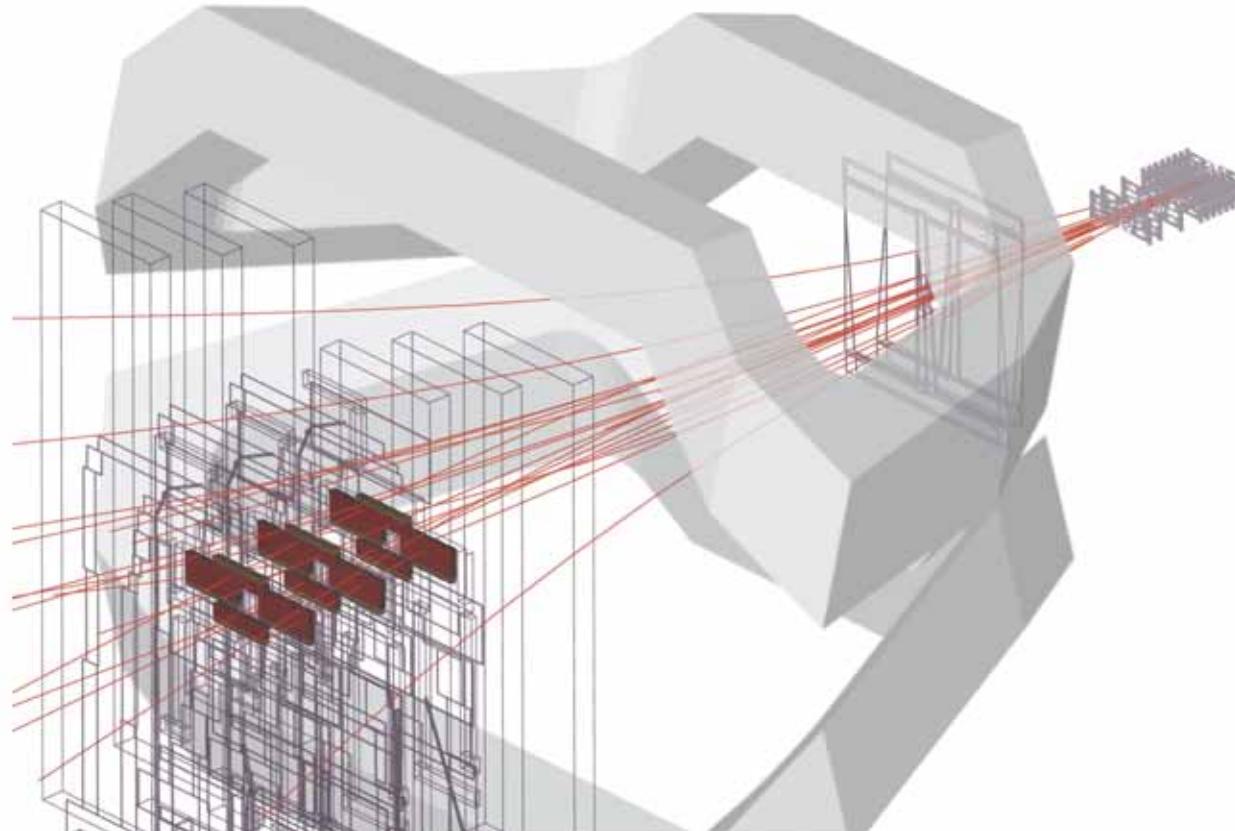


# Results on CP Violation in $B_s$ Mixing [measurements of $\phi_s$ and $\Delta\Gamma_s$ ]



Presentation on behalf of LHCb Collaboration  
Rencontres de Moriond, La Thuile, 3-10 March 2012



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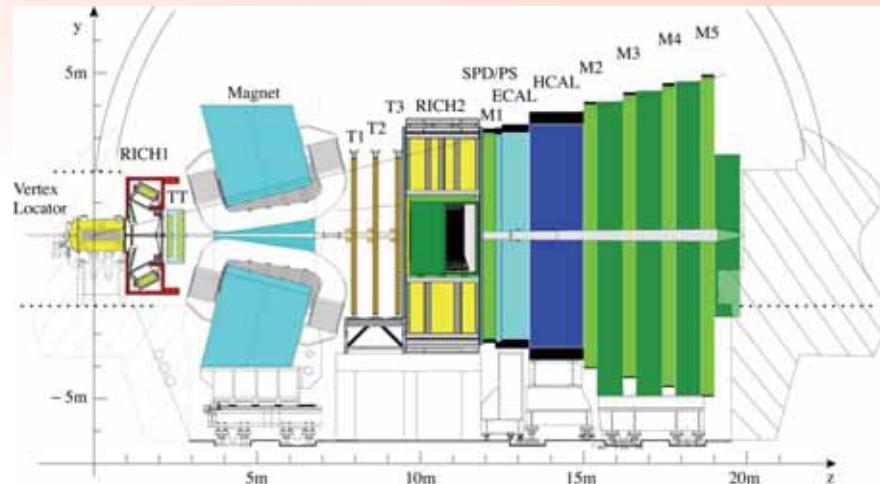
This talk presents new LHCb results since 2011 summer conferences

- Using the full  $1\text{fb}^{-1}$  of data from 2011 (was  $0.37\text{fb}^{-1}$ )
- CPV phase  $\phi_s$ ,  $\Delta\Gamma_s$  and other quantities from  $B_s \rightarrow J/\psi\Phi$ 
  - LHCb-CONF-2012-002
  - [arXiv:1112.3183v2](https://arxiv.org/abs/1112.3183v2) to be published in PRL
- $\phi_s$  from  $B_s \rightarrow J/\psi\pi\pi$ 
  - LHCb-PAPER-2012-006 to be submitted to PLB
- Resolution of the “two fold ambiguity” for  $\phi_s$  &  $\Delta\Gamma_s$ 
  - [arXiv:1202.4717v2](https://arxiv.org/abs/1202.4717v2) submitted to PRL

## The detector

These new results are due to

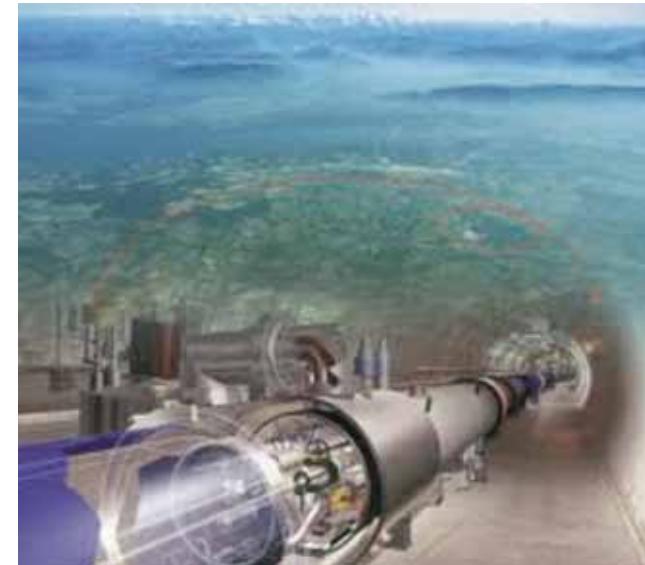
- Excellent running of detector
- Excellent running of LHC
- Efforts of all the people



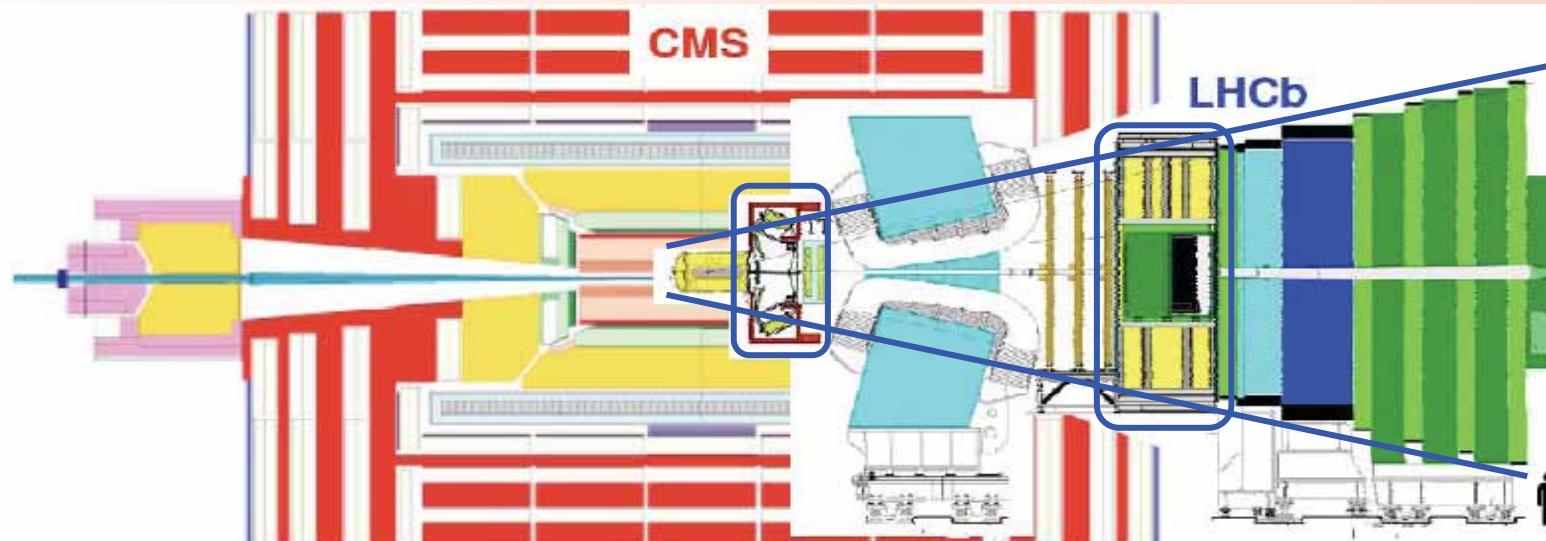
## The people



## The LHC



# LHCb in context



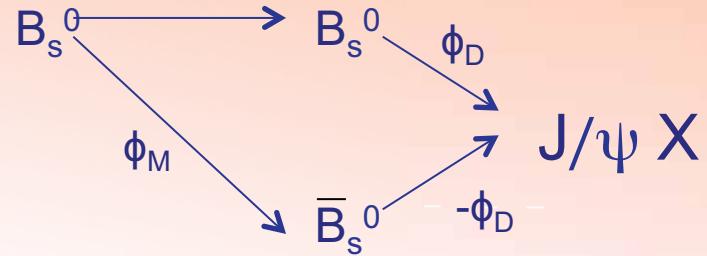
- LHCb is a forward spectrometer
- $2 < \eta < 5$
- Optimised for *b* and *c* physics
- Precise tracking and decay vertex finder
- Good particle ID

