

# Observation of gravitational waves from binary black-hole merger

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Coalescence of two black holes (credits: SXS)





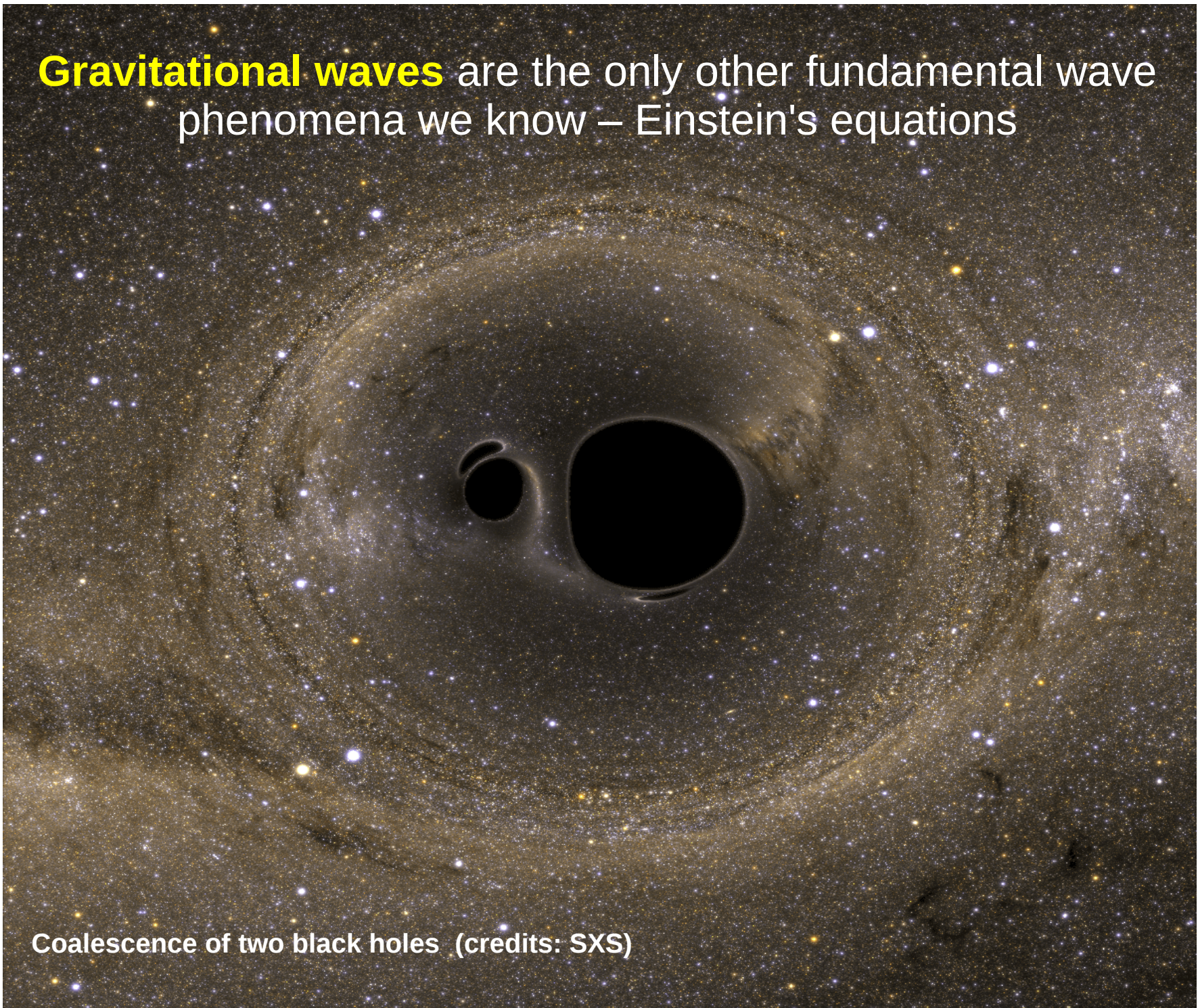


The only fundamental waves we have observed so far are **electromagnetic waves** – Maxwell's equations (light, radio, microwaves, gamma rays, x-rays)

So far, our **knowledge of the Universe** essentially comes from electromagnetic waves



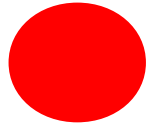
**Gravitational waves** are the only other fundamental wave phenomena we know – Einstein's equations



Coalescence of two black holes (credits: SXS)



# Outline



Primer on gravitational waves

Path to first detection: historical review

Interferometric detectors: from principles to sensitivity

Results from first aLIGO science run

Search summary

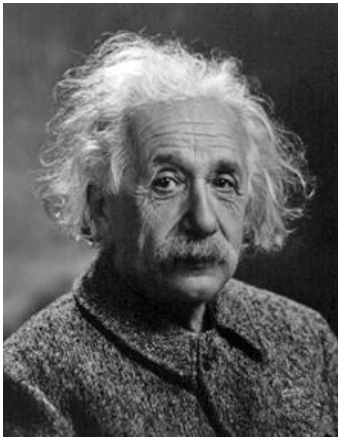
Science beyond detection

Multimessenger astronomy

Outlook



# Einstein's General relativity



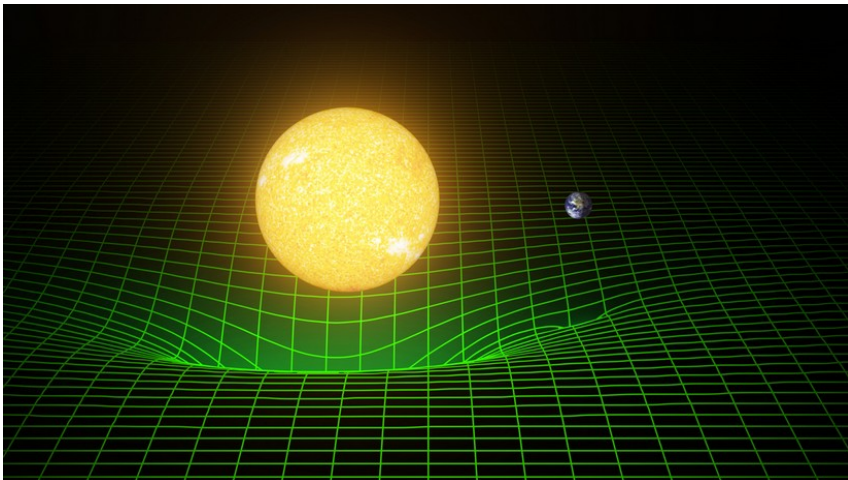
## General relativity – 1915

- Spacetime is a deformable and dynamic object
- Gravity describes as a **geometrical effect coming from spacetime curvature**
- Einstein's fields equations

Space-time  
geometry

$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Energy/  
Matter



*“spacetime tells matter how to move;  
matter tells spacetime how to curve”*

John Archibald Wheeler



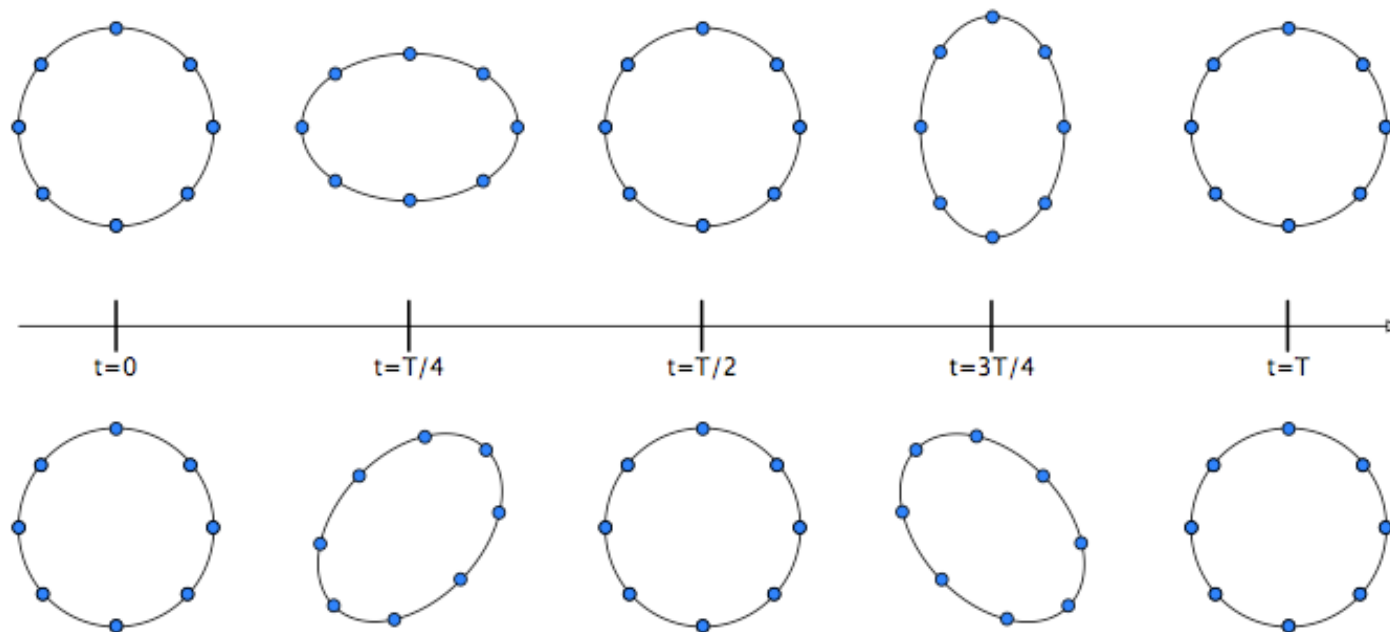
# Gravitational waves

- Linearization of Einstein equations

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu} \quad |h_{\mu\nu}| \ll 1 \quad \longrightarrow \quad \square \bar{h}_{\mu\nu} = 0$$

