
$$P_T \gg \Lambda_{\text{QCD}}$$

amazingly accurate data from HERMES, JLab...

HERMES [PLB728, 183]



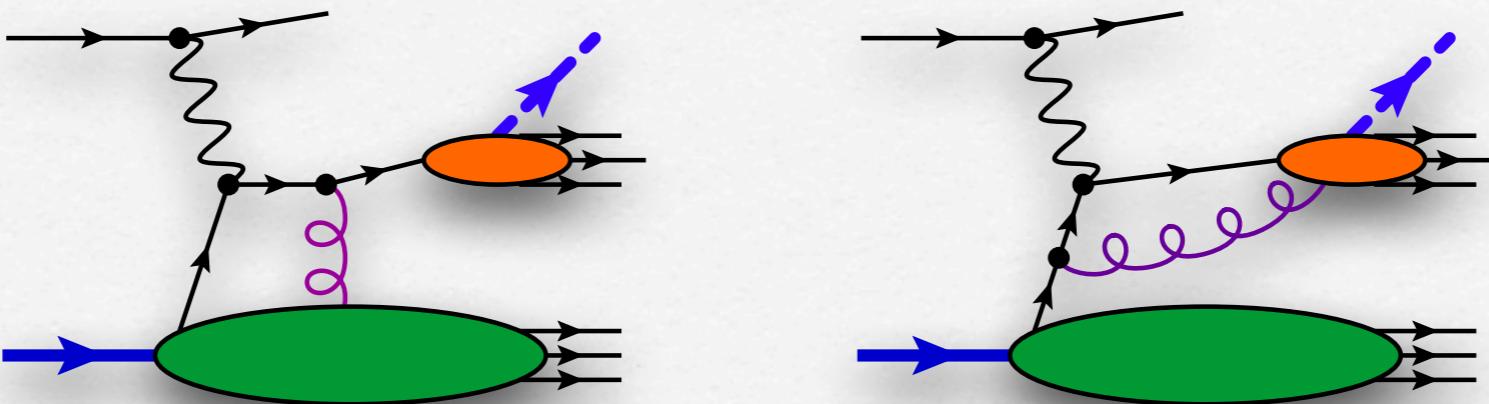
JLab [PRC89, 042201(R)]



$p_T < 1 \text{ GeV} \Rightarrow p\text{QCD}?$

LO calculation:

[Gamberg, Kang, Metz, Pitonyak, Prokudin, arxiv:1407.5078]

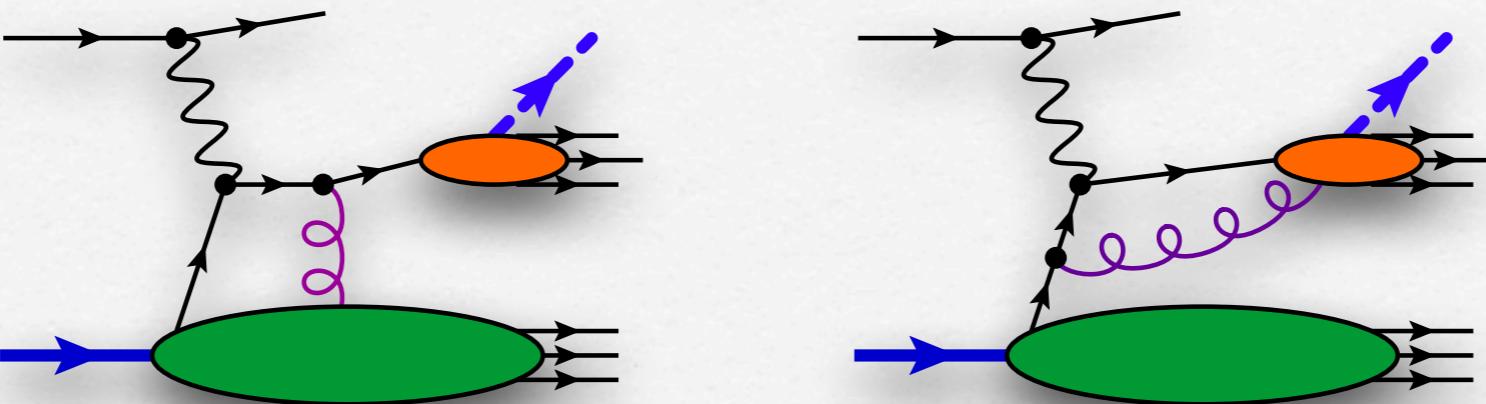


outgoing lepton momentum integrated out:

twist - 3 ETQS matrix elements \otimes twist - 3 fragmentation

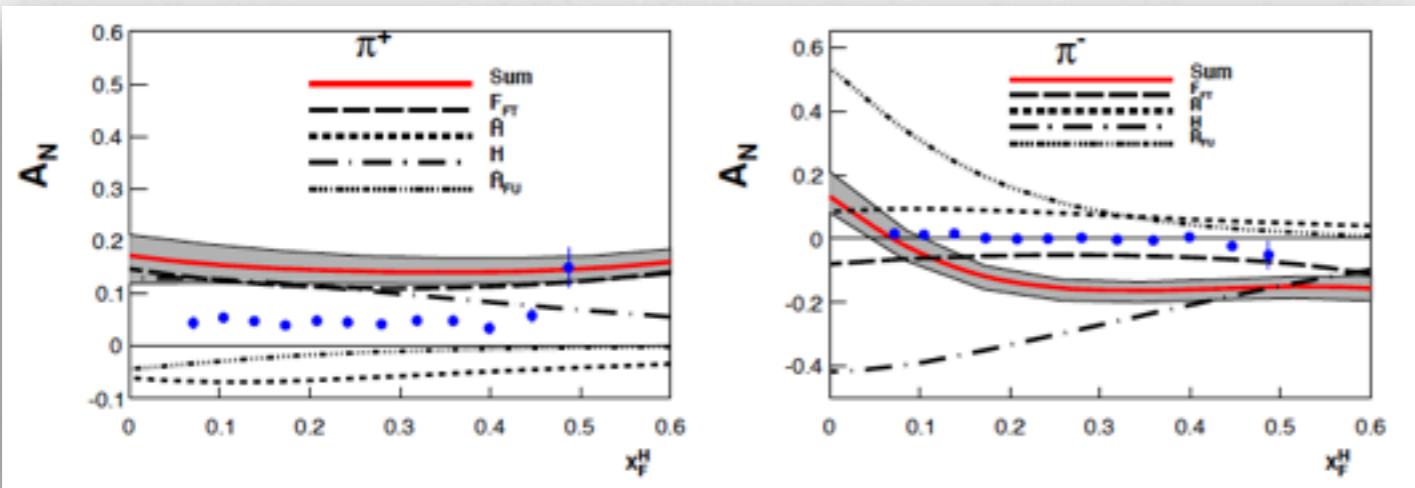
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LO input typically
overshoots the data

\rightarrow NLO?

\rightarrow refit?

\Rightarrow opportunity for EIC

opportunity for EIC: $e + p^\uparrow \longrightarrow \text{jet} + X$

Photon Semi-inclusive DIS

or

'inclusive DVCS'

($e + p \rightarrow e + \gamma + X$)

Photon semi-inclusive DIS: $e + p \rightarrow e + \gamma + X$

[Prokudin, Radyushkin, M.S., in preparation]

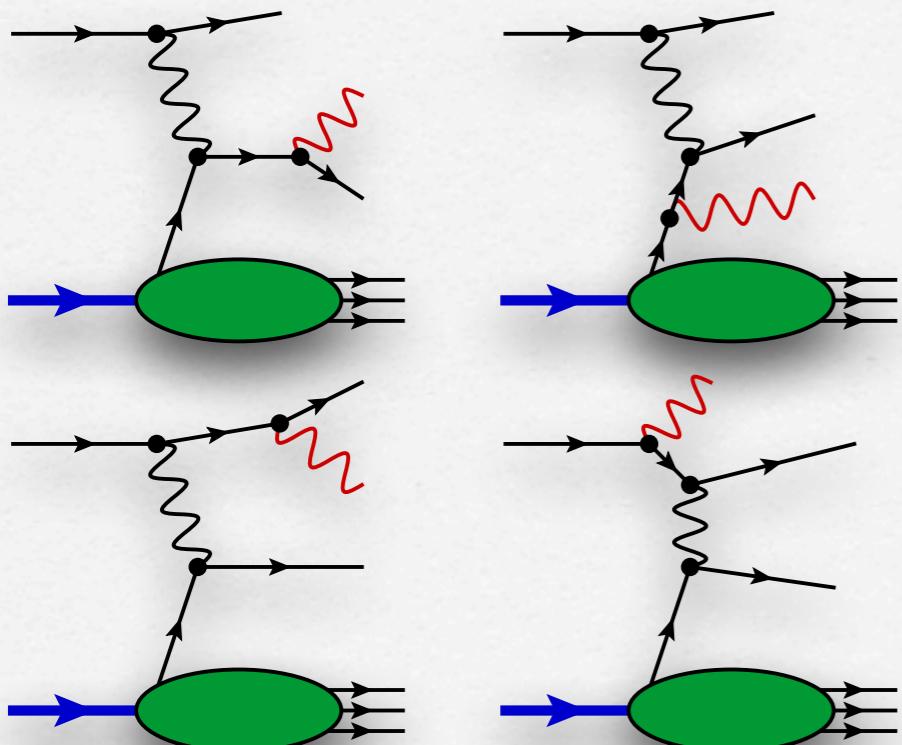
Circumvent Christ - Lee theorem: real photon emission