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## Experimental phenomenology of CP Violating phase $\phi_s$

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- Measure relative phase difference<sup>1</sup>  
 $\phi_s = \phi_M - 2\phi_D$  between two “legs”



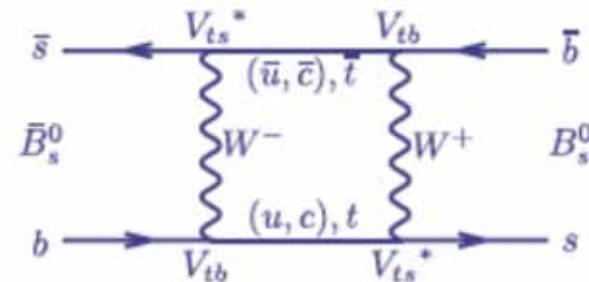
- In SM & normal conventions & ignoring penguins

$$\phi_D \sim 0$$

$$\phi_s^{\text{SM}} \sim \phi_M$$

- is predominantly determined<sup>2</sup> by  $\arg(V_{ts}^*)$
- is predicted to be small  $\sim -0.04$

[Charles et al. Phys. Rev. D84 (2011) 033005]



- New Physics (NP) can add large phases:

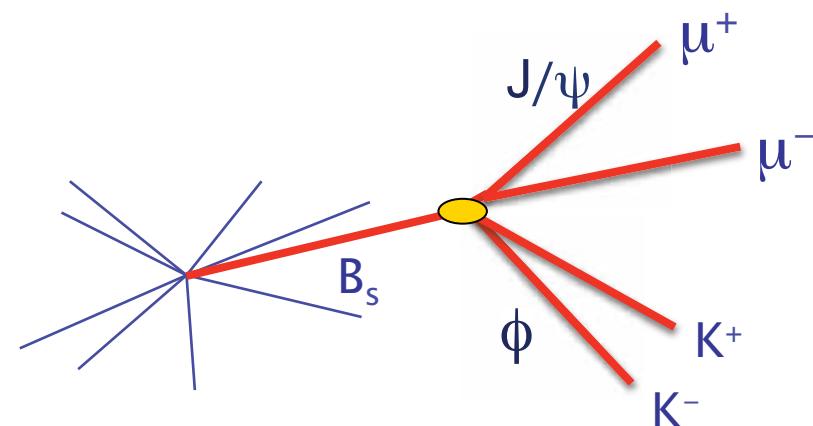
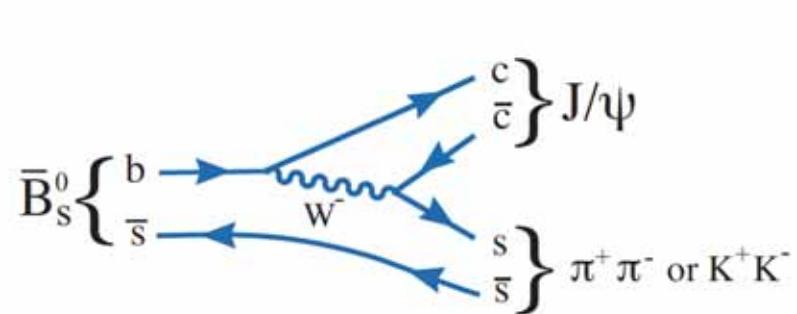
$$\phi_s = \phi_s^{\text{SM}} + \phi_s^{\text{NP}}$$

1] The term  $\phi_s$  is overloaded. It is also used for  $\text{Arg}(M_{12}/\Gamma_{12})$

2]  $\phi_s = -2 \arg(V_{ts} V_{tb}^* / V_{cs} V_{cb}^*)$

## The signals

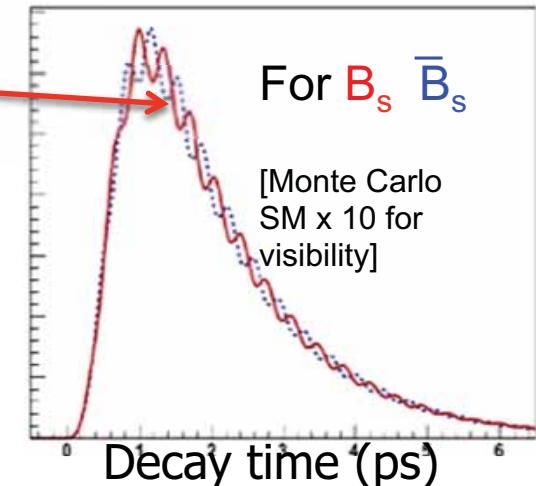
- $B_s \rightarrow J/\psi \Phi$  and  $B_s \rightarrow J/\psi \pi\pi$  are very clean decays



- Straightforward differential decay rates for  $B_s \rightarrow J/\psi \pi\pi$  :

$$\Gamma(B_s^0 \rightarrow J/\psi f_0) = \mathcal{N}_f e^{-\Gamma_s t} \left\{ e^{\Delta\Gamma_s t/2} (1 + \cos \phi_s) + e^{-\Delta\Gamma_s t/2} (1 - \cos \phi_s) - \sin(\phi_s) \sin(\Delta m_s t) \right\},$$

$$\Gamma(\bar{B}_s^0 \rightarrow J/\psi f_0) = \mathcal{N}_f e^{-\Gamma_s t} \left\{ e^{\Delta\Gamma_s t/2} (1 + \cos \phi_s) + e^{-\Delta\Gamma_s t/2} (1 - \cos \phi_s) + \sin(\phi_s) \sin(\Delta m_s t) \right\}.$$

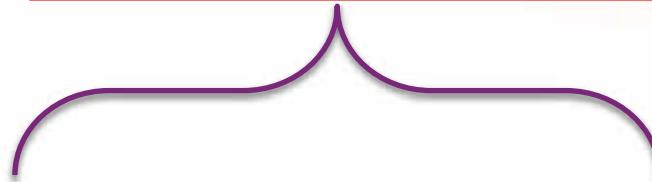


- Signal is sinusoidal time distribution
  - Amplitude proportional to  $\sin(\phi_s)$
  - Opposite sign for  $B$  and  $\bar{B}$  ➔ must tag
  - Diluted by wrong tagging probability  $\omega_{tag}$
  - Diluted by detector resolution  $\sigma_t$

- Fundamentally we measure:  $\sin(\phi_s) \times D(\sigma_t) \times (1 - 2\omega_{tag}) \times \sin(\Delta m_s t)$

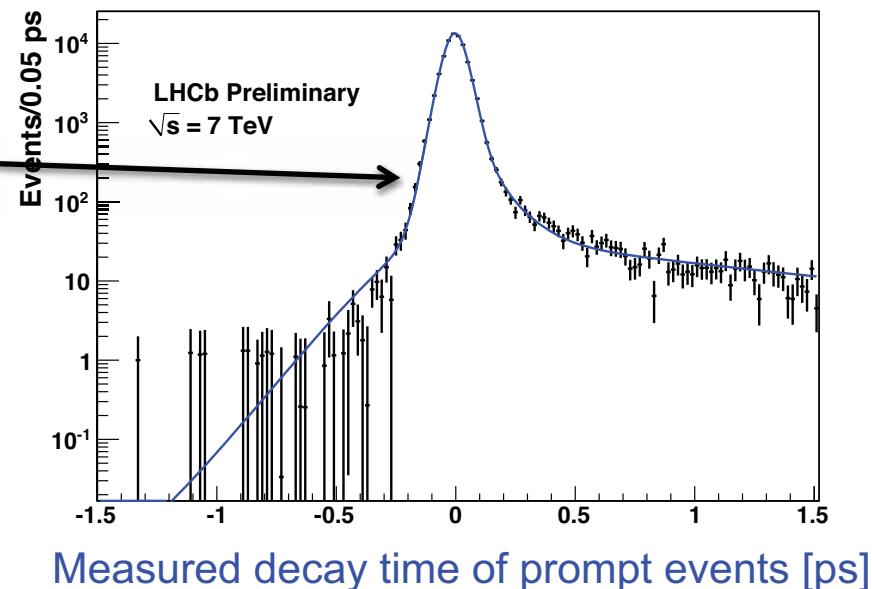
# Decay time resolution

$$\sin(\phi_s) \times D(\sigma_t) \times (1 - 2\omega_{tag}) \times \sin(\Delta m_s t)$$