- **Propagating perturbations of space-time metric**

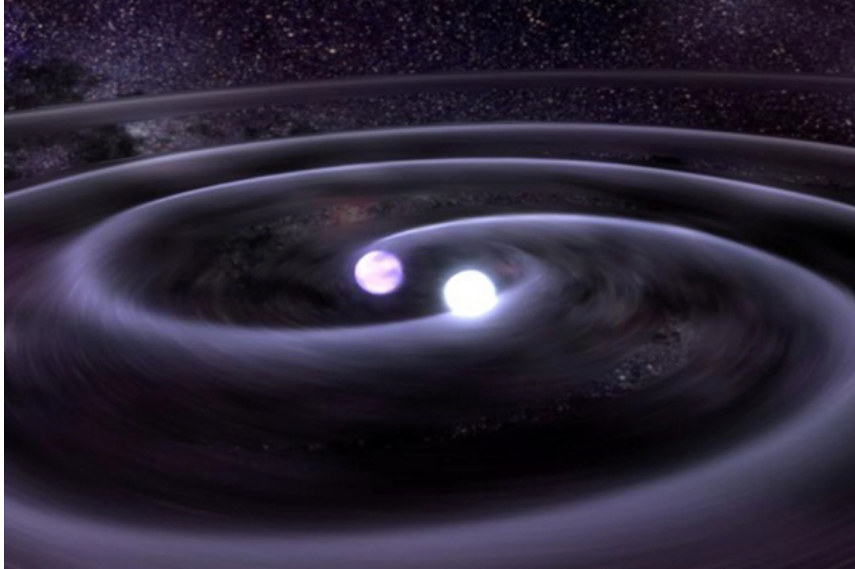
- Travel at the speed of light
- Transverse waves
- Two polarisations  $x$  and  $+$
- Dimensionless strain amplitude  $h$



$h \sim 0.5$   
in this illustration



# Gravitational waves

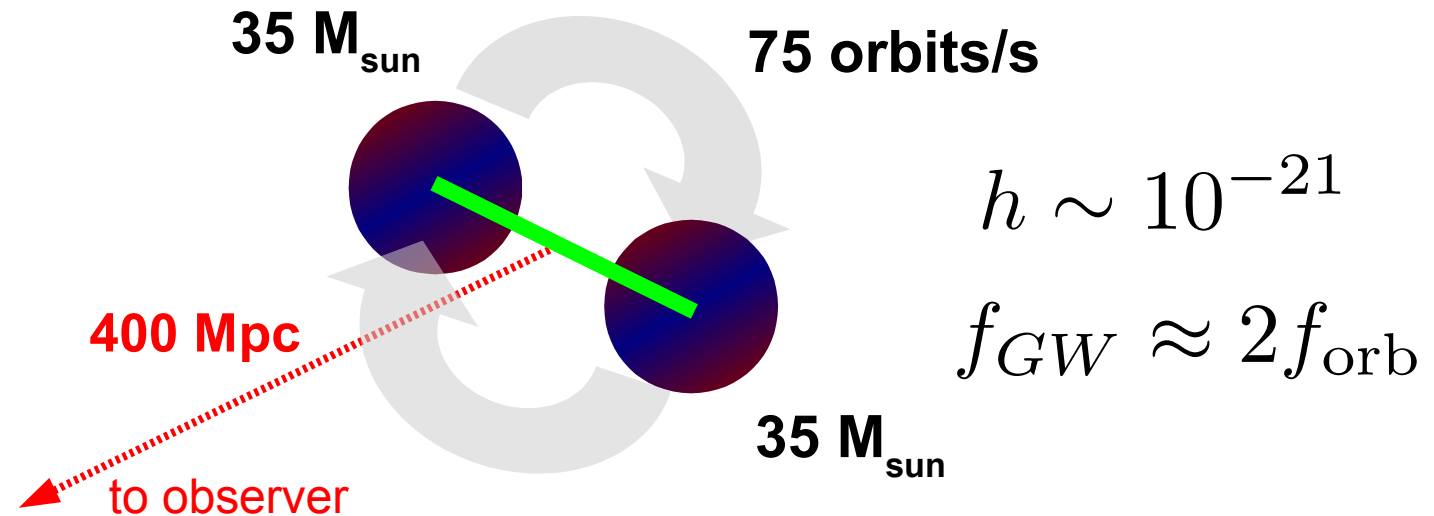


- Produced by **accelerated mass**
- Rapid changes in shape and orientation of massive systems
- Large masses, relativistic motion  
→ **astrophysical sources**
- Variation of the quadrupole  
→ Inspiralling binaries of black holes and neutron stars

Quadrupole formula

$$h \sim G/c^4 \ddot{Q}/d$$

$$c^4/G \sim 10^{44} N$$



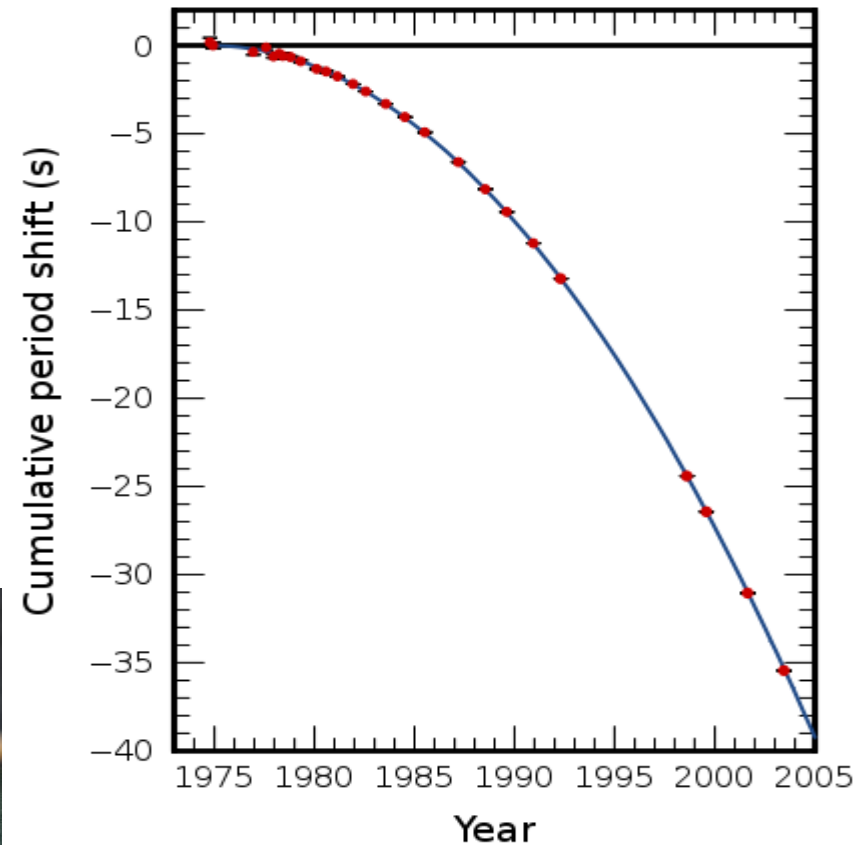
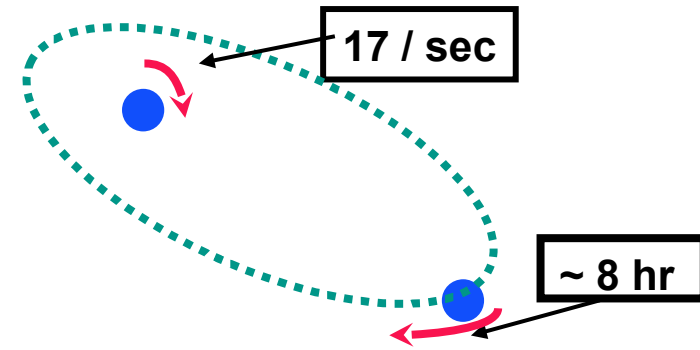


# Evidence of existence

- Binary pulsar PSR B1913+16
  - ◆ Orbital decay → energy loss due to GW
  - ◆ In agreement with GR to  $\sim 0.2\%$
  - ◆ Hulse & Taylor's Nobel prize 1993

« for the discovery of a new type of pulsar, a discovery that has opened up new possibilities for the study of gravitation »

Binary orbit will continue to decay over 300 millions years until coalescence



R Hulse



J Taylor



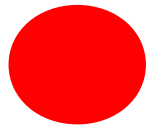
J Weisberg



T Damour

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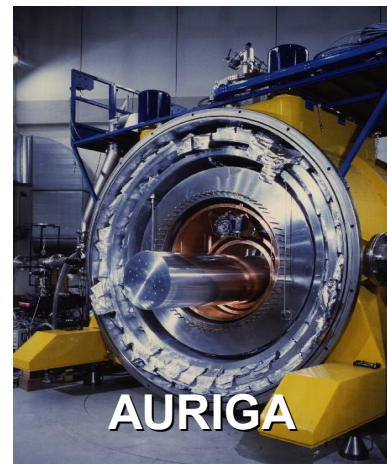
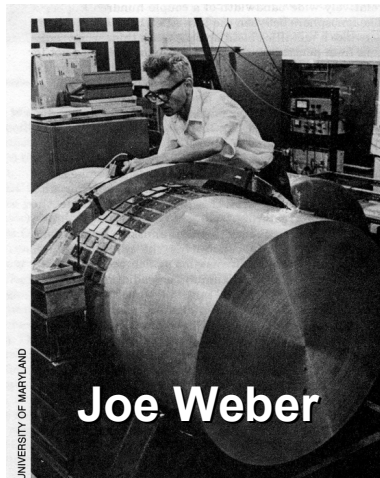
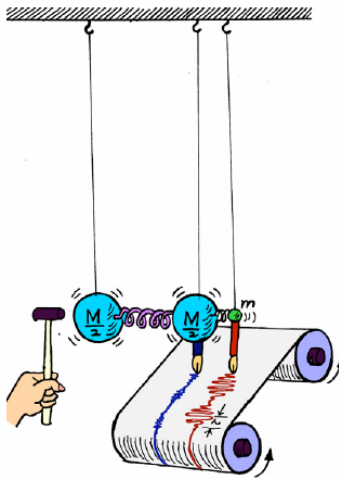
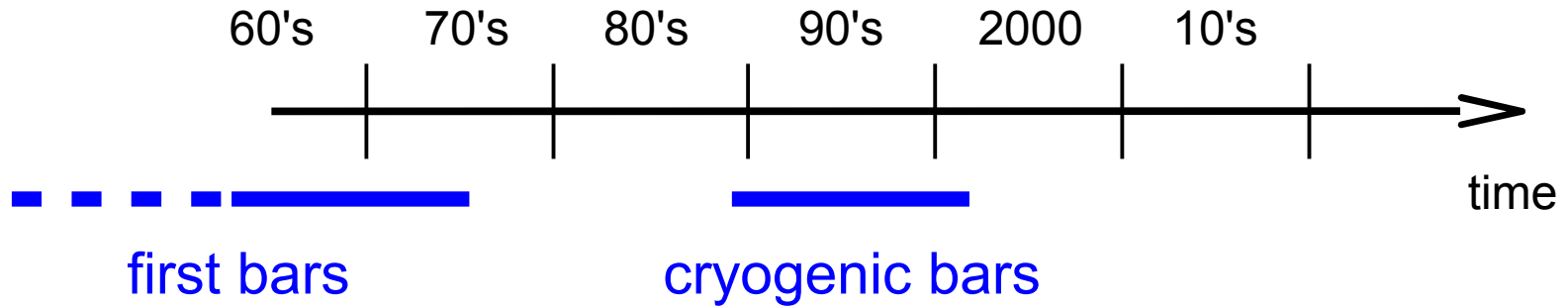
Science beyond detection