Photon semi-inclusive DIS: $e + p \rightarrow e + \gamma + X$

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Circumvent Christ - Lee theorem: real photon emission

unpolarized cross section in the parton model



- avoid photon fragmentation: isolated photons
- collinear factorization:
information on final quark is integrated out
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LO result:

$$E_\gamma E_e \frac{d\sigma_{UU}}{d^3 \vec{P}_\gamma d^3 \vec{P}_e} = \sum_q \left[e_q^2 \hat{\sigma}_2 + e_q^3 \hat{\sigma}_3 + e_q^4 \hat{\sigma}_4 \right] f_1^q(\bar{x})$$

- Different 'Bjorken-x':

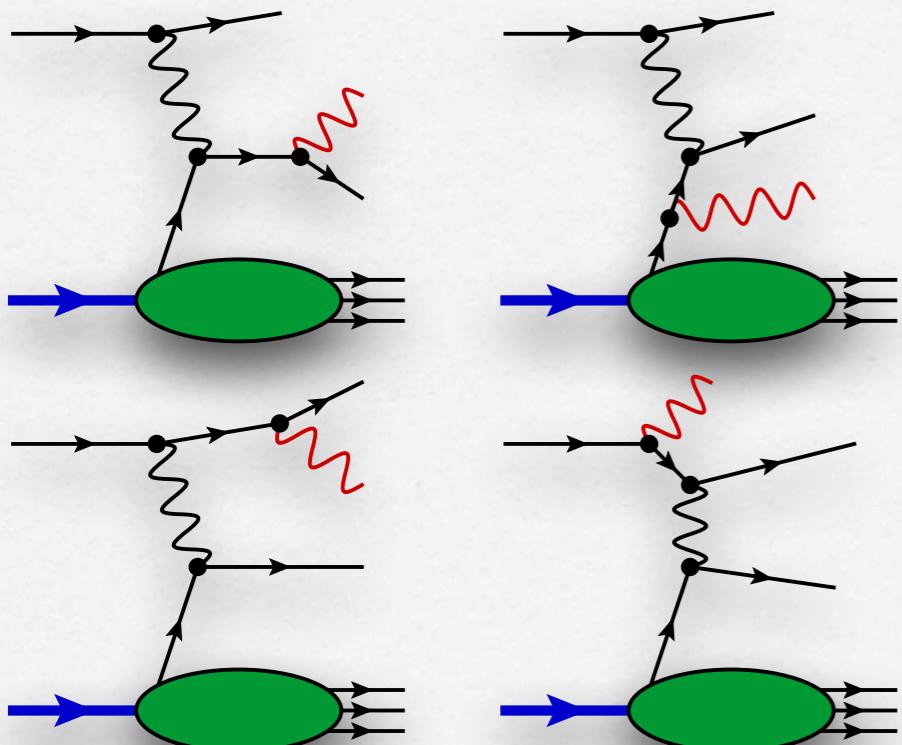
$$\bar{x} = -\frac{\bar{S} + \bar{T} + \bar{U}}{\bar{S} + \bar{T} + \bar{U}}$$

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[Prokudin, Radyushkin, M.S., in preparation]