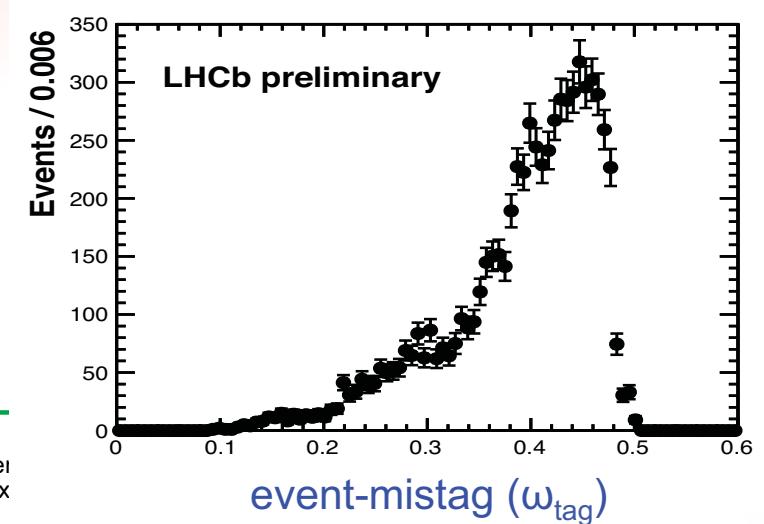
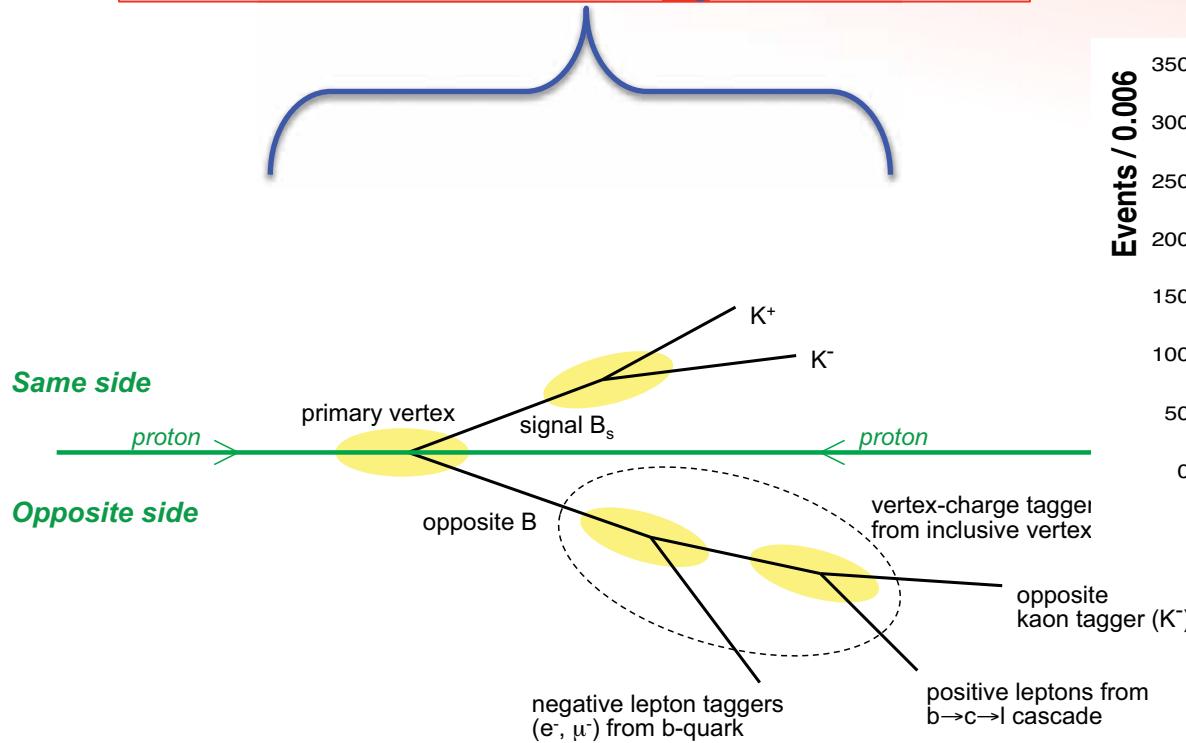
Need good proper time resolution w.r.t. sinusoid period  $\sim 350\text{fs}$

- We measure from data using prompt  $J/\psi$  which decay at  $t=0$
- width  $\sim 45\text{fs}$
- In analysis we actually use a resolution estimated per-event



# Need to tag B or $\bar{B}$ at production

$$\sin(\phi_s) \times D(\sigma_t) \times (1 - 2\omega_{tag}) \times \sin(\Delta m_s t)$$



tagging efficiency  $\epsilon_{tag} \sim 33\%$   
 effective mistag  $\omega_{tag} \sim 36.8\%$   
 effective tagging power  $\epsilon_{tag}(1 - 2\omega_{tag})^2 \sim 2.3\%$

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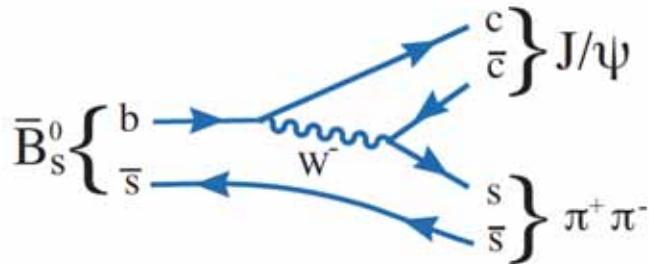
## Measurements of $\phi_s$ using $B_s \rightarrow J/\psi \pi\pi$

$\sim 1.0 \text{ fb}^{-1}$

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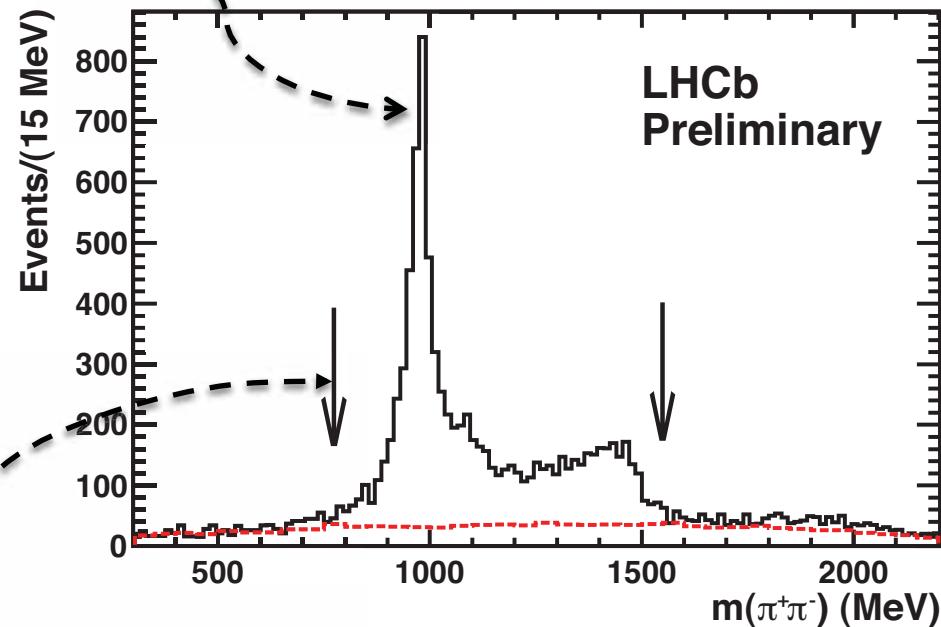
$\sim 0.41 \text{ fb}^{-1}$  published result: Phys. Lett. B707 (2012) 497, arXiv:1112.3056.

This update : LHCb-PAPER-2012-006



$B_s \rightarrow J/\psi \pi\pi$

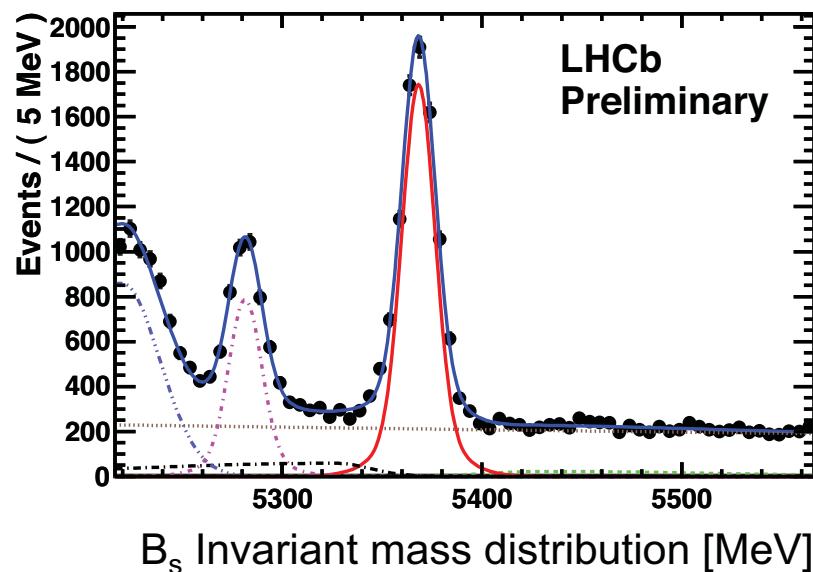
- Previous analysis was  $B_s \rightarrow J/\psi f_0(980)$



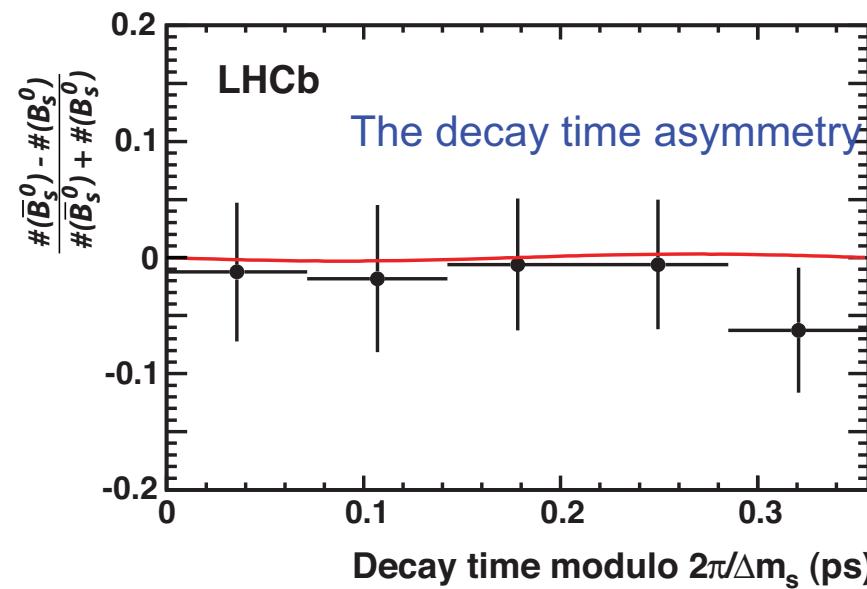
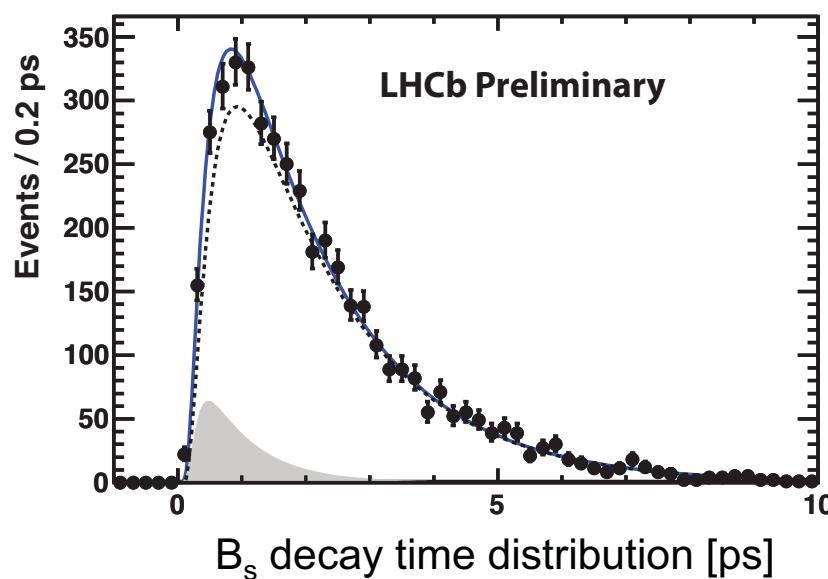
- All  $m(\pi\pi)$  range found to be CP-odd  
(97.7% @ 95% C.L.)  
[LHCb-PAPER-2012-005]