Multimessenger astronomy

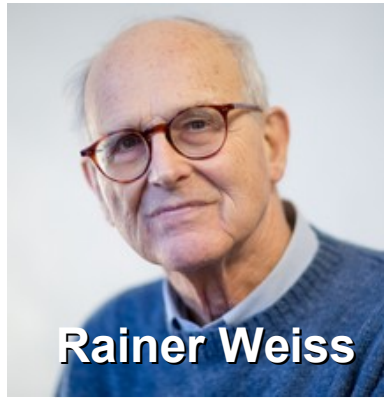
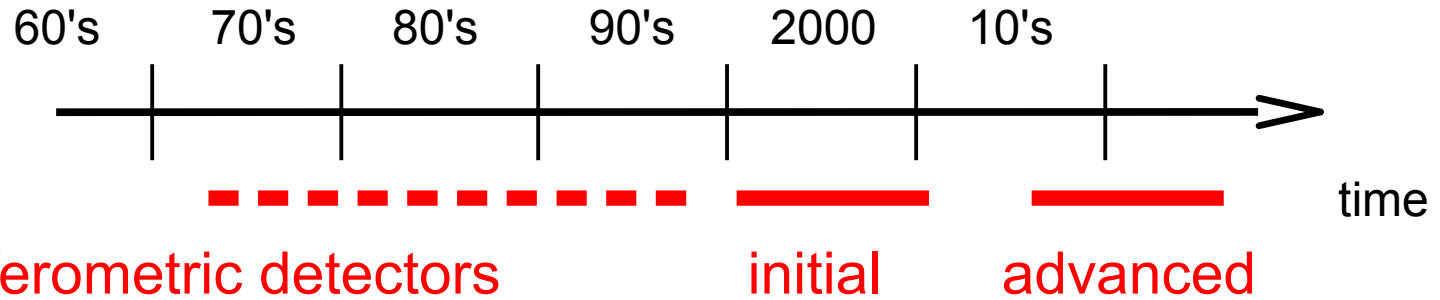
Outlook



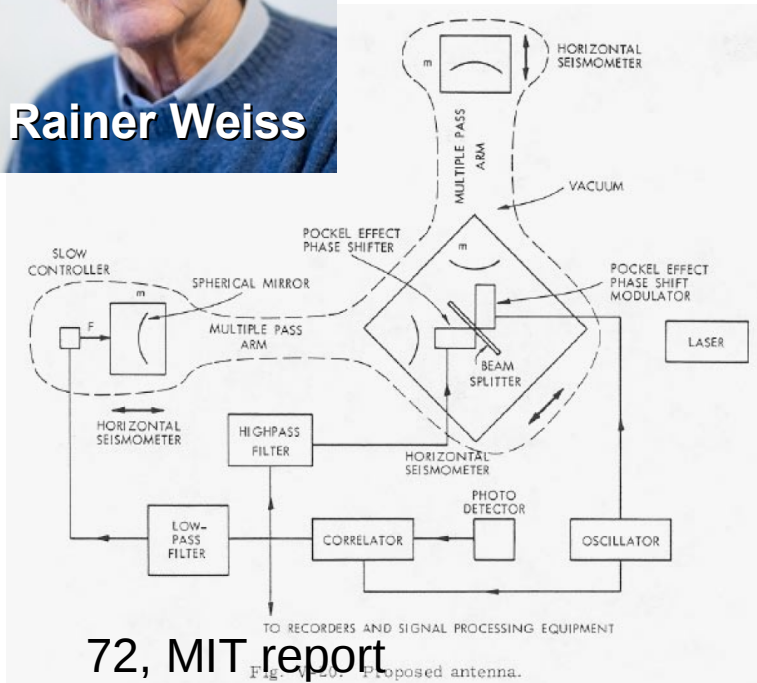
# History of direct detection (1)



# History of direct detection (2)



Since 2007 LIGO and Virgo operates as a network  
Data are shared and analyzed jointly

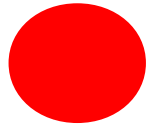




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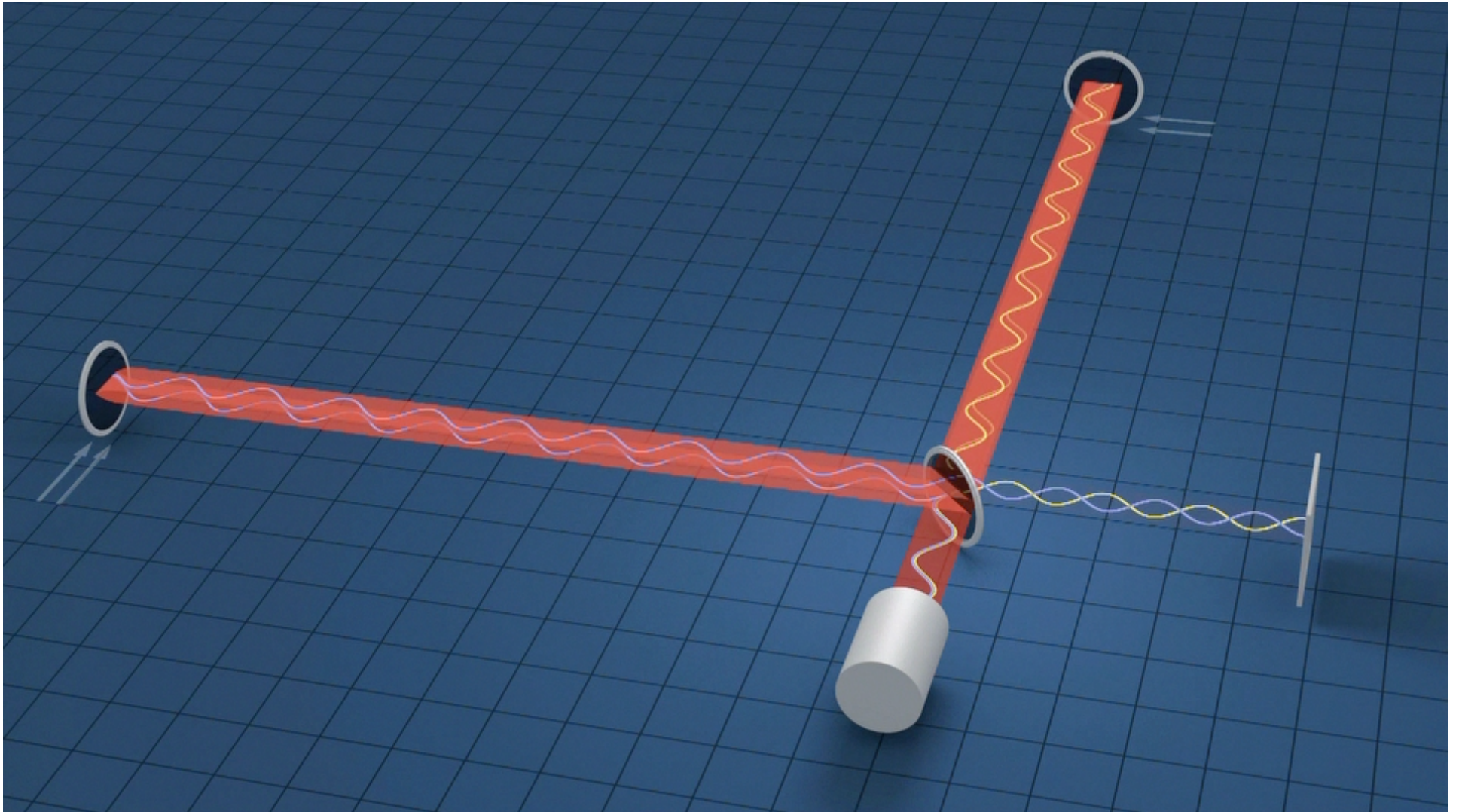
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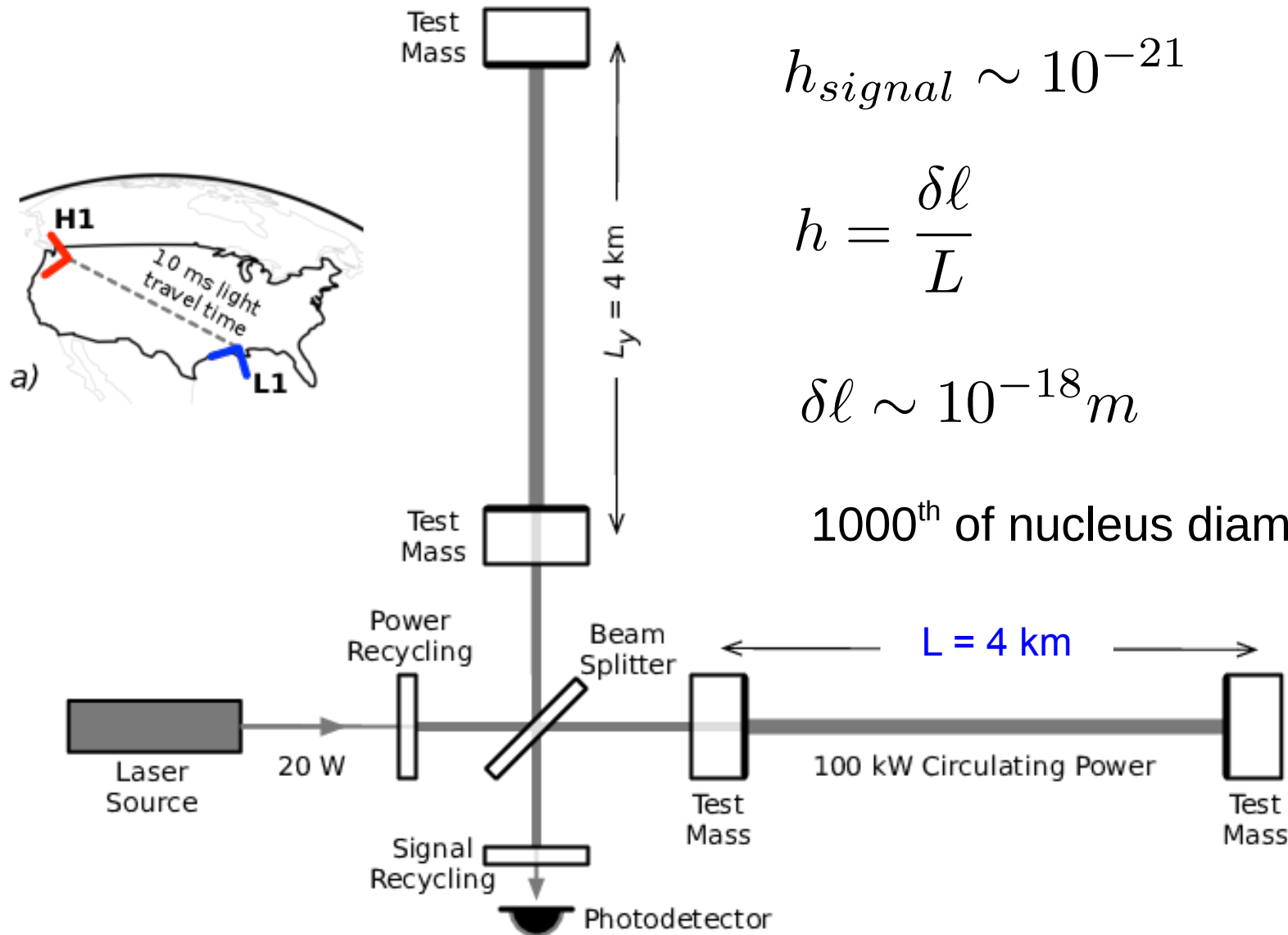
Outlook