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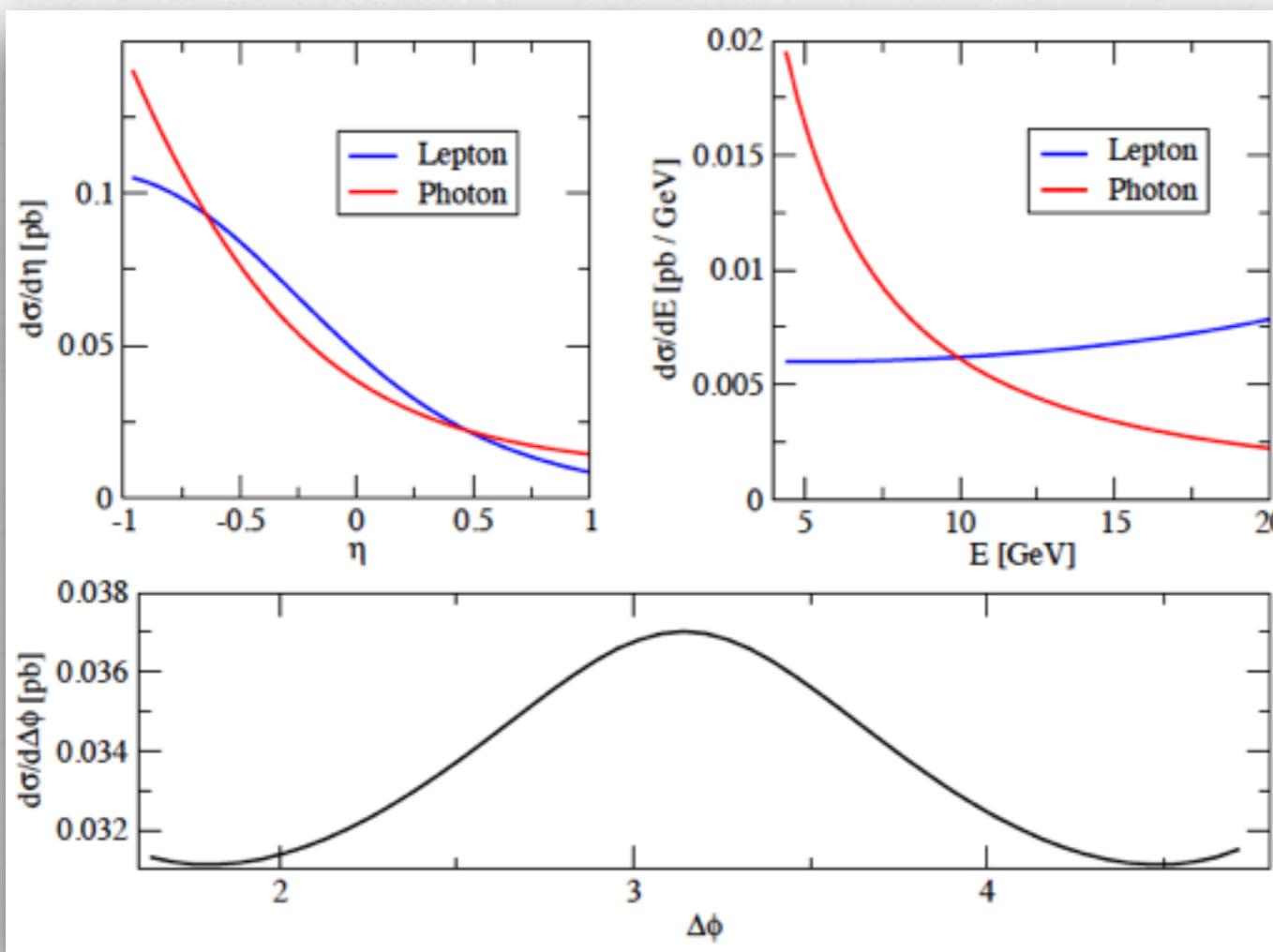
rare process, cross section = $\mathcal{O}(\alpha^3)$ \rightarrow too rare?