- Now use wider  $M(\pi\pi)$  range hence:  $B_s \rightarrow J/\psi \pi\pi$

# $B_s \rightarrow J/\psi \pi\pi$ signal



- Boosted Decision Tree selection
- Maximum likelihood fit to time and mass
- Uses  $\Gamma_s$  and  $\Delta\Gamma_s$  from the  $B_s \rightarrow J/\psi\Phi$  analysis (+correlation)
- Approx. 7400 signal events



# $B_s \rightarrow J/\psi \pi\pi$ final result

$$\phi_s = -0.02 \pm 0.17(\text{stat.}) \pm 0.02(\text{syst.}) \text{ rad.}$$

Quantity (Q)	$\pm \Delta Q$	+Change in $\phi_s$ (rad)	-Change in $\phi_s$ (rad)
$\beta$	$4.4 \times 10^{-3}$	0.0008	-0.0007
$\tau_{\text{bkg}_1}$ (ps)	0.046	-0.0006	0.0014
$\tau_{\text{bkg}_2}$ (ps)	0.8	-0.0014	0.0014
$f_2$	0.02	-0.0006	0.0012
$N_{\text{bkg}}$	38	0.0009	-0.0001
$N_{\eta'}$	9	0.0006	0.0001
$N_{\text{sig}}$	105	0.0021	0.0006
$m_0$ (MeV)	0.12	0.0012	-0.0004
$\sigma_1^m$ (MeV)	0.1	-0.0002	0.0008
$\alpha$	$1.1 \times 10^{-4}$	0.0003	0.0003
$T$ function	5%	0.0005	0.0005
$CP$ -even	increase mistag by 2.3%	-0.0160	0
Direct $CP$	free in fit	-0.0020	0
Total systematic error on $\phi_s$		${}^{+0.004}_{-0.017}$	

## Systematic errors

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## Measurements of $\phi_s$ using $B_s \rightarrow J/\psi\Phi$

$\sim 1.0 \text{ fb}^{-1}$

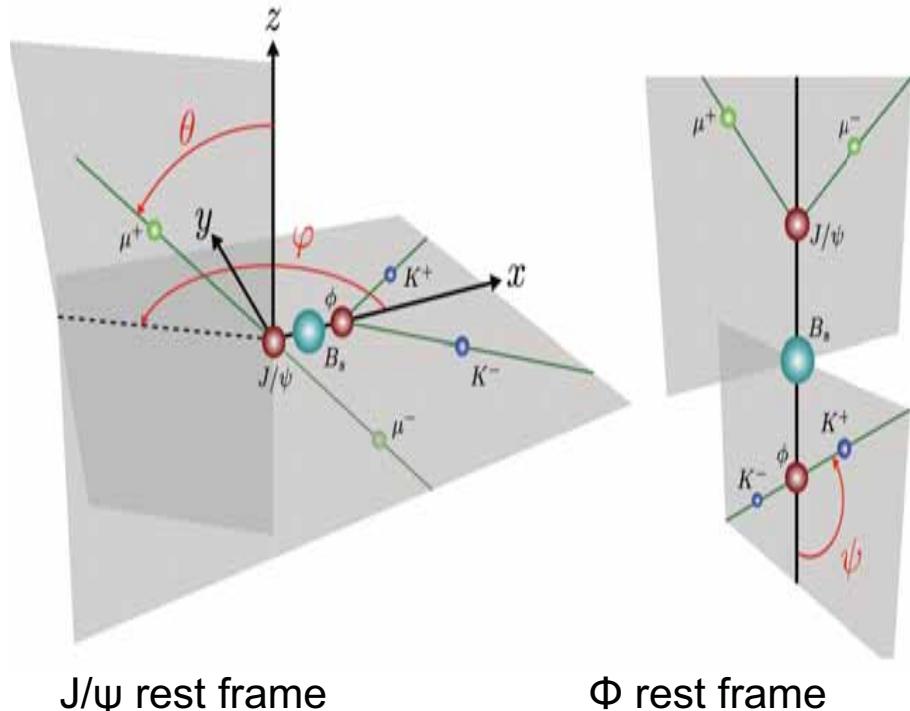
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0.37  $\text{fb}^{-1}$  published result: arXiv:1112.3183 [LHCb-PAPER-2011-021]

This update: LHCb-CONF-2012-002

# $B_s \rightarrow J/\psi \Phi$ analysis

- Decay to CP-odd and CP-even final states,  
→ need analysis of decay angle distribution



- Much larger branching fraction

$$J/\psi \Phi / J/\psi \pi\pi \sim 5$$

- Differential cross section is “very rich”
  - 3 “P-wave” amplitudes of KK system
  - 1 “S”-wave amplitude
  - 10 terms with all interferences

- ..but fundamentally for  $\phi_s$  we still measure:

$$\sin(\phi_s) \times D(\sigma_t) \times (1 - 2\omega_{tag}) \times \sin(\Delta m_s t)$$

- ..and because we separate the terms, we measure the lifetimes of Heavy and Light eigenstates separately:

$$\Gamma_L \text{ & } \Gamma_H \Leftrightarrow \Gamma_s \text{ & } \Delta\Gamma_s$$

- There is a two fold ambiguity in the solutions

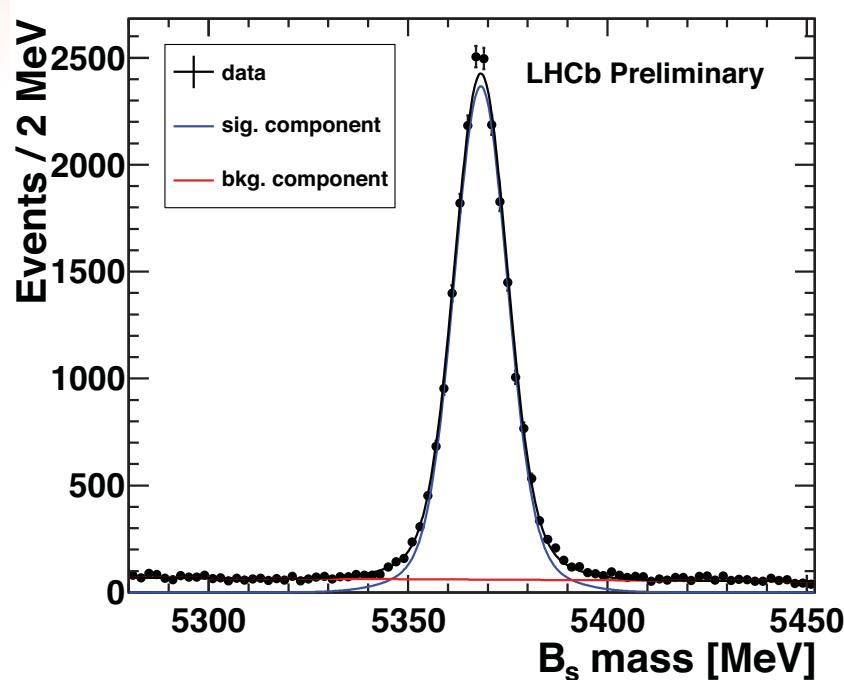
$$\phi_s \Leftrightarrow \pi - \phi_s$$

$$\Delta\Gamma_s \Leftrightarrow -\Delta\Gamma_s$$

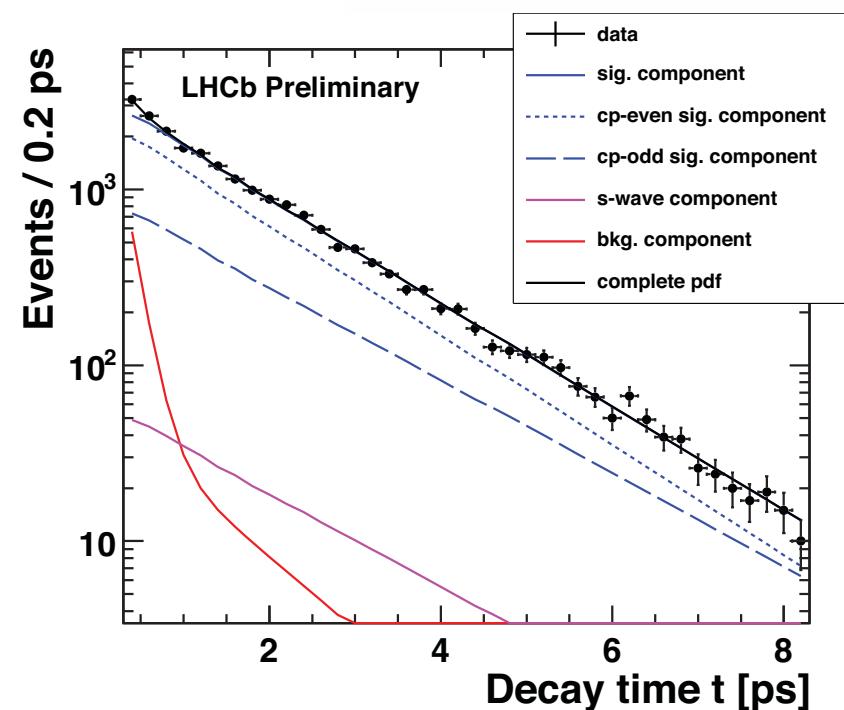
+ strong phase changes

$$\begin{aligned}
 A_1 &= |A_0|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta mt)] \\
 A_2 &= |A_\parallel|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta mt)] \\
 A_3 &= |A_\perp|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta mt)] \\
 A_4 &= |A_\parallel||A_\perp| e^{-\Gamma_s t} [-\cos(\delta_\perp - \delta_\parallel) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \cos(\delta_\perp - \delta_\parallel) \cos\phi_s \sin(\Delta mt) \\
 &\quad + \sin(\delta_\perp - \delta_\parallel) \cos(\Delta mt)] \\
 A_5 &= |A_0||A_\parallel| e^{-\Gamma_s t} \cos(\delta_\parallel - \delta_0) [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta mt)] \\
 A_6 &= |A_0||A_\perp| e^{-\Gamma_s t} [-\cos(\delta_\perp - \delta_0) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \cos(\delta_\perp - \delta_0) \cos\phi_s \sin(\Delta mt) \\
 &\quad + \sin(\delta_\perp - \delta_0) \cos(\Delta mt)] \\
 A_7 &= |A_s|^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta mt)] \\
 A_8 &= |A_s||A_\parallel| e^{-\Gamma_s t} [-\sin(\delta_\parallel - \delta_S) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_\parallel - \delta_S) \cos\phi_s \sin(\Delta mt) \\
 &\quad + \cos(\delta_\parallel - \delta_S) \cos(\Delta mt)] \\
 A_9 &= |A_s||A_\perp| e^{-\Gamma_s t} \sin(\delta_\perp - \delta_S) [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta mt)] \\
 A_{10} &= |A_s||A_0| e^{-\Gamma_s t} [-\sin(\delta_0 - \delta_S) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_0 - \delta_S) \cos\phi_s \sin(\Delta mt) \\
 &\quad + \cos(\delta_0 - \delta_S) \cos(\Delta mt)]
 \end{aligned}$$