# Michelson interferometer





# Advanced LIGO (1)



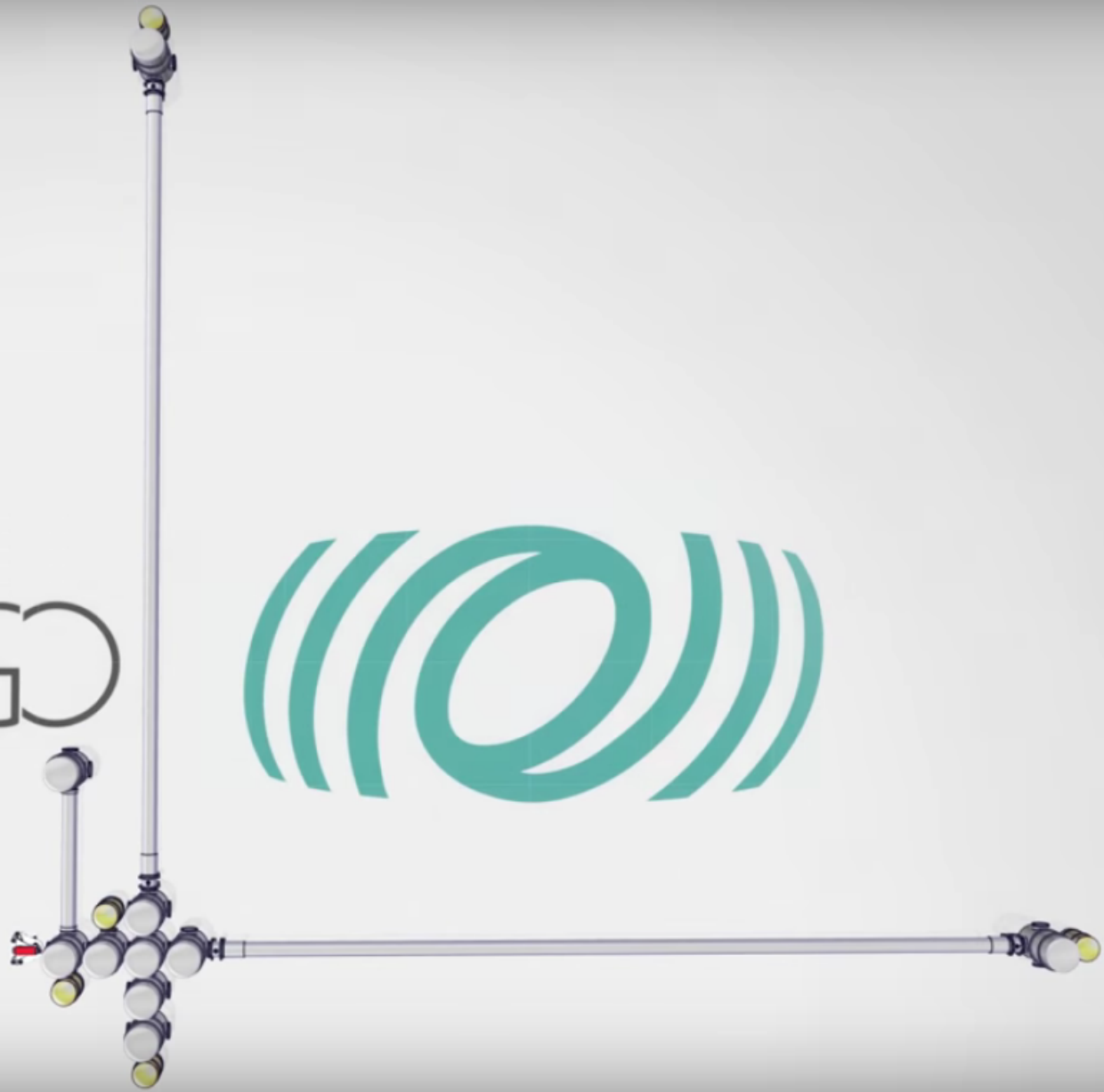
$$h_{signal} \sim 10^{-21}$$

$$h = \frac{\delta l}{L}$$

$$\delta l \sim 10^{-18} m$$

1000<sup>th</sup> of nucleus diameter!

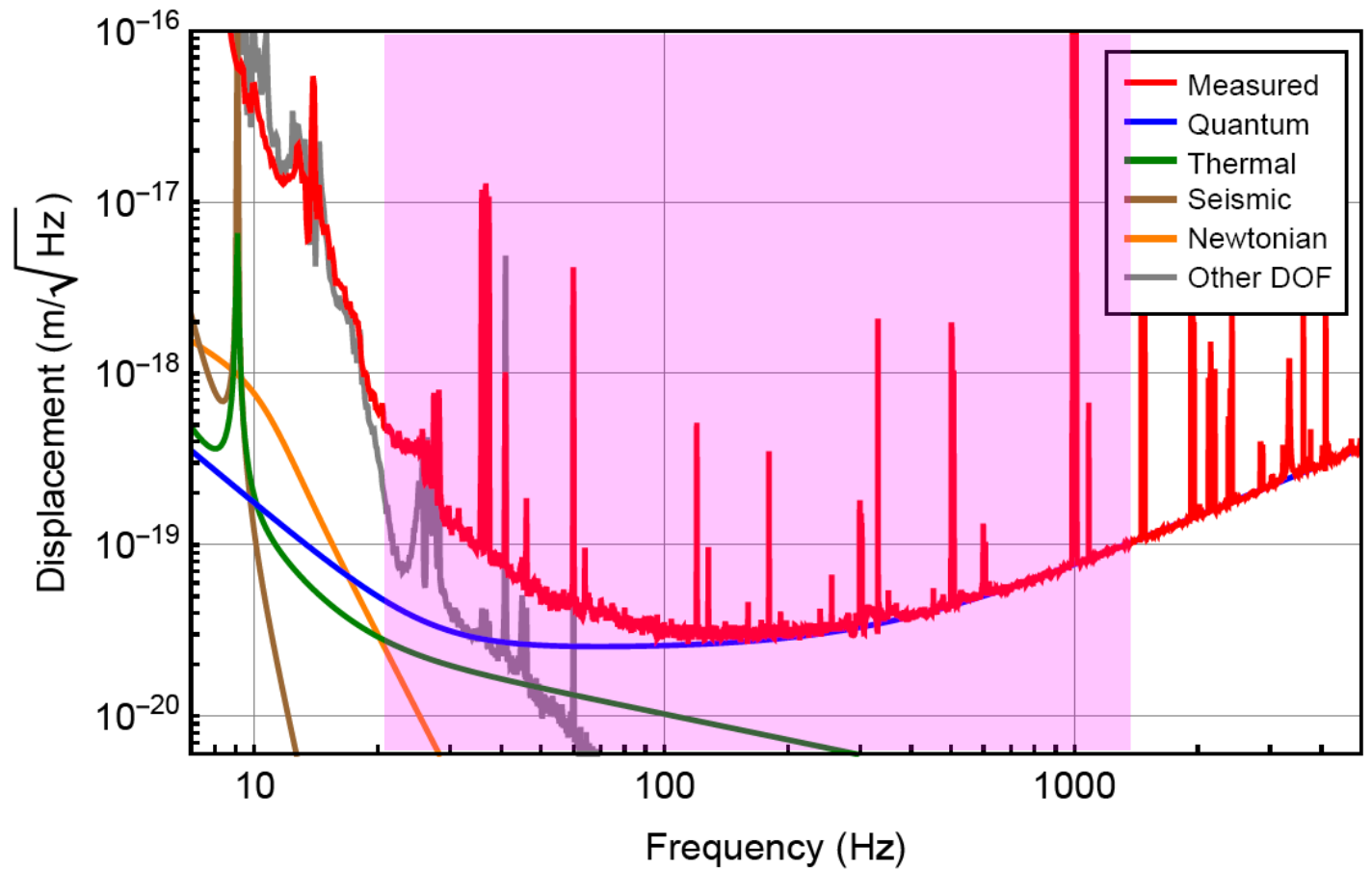
VIRGO





# O1 science run

sep 2015 - 4 months



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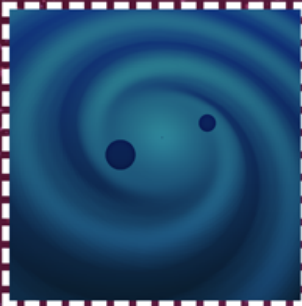
Outlook