LO numerical estimate

- Assume collider mode, $S^{1/2} = 100 \text{ GeV}$ (EIC)
- e - p - c.m. frame & midrapidity "back-to-back" lepton-photon pairs
 - ⇒ assume cuts $-1 \leq \eta_{\gamma/e} \leq 1$, $E_{\gamma/e} \leq S^{1/2}/2$, $\pi/2 \leq \Delta\phi \leq 3\pi/2$
 - ⇒ no "soft" propagators in LO hard part

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total cross section

$$\sigma^{\gamma SIDIS} \simeq 100 \text{ fb}$$

$$(\sigma^{\text{DIS}} \simeq 100 \text{ pb})$$

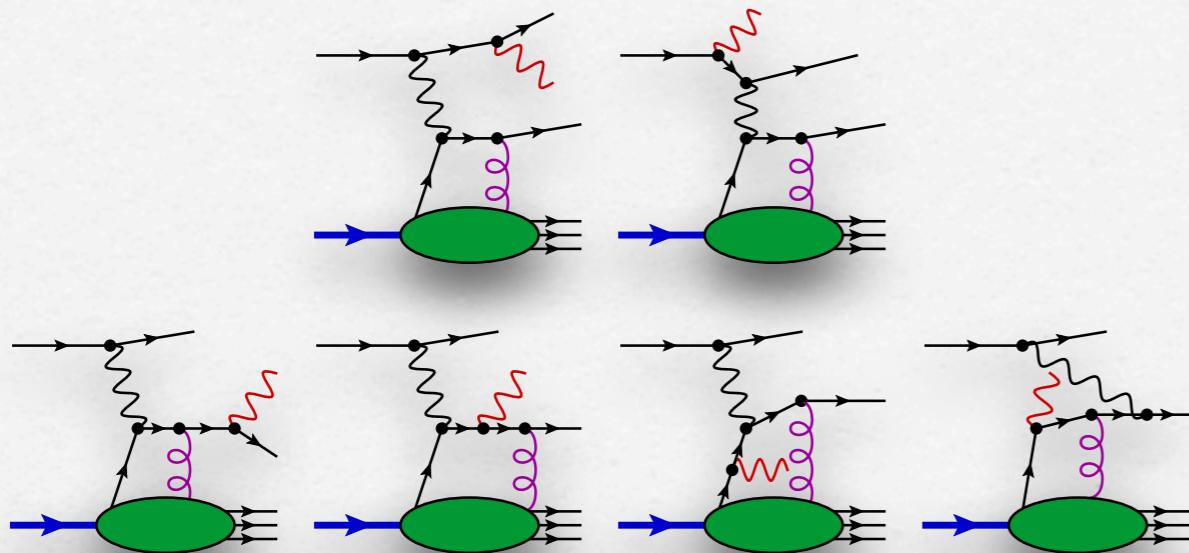
differential cross section

$$d\sigma^{\gamma SIDIS} \simeq O(10 \text{ fb})$$

\Rightarrow Needs large luminosity
 (JLab or EIC)

Transverse SSA in photon SIDIS

Include 'bad components', 'kinematical' & 'dynamical' twist - 3 contributions



At tree-level (LO):

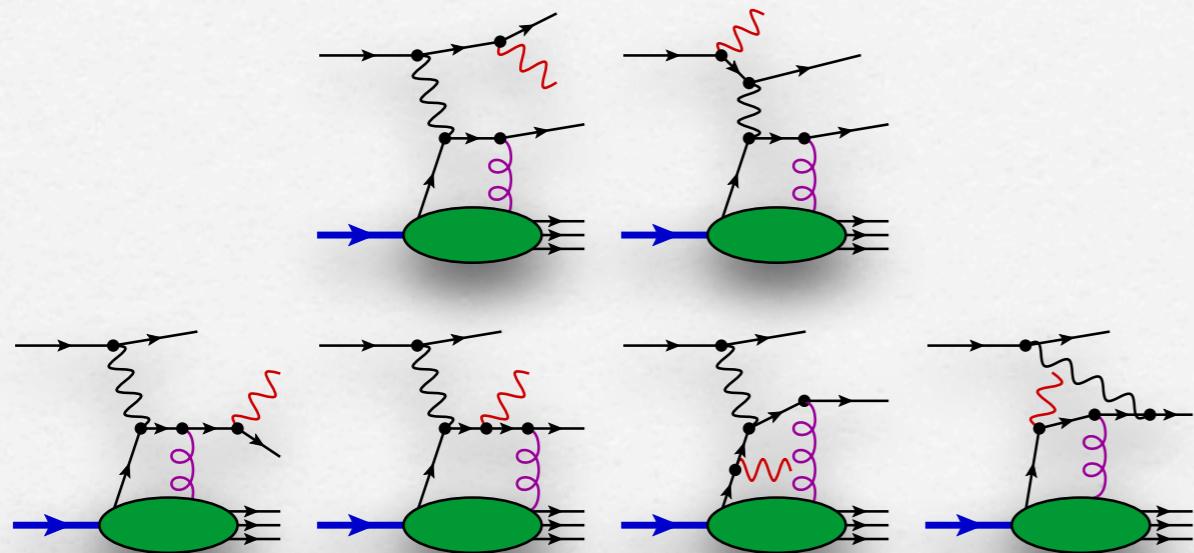
No contribution from g_T and $g_{IT}^{(1)}$
(no imaginary part)