# $B_s \rightarrow J/\psi\Phi$ signal

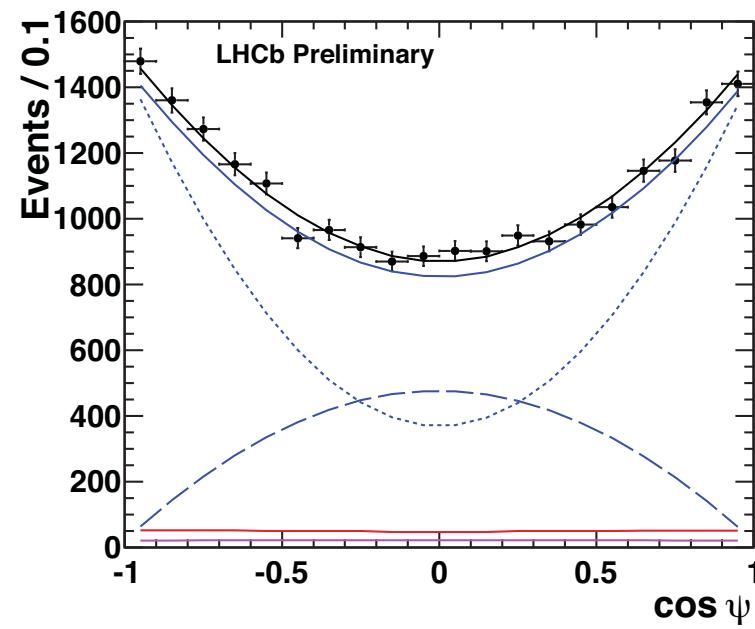
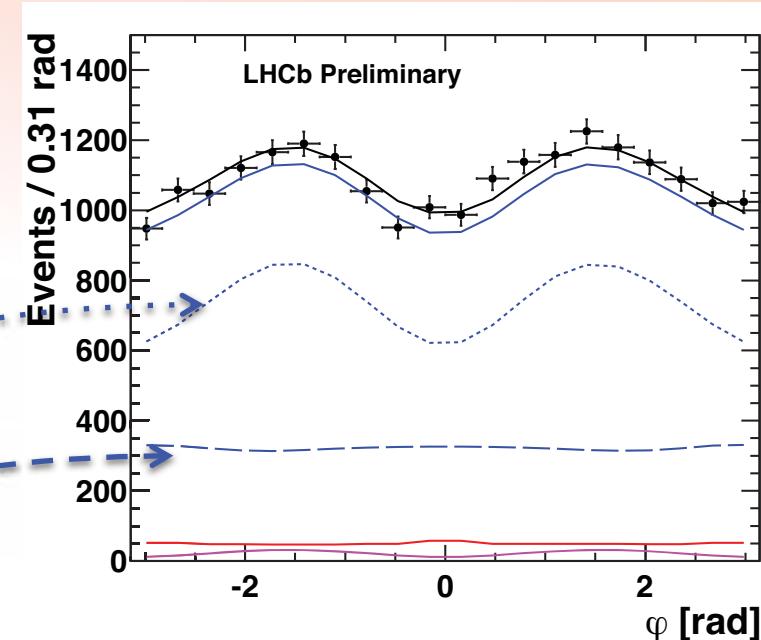
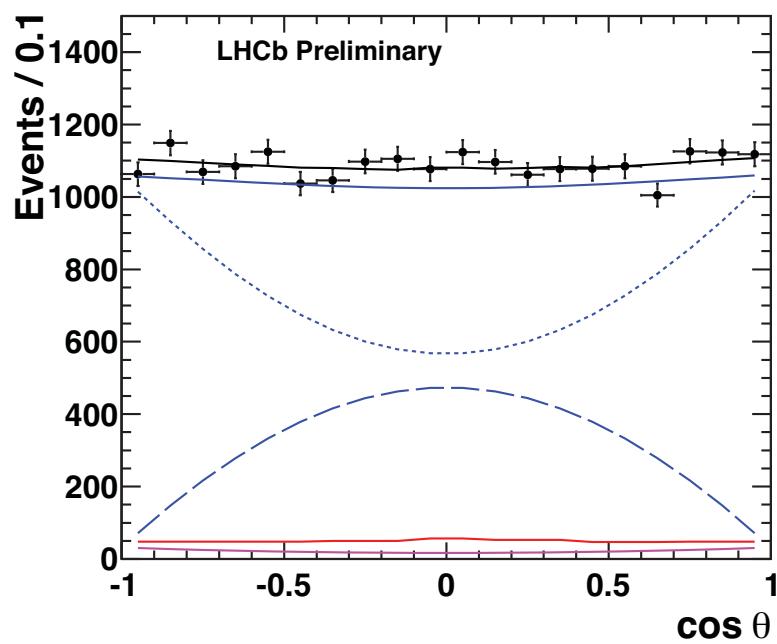


- Simple selection with kinematic cuts
- Most background removed by decay time cut  $t > 0.3$  ps
- Very clean signal
- Approx. 21200 signal events



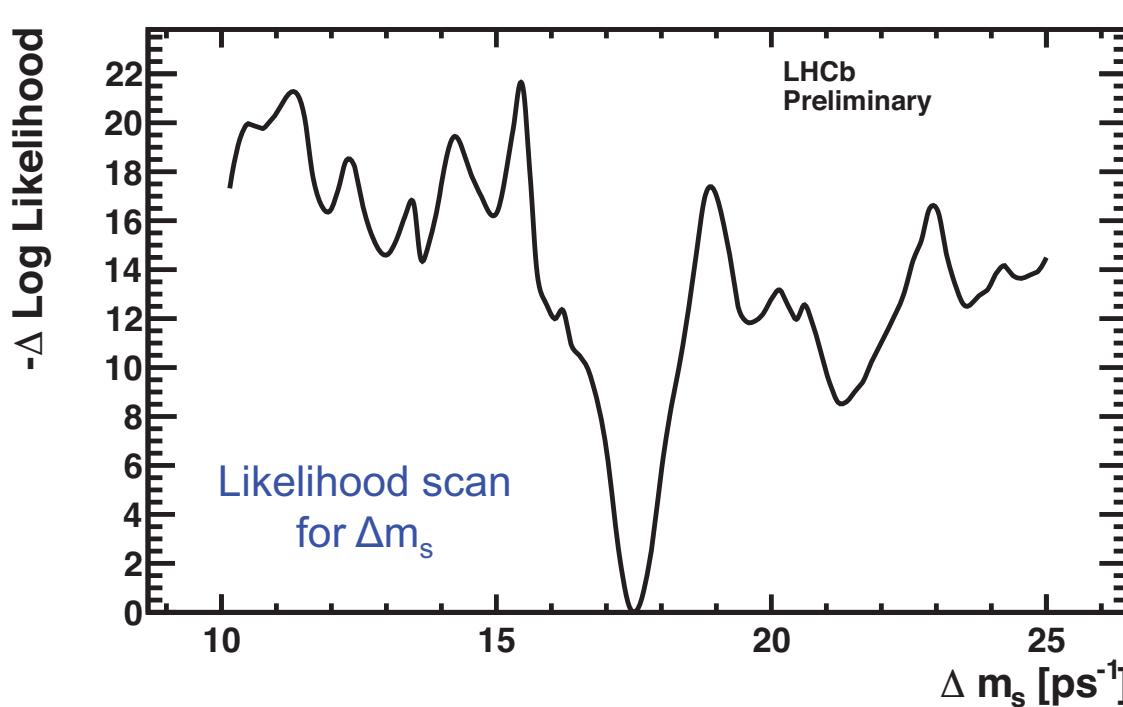
# $B_s \rightarrow J/\psi\Phi$ decay angle distributions

- The CP-even / CP-odd separation is very clear in all distributions.



## Digression: measurement of $\Delta m_s$

- The data has sinusoidal terms which measure  $\Delta m_s$  independently of  $\phi_s$



- We observe a central value  $\Delta m_s = 17.50 \pm 0.15 \text{ (stat)} \text{ ps}^{-1}$ 
  - Compare to LHCb published measurement  $17.63 \pm 0.11 \pm 0.02$  arXiv:1112.4311
  - This gives confidence that if there is a  $\sin(\phi_s) \times \sin(\Delta m_s t)$  term we would see it.