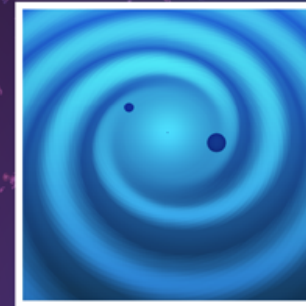
September 14, 2015  
CONFIRMED



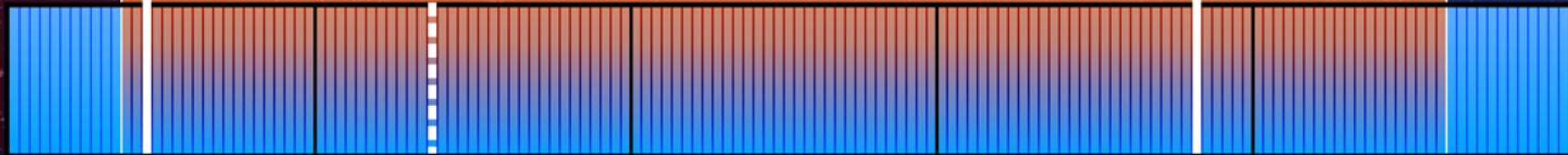
October 12, 2015  
CANDIDATE



December 26, 2015  
CONFIRMED



LIGO's first observing run  
September 12, 2015 - January 19, 2016



September 2015

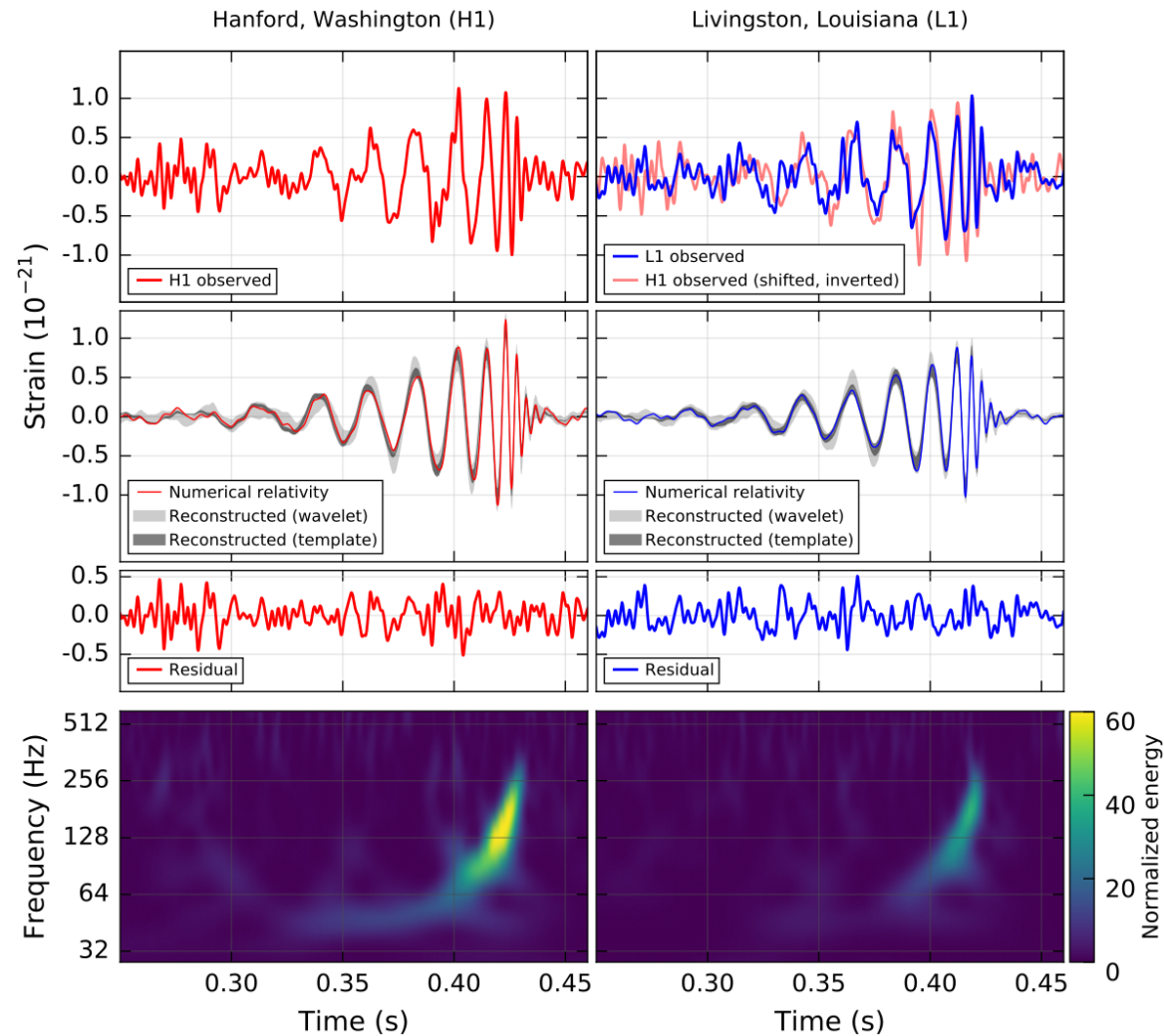
October 2015

November 2015

December 2015

January 2016

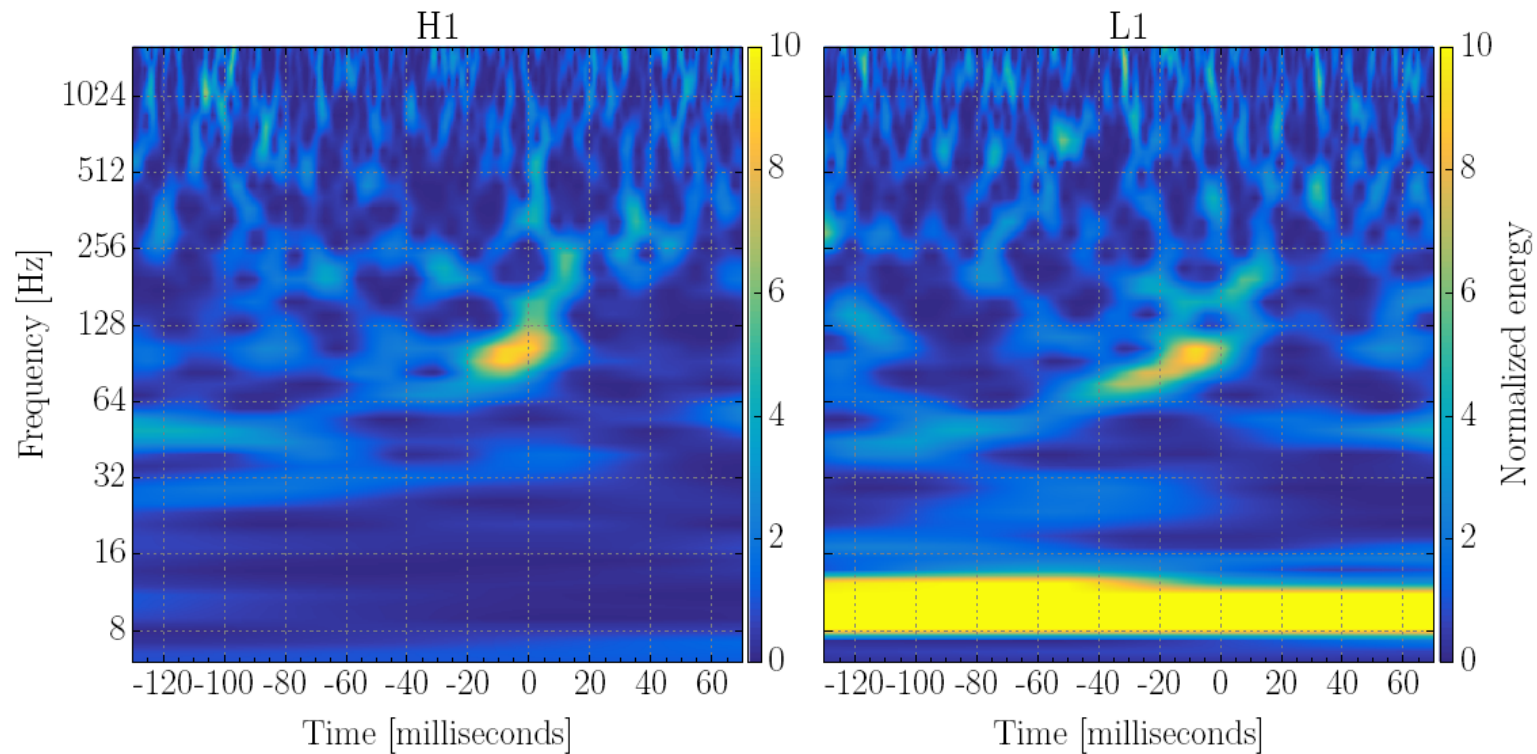
# Sep 14, 2015 09:50:45 UTC



Merger of  $36_{-4}^{+5} M_{\odot}$  and  $29_{-4}^{+4} M_{\odot}$  black holes at  $410_{-180}^{+160}$  Mpc