Quark - Gluon correlations:

- 1) Soft Gluon Poles: $G_F(x,x)$
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LO Result:

$$\bar{x} = -\frac{\bar{S} + \bar{T} + \bar{U}}{\bar{S} + \bar{T} + \bar{U}} \quad ; \quad \tilde{x} = -\frac{\bar{T}}{\bar{S} + \bar{T}}$$

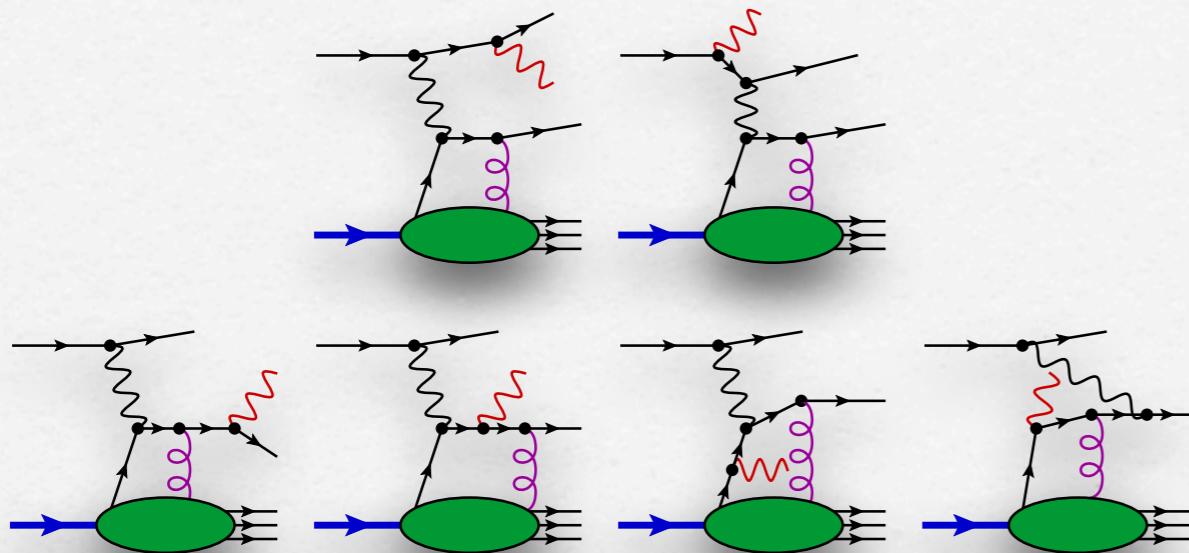
$$E_\gamma E_e \frac{d\sigma_{UT}}{d^3 \vec{P}_\gamma d^3 \vec{P}_e} = \sum_q \left[\hat{C}_{1,\text{SGP}} G_F(\bar{x}, \bar{x}) + \hat{C}_{2,\text{SGP}} \frac{d}{d\bar{x}} G_F(\bar{x}, \bar{x}) \right. \\ \left. + \hat{C}_{+,\text{SFP}} G_F(\bar{x}, 0) + \hat{C}_{-,\text{SFP}} \tilde{G}_F(\bar{x}, 0) \right. \\ \left. + \hat{C}_{+,\text{HFP}} G_F(\bar{x}, \tilde{x}) + \hat{C}_{-,\text{HFP}} \tilde{G}_F(\bar{x}, \tilde{x}) \right]$$

Soft Gluon Poles vanish
($C_{1/2,\text{SGP}} = 0$)!

Coefficients $e_q^2 C^2 = 0$
(Christ - Lee theorem)!

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⇒ unique process to directly study "off-diagonal" support
of twist - 3 Quark - Gluon Correlation functions!