# $B_s \rightarrow J/\psi\Phi$ : New Preliminary Results

- Maximum likelihood fit to signal + background time, angle and mass distributions.
- Constrain  $\Delta m_s$  to  $17.63 \pm 0.11$  ps
- “Solution-I” shown here

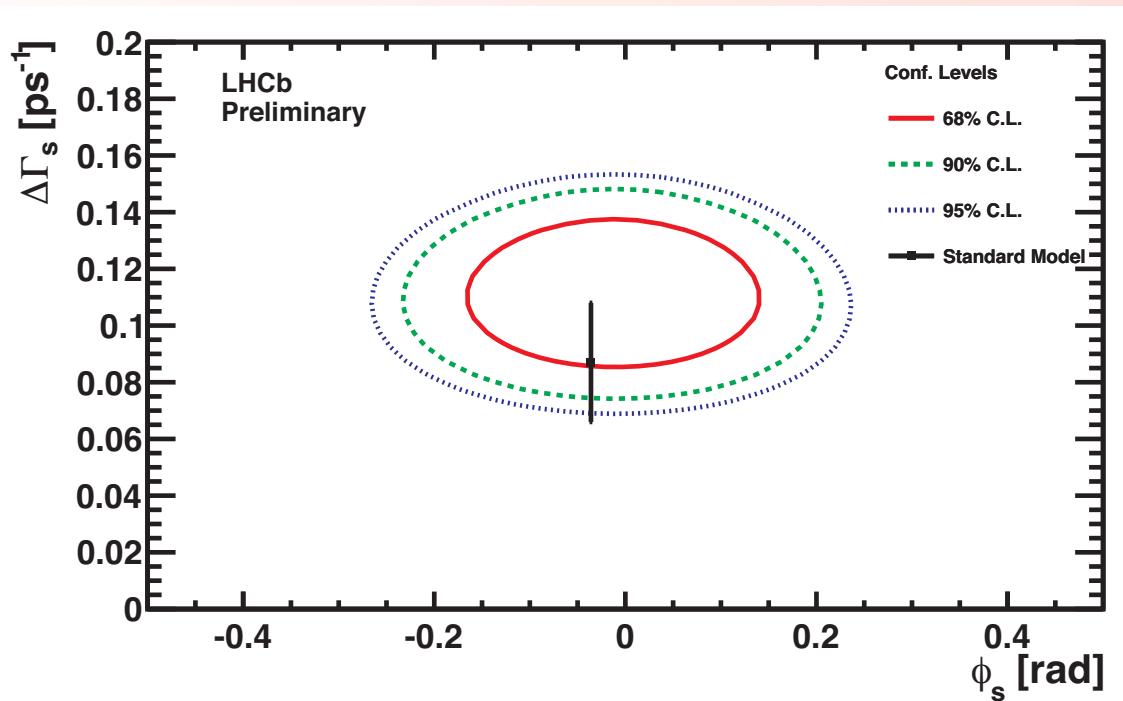
Parameter	Value	Stat.	Syst.
$\Gamma_s$ [ps $^{-1}$ ]	0.6580	0.0054	0.0066
$\Delta\Gamma_s$ [ps $^{-1}$ ]	0.116	0.018	0.006
$ A_\perp(0) ^2$	0.246	0.010	0.013
$ A_0(0) ^2$	0.523	0.007	0.024
$F_S$	0.022	0.012	0.007
$\delta_\perp$ [rad]	2.90	0.36	0.07
$\delta_\parallel$ [rad]	[2.81, 3.47]		0.13
$\delta_s$ [rad]	2.90	0.36	0.08
$\phi_s$ [rad]	-0.001	0.101	0.027

- $\phi_s$  uncorrelated with other quantities

	$\Gamma_s$	$\Delta\Gamma_s$	$ A_\perp ^2$	$ A_0 ^2$	$\phi_s$
$\Gamma_s$	1.00	-0.38	0.39	0.20	-0.01
$\Delta\Gamma_s$		1.00	-0.67	0.63	-0.01
$ A_\perp(0) ^2$			1.00	-0.53	-0.01
$ A_0(0) ^2$				1.00	-0.02
$\phi_s$					1.00

# $B_s \rightarrow J/\psi\Phi$ : New Preliminary Results $1.0 \text{ fb}^{-1}$

Contour for  
 $\phi_s - \Delta\Gamma_s$



$$\Gamma_s = 0.6580 \pm 0.0054(\text{stat.}) \pm 0.0066(\text{syst.}) \text{ ps}^{-1}$$

$$\Delta\Gamma_s = 0.116 \pm 0.018(\text{stat.}) \pm 0.006(\text{syst.}) \text{ ps}^{-1}$$

$$\phi_s = -0.001 \pm 0.101(\text{stat.}) \pm 0.027(\text{syst.}) \text{ rad}$$

# Systematics

Source	$\Gamma_s$ [ps $^{-1}$ ]	$\Delta\Gamma_s$ [ps $^{-1}$ ]	$A_{\perp}^2$	$A_0^2$	$F_S$	$\delta_{\parallel}$ [rad]	$\delta_{\perp}$ [rad]	$\delta_s$ [rad]	$\phi_s$ [rad]
Description of background	0.0010	0.004	-	0.002	0.005	0.04	0.04	0.06	0.011
Angular acceptances	0.0018	0.002	0.012	0.024	0.005	0.12	0.06	0.05	0.012
$t$ acceptance model	0.0062	0.002	0.001	0.001	-	-	-	-	-
$z$ and momentum scale	0.0009	-	-	-	-	-	-	-	-
Production asymmetry ( $\pm 10\%$ )	0.0002	0.002	-	-	-	-	-	-	0.008
CPV mixing & decay ( $\pm 5\%$ )	0.0003	0.002	-	-	-	-	-	-	0.020
Fit bias	-	0.001	0.003	-	0.001	0.02	0.02	0.01	0.005
Quadratic sum	0.0066	0.006	0.013	0.024	0.007	0.13	0.07	0.08	0.027

- Note: Tagging and resolution parameters floated in fit within uncertainties, hence not explicitly included in systematics

# $B_s \rightarrow J/\psi\Phi$ and $B_s \rightarrow J/\psi\pi\pi$ combined prelim.result

- ❑ Used a simultaneous fit to both datasets, taking all common parameters and correlations into account.
- ❑ Used largest syst. error.

$$\phi_s = -0.002 \pm 0.083(\text{stat.}) \pm 0.027(\text{syst.}) \text{ rad}$$

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## Resolving the ambiguous solution

The sign of  $\Delta\Gamma_s$

$\sim 0.37 \text{ fb}^{-1}$

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LHCb-PAPER-2012-28, submitted PRL, [arXiv:1202.4717v2](https://arxiv.org/abs/1202.4717v2)

- There are two ambiguous solutions related by  $\phi_s \Leftrightarrow \pi - \phi_s$  and  $\Delta\Gamma \Leftrightarrow -\Delta\Gamma$
- We can disambiguate using the P-Wave  $\Leftrightarrow$  S-Wave interference

[Y. Xie et al., JHEP 0909:074, 2009]

Similar to Babar measurement of sign of  $\cos(2\beta)$ , PRD 71, 032005 (2007)

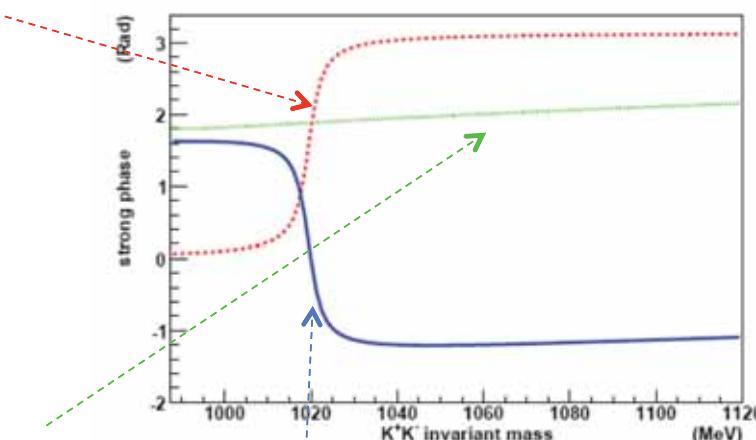
### **K<sup>+</sup>K<sup>-</sup> P-wave:**

Phase of Breit-Wigner amplitude increases rapidly across  $\phi(1020)$  mass region

$$BW(m_{KK}) = \frac{F_r F_D}{m_\phi^2 - m_{KK}^2 - im_\phi \Gamma(m_{KK})}$$

### **K<sup>+</sup>K<sup>-</sup> S-wave:**

Phase of Flatté amplitude for  $f_0(980)$  relatively flat (similar for non-resonance)



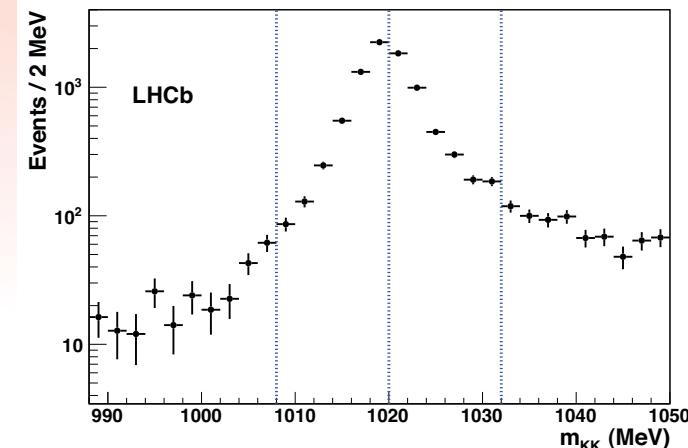
### **Phase difference between S- and P-wave amplitudes**

Decreases rapidly across  $\phi(1020)$  mass region

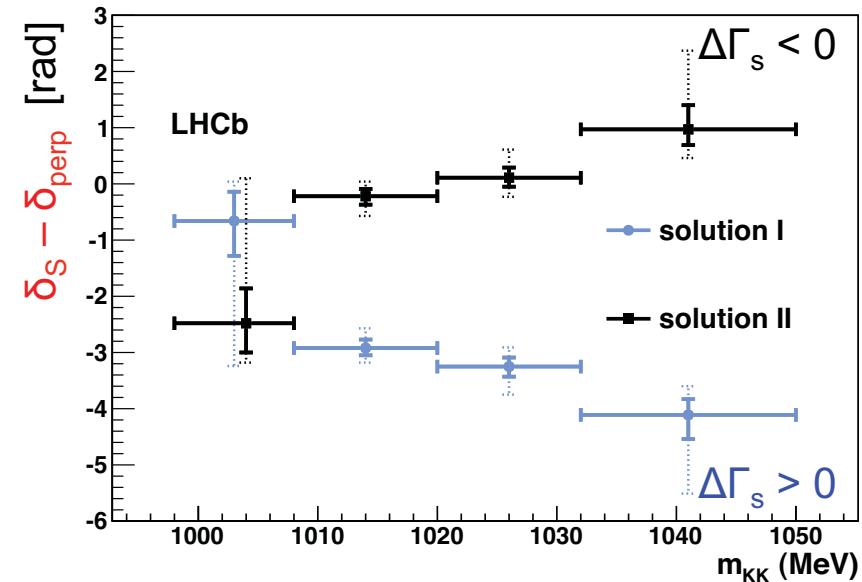
**Resolution method:** choose the solution with decreasing trend of  $\delta_s - \delta_P$  vs  $m_{KK}$  in the  $\phi(1020)$  mass region