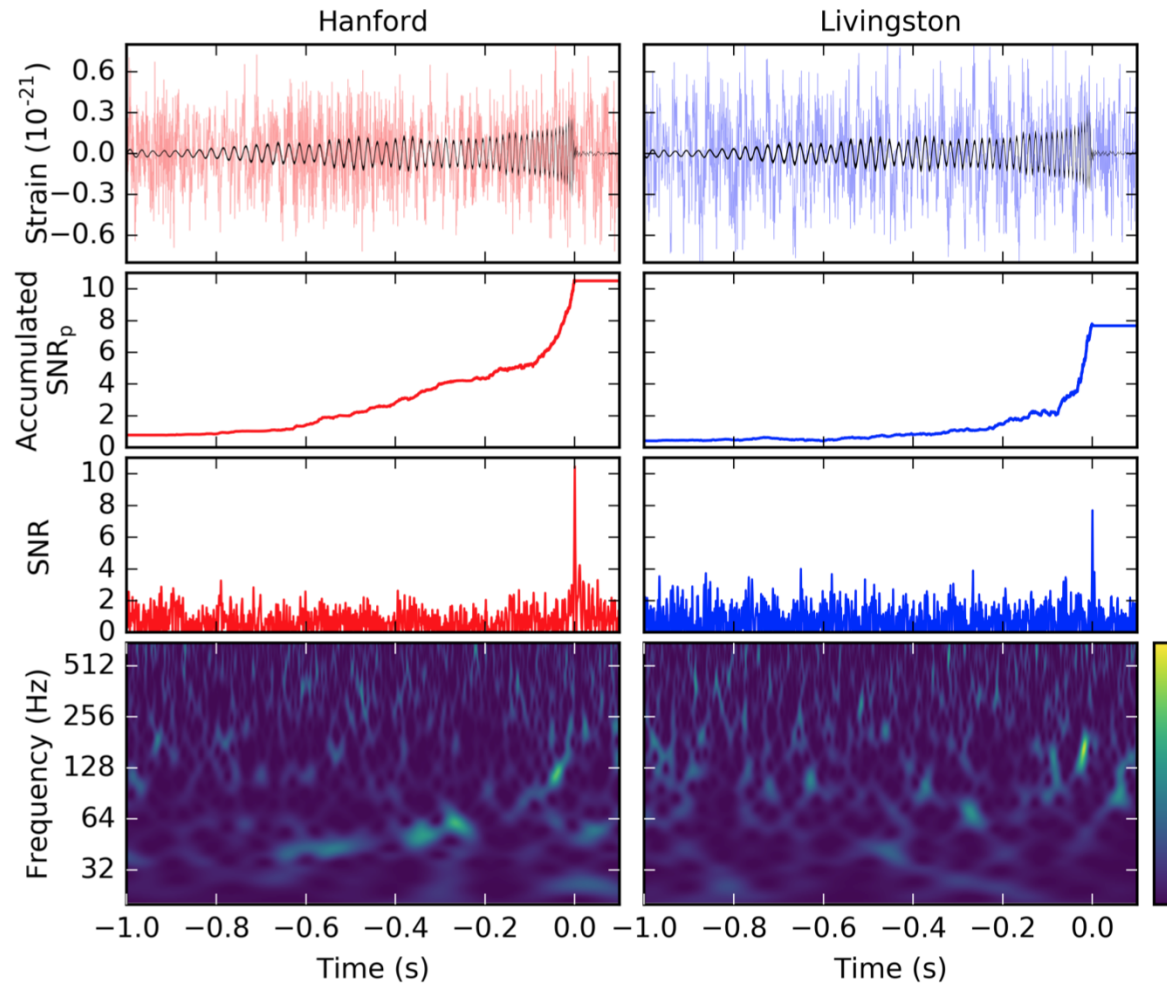


# Oct 12 2015 09:54:43 UTC



Likely merger of  $23_{-5}^{+18} M_{\odot}$  and  $13_{-5}^{+4} M_{\odot}$  black holes at  $1100_{-500}^{+500}$  Mpc

# Dec 26 2015 03:38:53 UTC

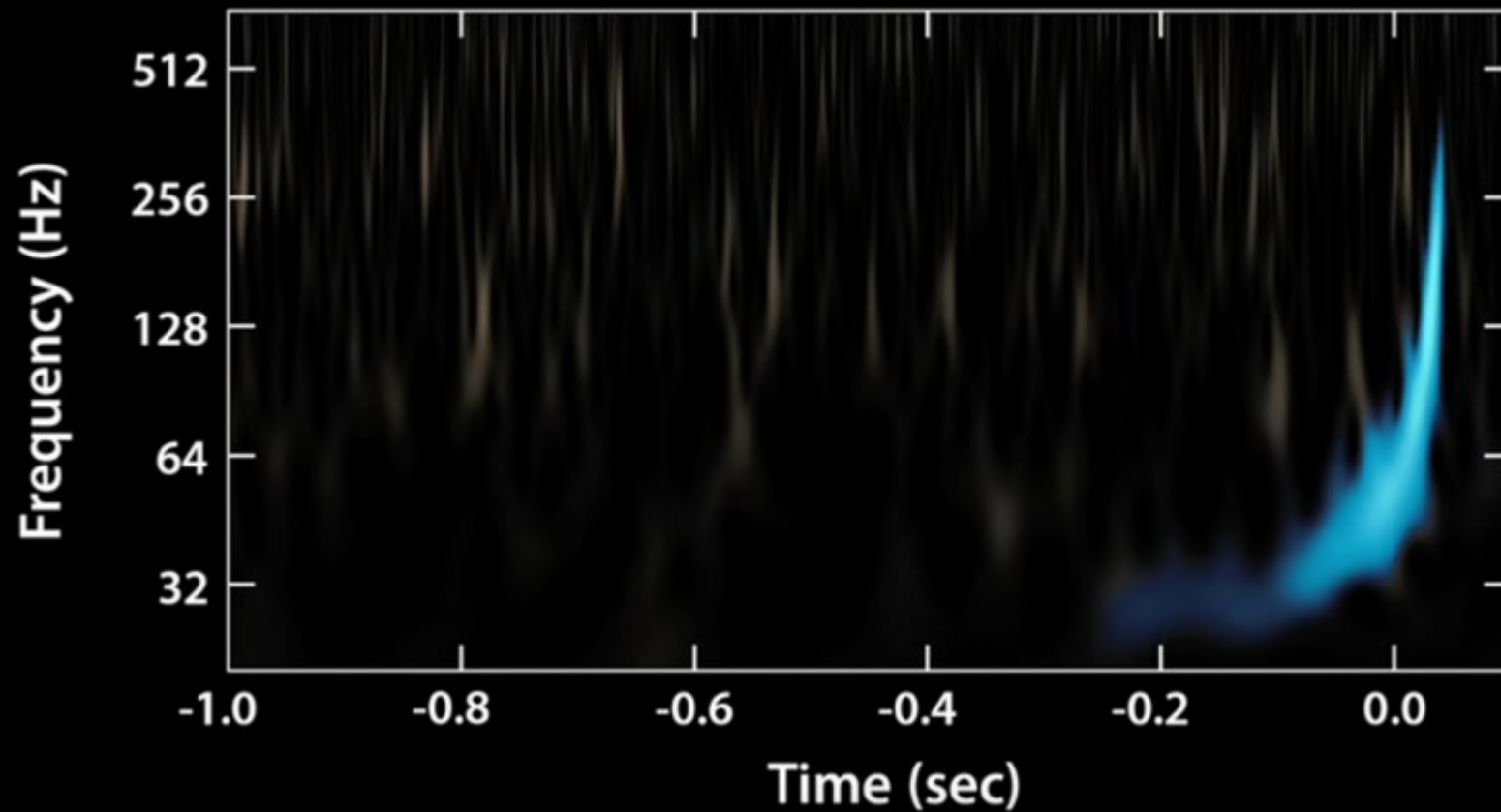


Merger of  $14.2^{+8.3}_{-3.7} M_{\odot}$  and  $7.5^{+2.3}_{-2.3} M_{\odot}$  black holes at  $440^{+180}_{-190}$  Mpc

# Chirps!

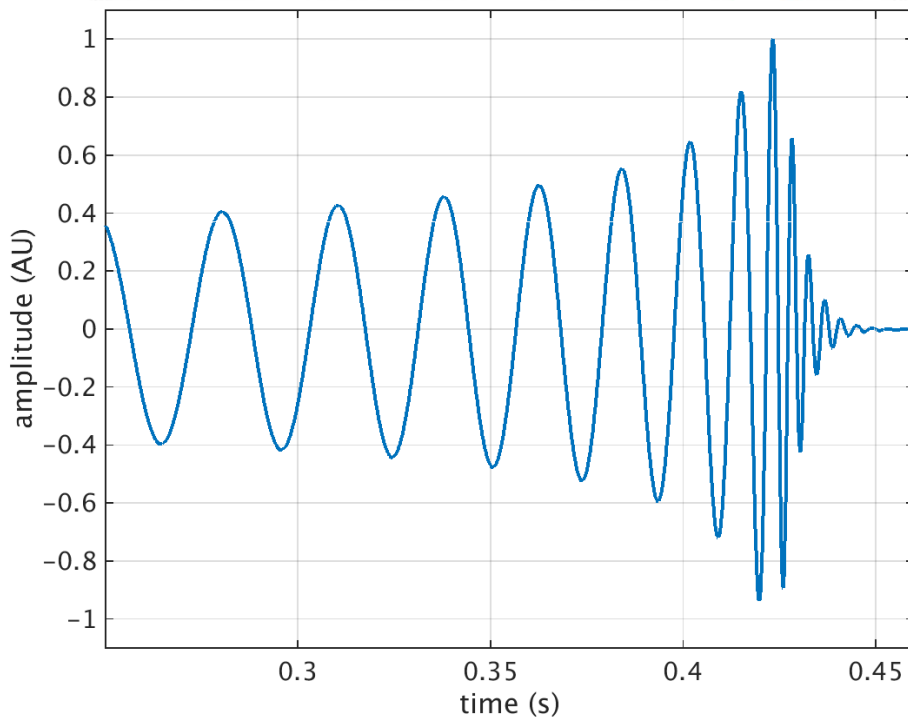
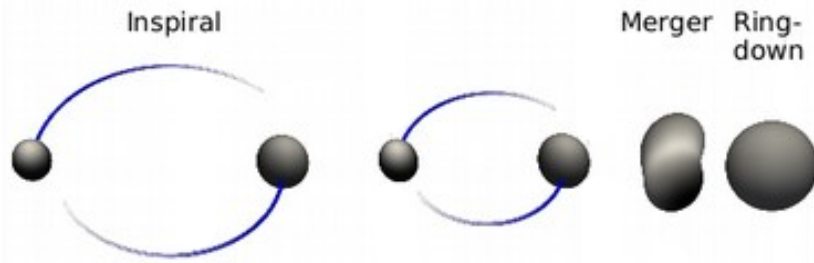
September 14, 2015