Summary

- Twist - 3 matrix elements essential for the understanding of transverse SSA.
- ETQS - matrix element $G_F(x,x)$: extractions from semi-inclusive data
- Most promising process to fine-tune $G_F(x,x)$: $e + p^\uparrow \longrightarrow h/\text{jet} + X!$
- Direct information at LO on "non-diagonal" from photon SIDIS.

wandzura - Wilczek (WW) relation

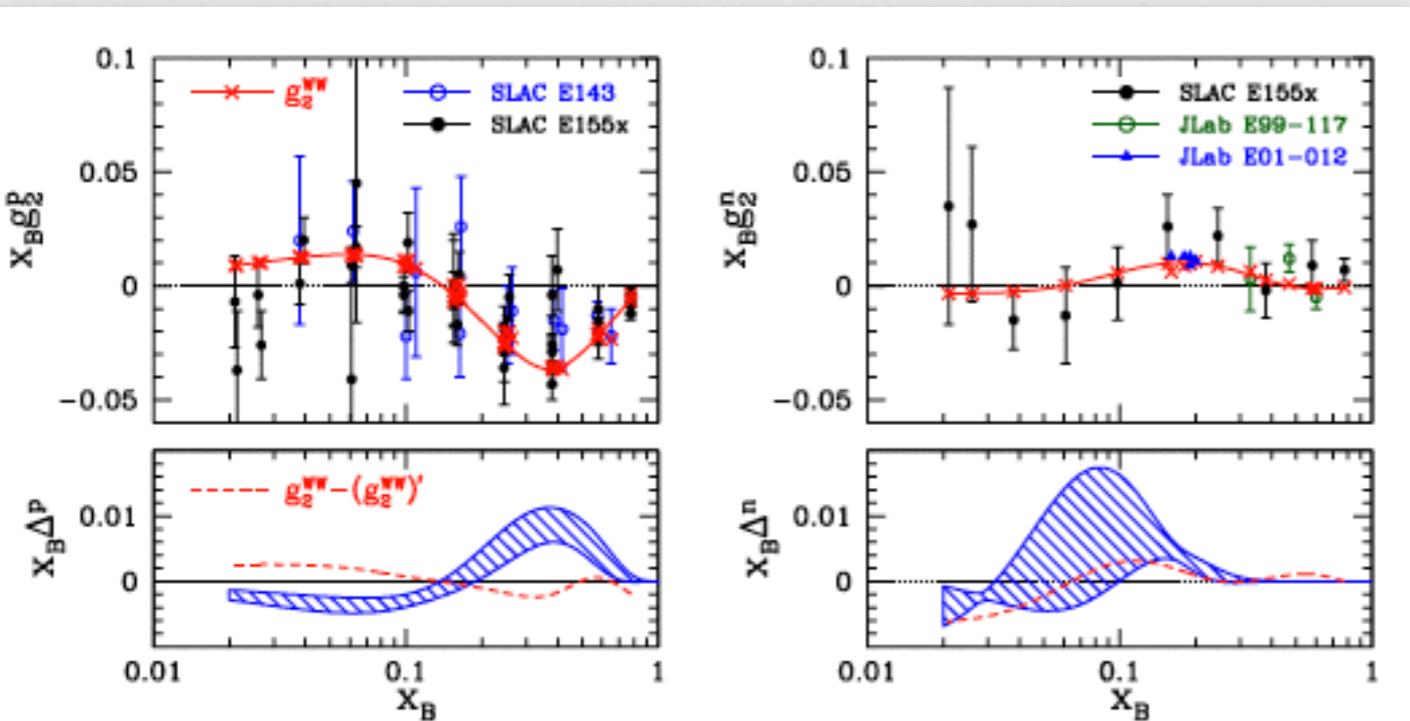
$$(g_1 + g_2)(x_B, Q^2) = \int_{x_B}^1 \frac{dy}{y} g_1(y, Q^2) + \Delta(x_B, Q^2)$$

- derivation from Operator Product Expansion
- Breaking term of the WW approximation: Δ - term
- Common assumption: $\Delta = 0$ (small!)
- $\Delta \iff$ Quark - Gluon Correlation functions $(G_F(x, x'), \tilde{G}_F(x, x'))$

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Quantitative analysis
[Accardi, Bacchetta, Melnitchouk, MS, JHEP0911(2009)093]

Fit to JLab & SLAC (p,n) data

$$\Delta(x_B) = \alpha(1 - x_B)^\beta((2 + \beta)x_B - 1)$$

Effect about 15% - 40% of g_2^{WW} !
Quark - Gluon - Quark Correlations
not necessarily small!