□ Split data into 4 bins of  $m_{KK}$

- In each bin measure
- Fraction of S-wave
  - Measure relative strong phase difference  $\delta_s - \delta_{\text{perp}}$



Parameter	Solution I	Solution II
$\phi_s$ (rad)	$0.167 \pm 0.175$	$2.975 \pm 0.175$
$\Delta\Gamma$ (ps <sup>-1</sup> )	$0.120 \pm 0.028$	$-0.120 \pm 0.028$
$F_{S;1}$	$0.283 \pm 0.113$	$0.283 \pm 0.113$
$F_{S;2}$	$0.061 \pm 0.022$	$0.061 \pm 0.022$
$F_{S;3}$	$0.044 \pm 0.022$	$0.044 \pm 0.022$
$F_{S;4}$	$0.269 \pm 0.067$	$0.269 \pm 0.067$
$\delta_{S\perp;1}$ (rad)	$-0.46^{+0.35}_{-0.42}$	$-2.68^{+0.42}_{-0.35}$
$\delta_{S\perp;2}$ (rad)	$-2.92^{+0.15}_{-0.13}$	$-0.22^{+0.13}_{-0.15}$
$\delta_{S\perp;3}$ (rad)	$-3.25^{+0.16}_{-0.18}$	$0.11^{+0.18}_{-0.16}$
$\delta_{S\perp;4}$ (rad)	$-4.11^{+0.28}_{-0.43}$	$0.97^{+0.43}_{-0.28}$

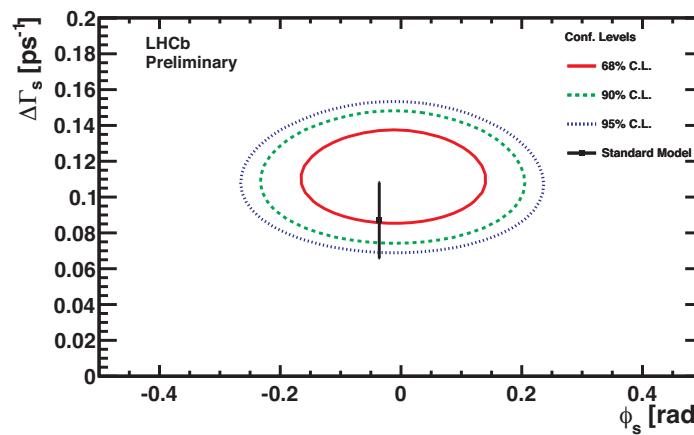


Solution-I is selected [4.7 $\sigma$  from being flat]

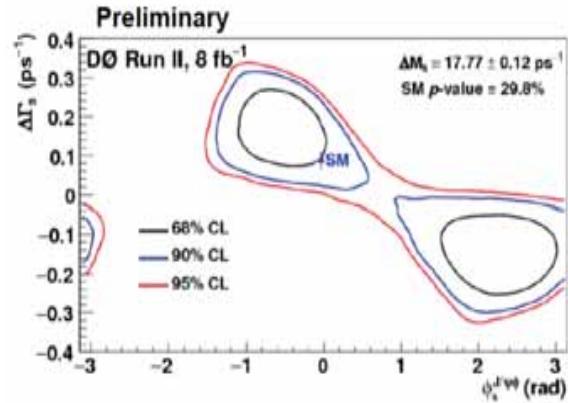
$$\Delta\Gamma_s > 0$$

# LHC + Tevatron Results

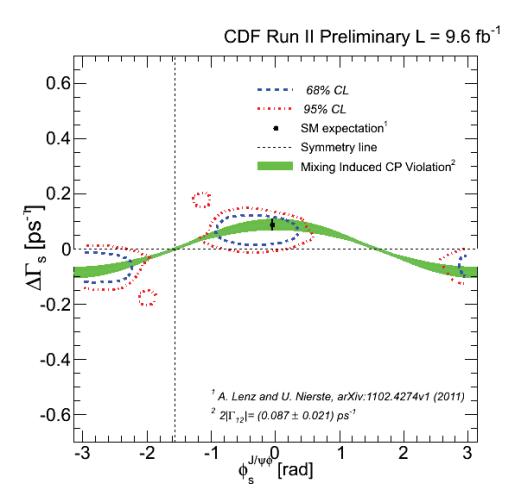
This result  $1 \text{ fb}^{-1}$



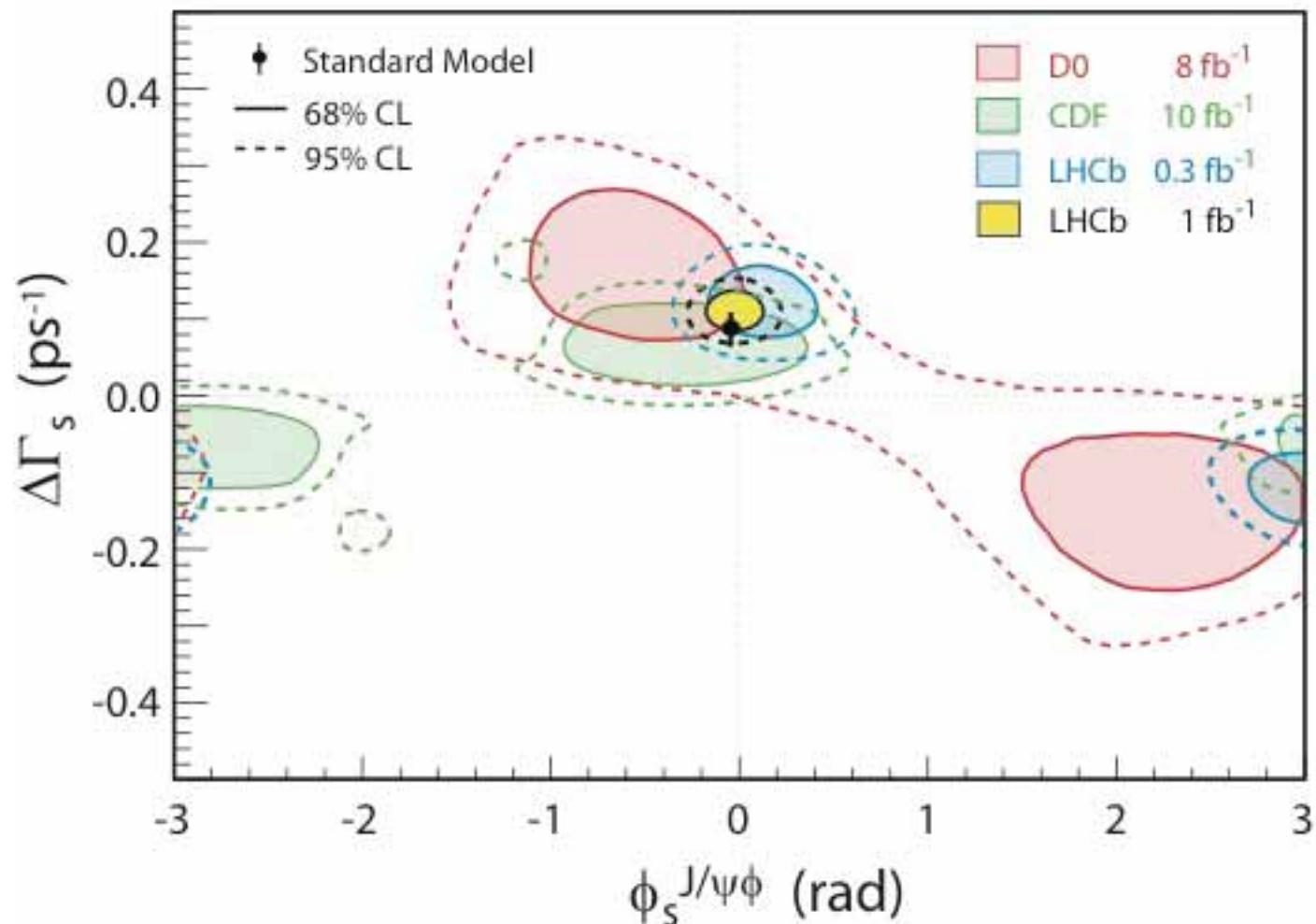
D0  $8 \text{ fb}^{-1}$  [S.Burin, EPS 2011]



CDF  $10 \text{ fb}^{-1}$  [Sabato Leo talk, Lake Louise]



# Pictorial overlay - winter 2012



# Conclusion

□ LHCb has presented new preliminary results using the full 2011 data ( $1 \text{ fb}^{-1}$ )

□ From an analysis of the  $\text{J}/\psi\phi$  channel we find:

$$\Gamma_s = 0.6580 \pm 0.0054(\text{stat.}) \pm 0.0066(\text{syst.}) \text{ ps}^{-1}$$

$$\Delta\Gamma_s = 0.116 \pm 0.018(\text{stat.}) \pm 0.006(\text{syst.}) \text{ ps}^{-1}$$

$$\phi_s = -0.001 \pm 0.101(\text{stat.}) \pm 0.027(\text{syst.}) \text{ rad.}$$

□ From an analysis of the  $\text{J}/\psi\pi\pi$  channel we find:

$$\phi_s = -0.02 \pm 0.17(\text{stat.}) \pm 0.02(\text{syst.}) \text{ rad}$$

□ Combining both results we find:

$$\phi_s = -0.002 \pm 0.083(\text{stat.}) \pm 0.027(\text{syst.}) \text{ rad.}$$

□ We resolve the 2-fold ambiguity and find:  $\Delta\Gamma_s > 0$

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## Extra Information

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# $B_s \rightarrow J/\psi \pi\pi$ analysis:

## 1. CP-odd fraction: Table from LHCb-PAPER-2012-006

Table 1: Fit fractions of contributing resonances [16]. The final state helicity of the D-wave is denoted by  $\Lambda$ . Only statistical errors are quoted.