Hanford Observatory  
Natural Pitch





# What did we search for?

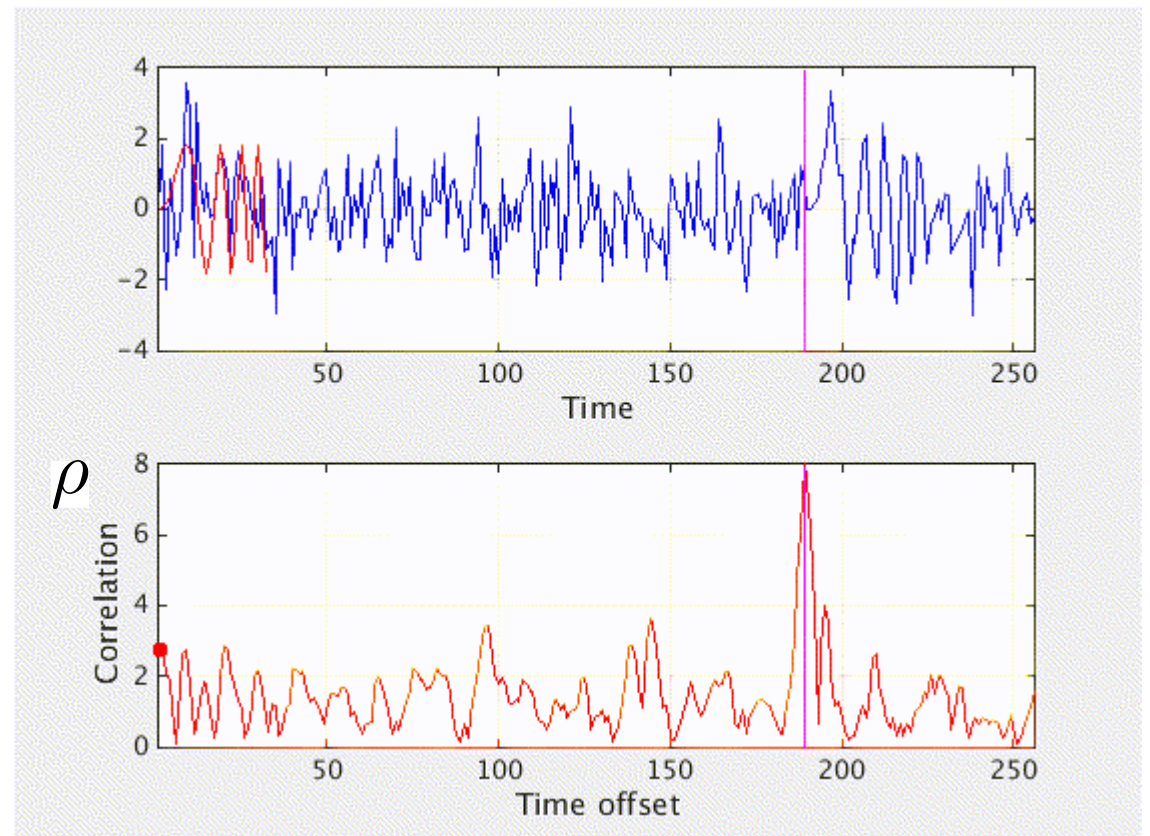
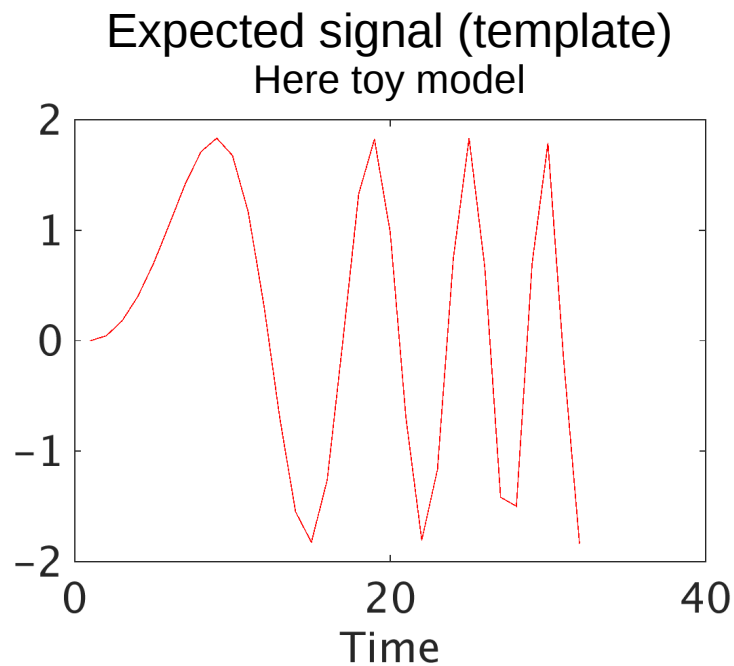


## Template from astrophysical model

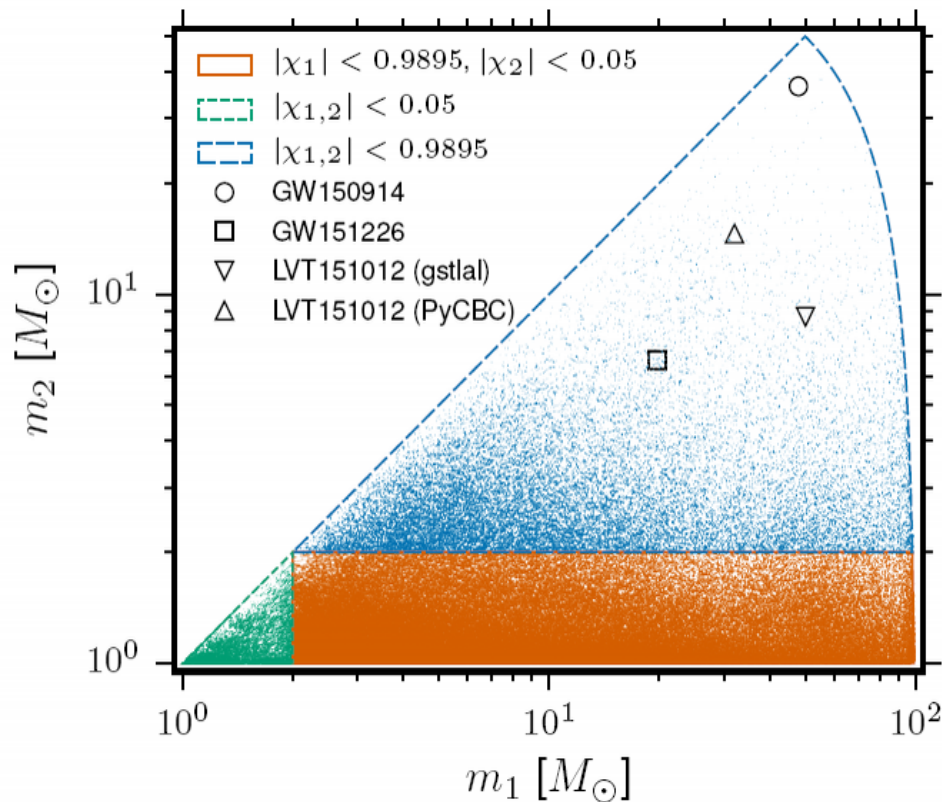
- Characteristic chirp waveform
- Encodes system dynamics
  - Inspiral
    - Leading order: *chirp mass*
    - Next to leading order: mass ratio, spin (assumed aligned with orbital angular momentum)
  - Merger and ringdown
    - Governed by final black-hole mass and spin
- **11 parameters total**
  - 4 mass and (aligned) spins, and geometrical params (no excentricity)

# How did we search? Matched filtering

Correlate data with expected signal



# Matched filtering: basic ideas (2)



**250 000 templates**

covers BNS, NS-BH, BBH

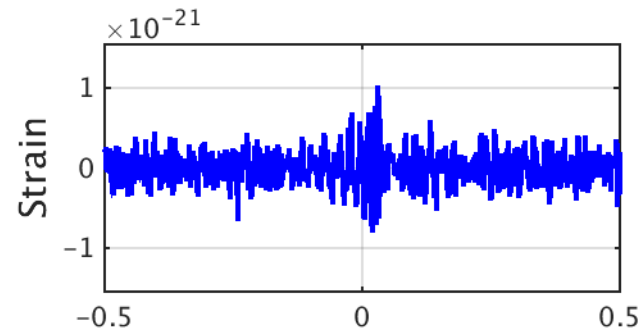
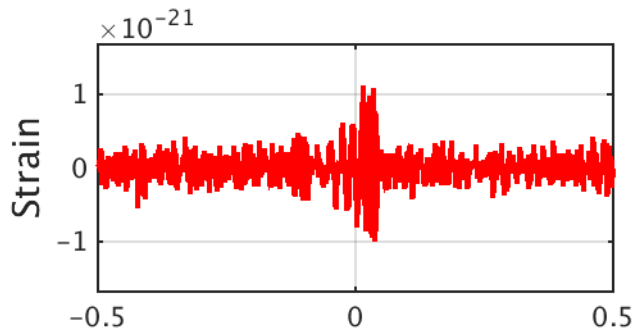
## Bank of chirp templates