Resonance	Normalized fraction (%)
$f_0(980)$	$69.7 \pm 2.3$
$f_0(1370)$	$21.2 \pm 2.7$
non-resonant $\pi^+ \pi^-$	$8.4 \pm 1.5$
$f_2(1270), \Lambda = 0$	$0.49 \pm 0.16$
$f_2(1270), \Lambda =  1 $	$0.21 \pm 0.65$

- Upper limit on  $\rho(770)$  found to be 1.5% @ 95% C.L.
- Total is quadrature sum of  $f_2(1270) + \rho(770)$

## 2. Profile Likelihood

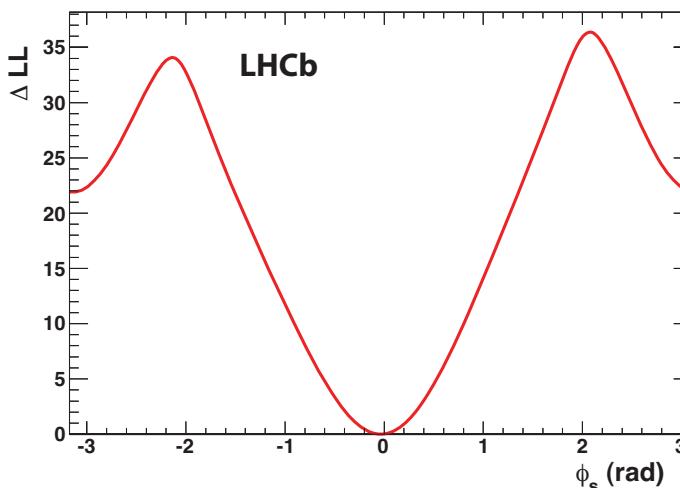
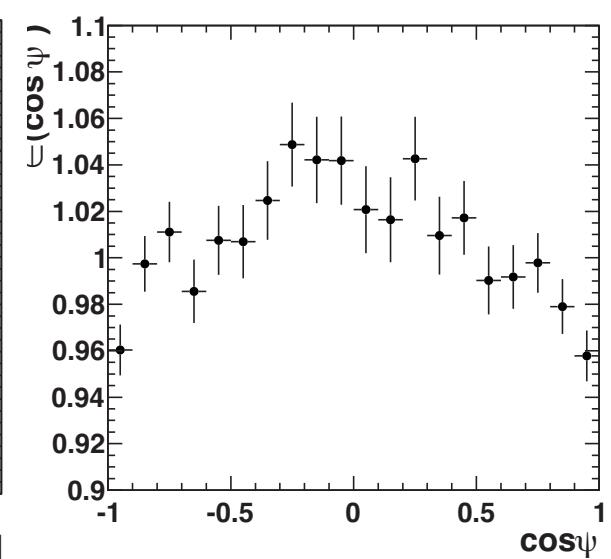
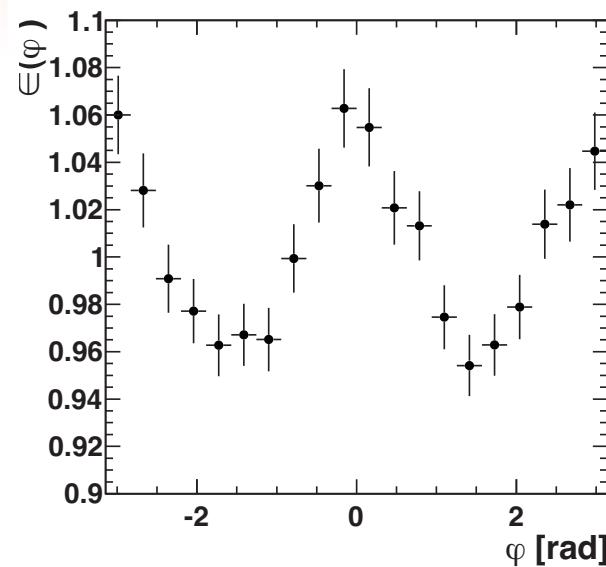
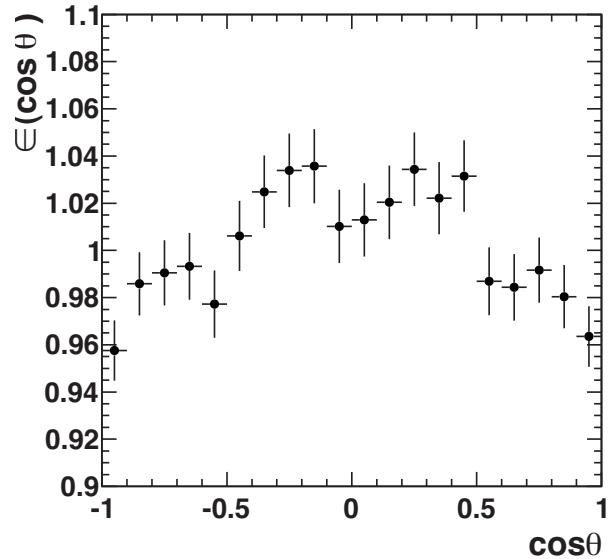


Figure 8: Log-likelihood difference as a function of  $\phi_s$  for  $\bar{B}_s^0 \rightarrow J/\psi f_{\text{odd}}$  events.

## Decay angle acceptances

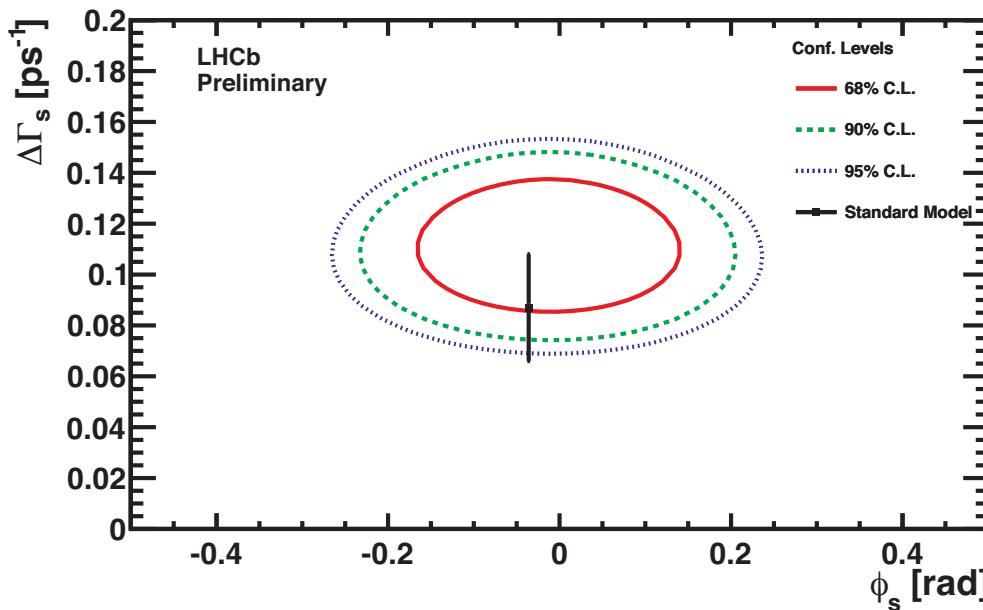


All acceptances  $\sim 5\%$  effects

Accounted for in ML fit

# $B_s \rightarrow J/\psi\Phi$ : New Preliminary Results

This new preliminary result  $1.0 \text{ fb}^{-1}$

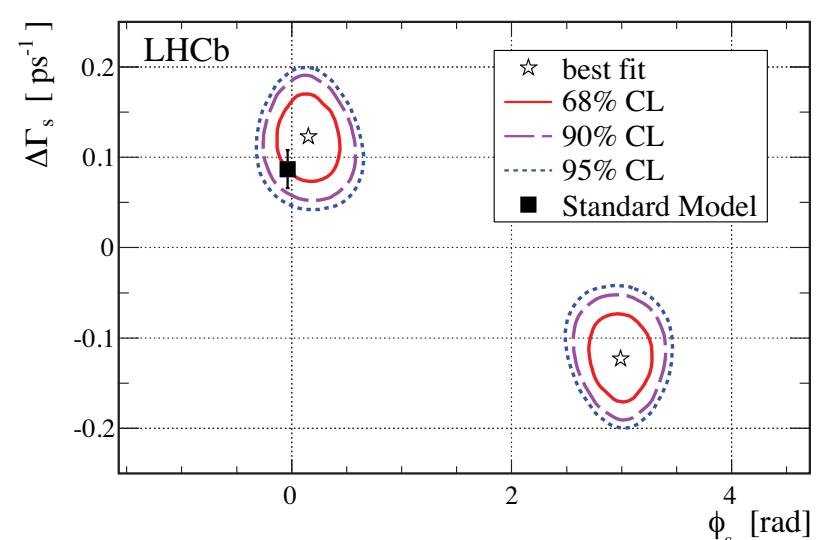


$$\Gamma_s = 0.6580 \pm 0.0054(\text{stat.}) \pm 0.0066(\text{syst.}) \text{ ps}^{-1}$$

$$\Delta\Gamma_s = 0.116 \pm 0.018(\text{stat.}) \pm 0.006(\text{syst.}) \text{ ps}^{-1}$$

$$\phi_s = -0.001 \pm 0.101(\text{stat.}) \pm 0.027(\text{syst.}) \text{ rad.}$$

Previous published result  $0.37 \text{ fb}^{-1}$   
arXiv:1112.3183



$$\Gamma_s = 0.657 \pm 0.009(\text{stat.}) \pm 0.008(\text{syst.}) \text{ ps}^{-1}$$

$$\Delta\Gamma_s = 0.123 \pm 0.029(\text{stat.}) \pm 0.011(\text{syst.}) \text{ ps}^{-1}$$

$$\phi_s = 0.151 \pm 0.18(\text{stat.}) \pm 0.06(\text{syst.}) \text{ rad.}$$

Syst error due to possible direct CVP

- We vary  $|\lambda|^2$  by 5%
- Motivated by a fit for  $|\lambda|^2$  gives < 5%

$$R(t, q) \propto e^{-\Gamma_s t} \left\{ \cosh \frac{\Delta \Gamma_s t}{2} + \frac{2|\lambda|}{1 + |\lambda|^2} \cos \phi_s \sinh \frac{\Delta \Gamma_s t}{2} - \frac{2qD}{1 + |\lambda|^2} [|\lambda| \sin \phi_s \sin(\Delta m_s t) + (1 - |\lambda|^2) \cos(\Delta m_s t)] \right\}.$$