- Detect **any signal** in a **space of possible signals** all with different phase evolution
- Do it with a **finite set of templates!**
- Make sure there is a “close” template for every part of the signal space
- Natural metric: correlation between neighboring templates → regular or random lattices of templates

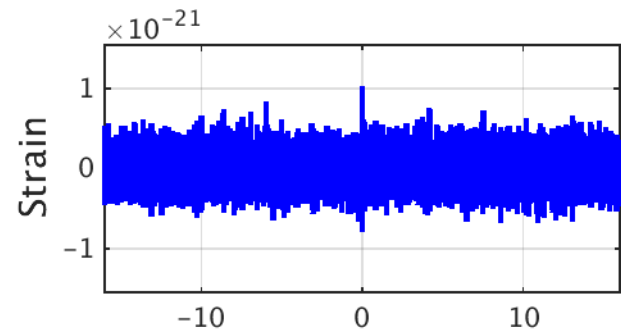
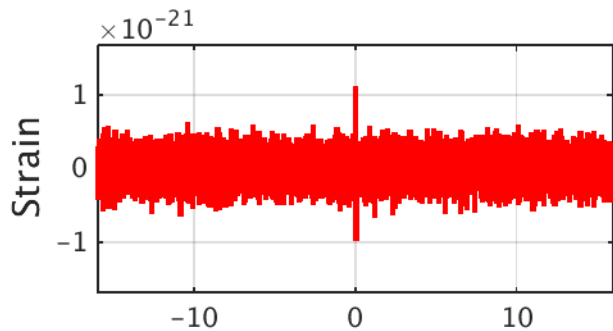


# Non-Gaussian noise - Glitches

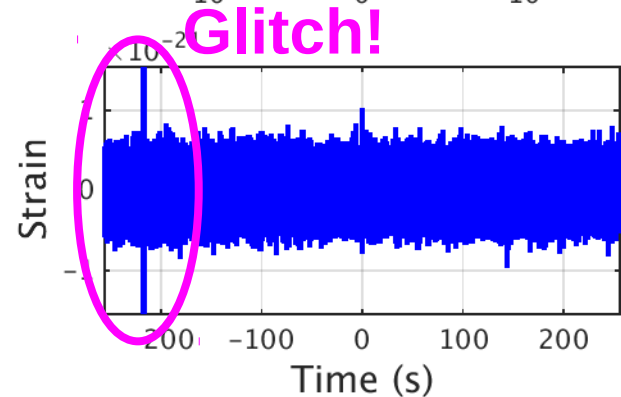
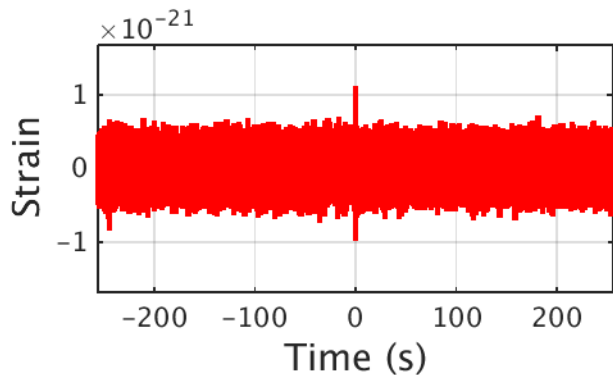
second



$\sim$ minutes

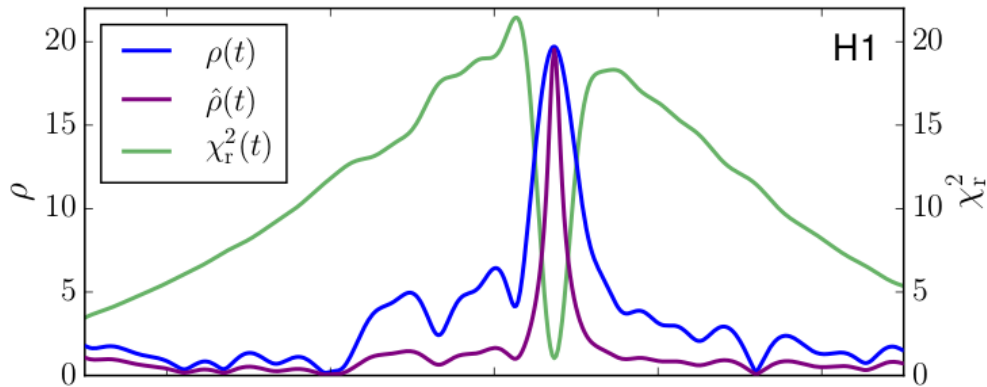


$\sim$  10 minutes



Glitch rate  $\sim$  1 per few seconds to 1 per 20 min

# Signal consistency



Non-Gaussian artefacts (glitches)

Waveform consistency

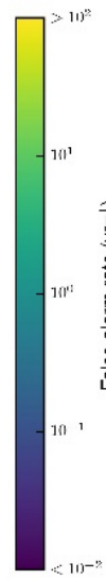
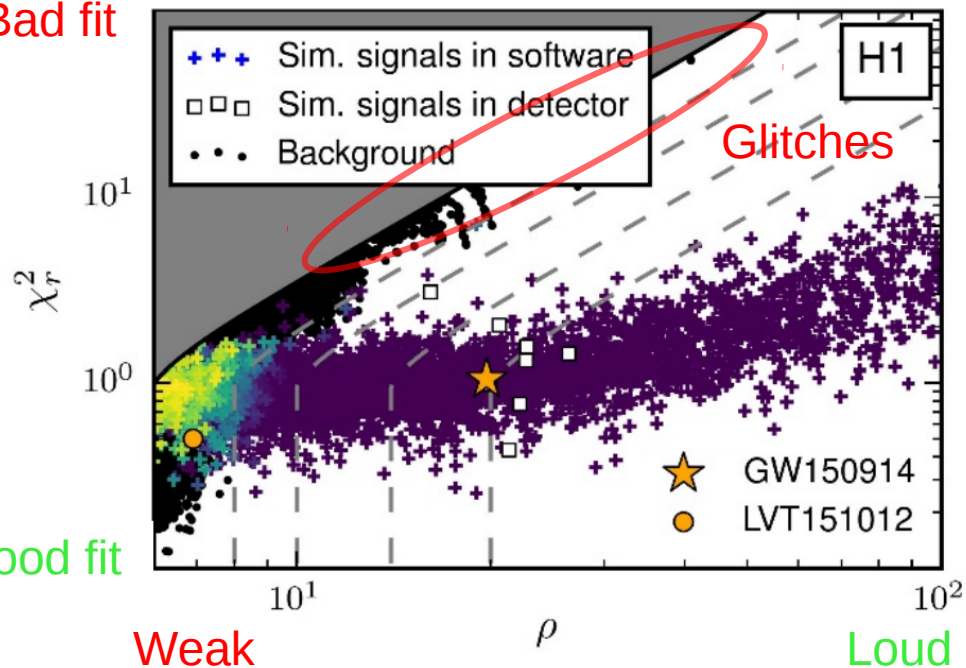
- $\chi_r^2$  test that checks consistency of spectral power distribution

- Detection statistic

$$\hat{\rho} = \rho \left\{ \left[ 1 + (\chi_r^2)^3 \right] / 2 \right\}^{-1/6}$$

Coincident triggers in both detectors (time and mass/spins)

Bad fit



Good fit

Weak

Loud

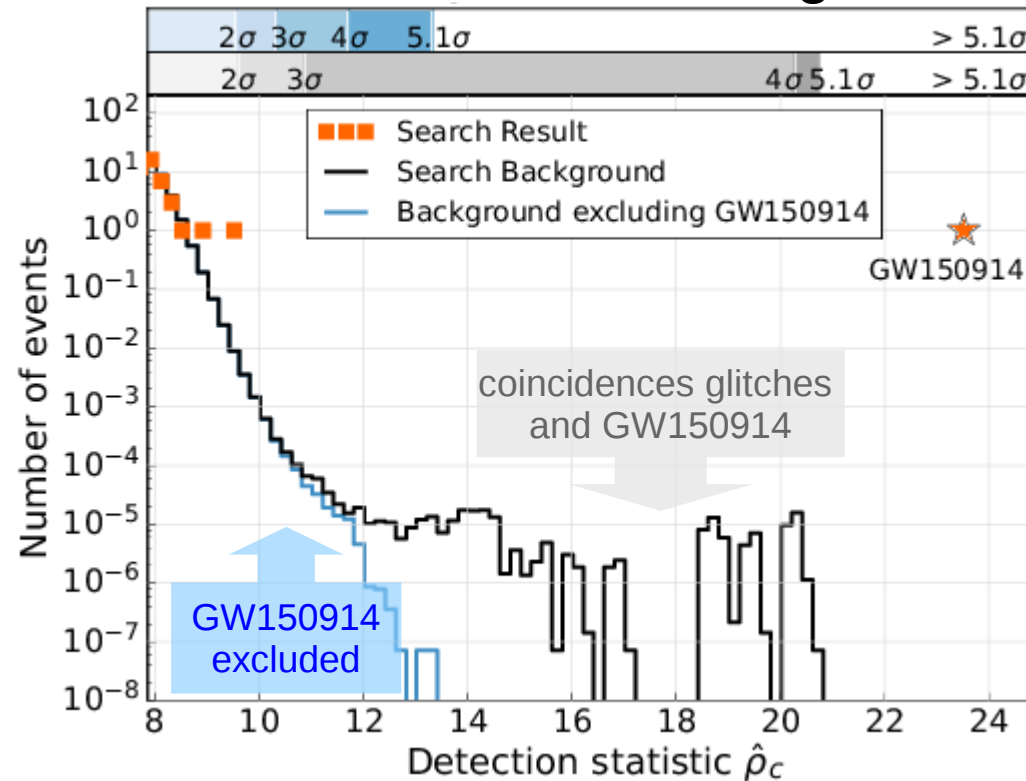
# Statistical significance (1)

- What is the chance that this event is noise?  
(i.e., the event **statistical significance**)
  - Probability that glitches occur in coincidence at both detectors
  - Challenging to **measure the experimental background**
    - ♦ Non-Gaussian noise (glitches) is **impossible to model**
    - ♦ **Can't shield the detector** from gravitational wave!
    - ♦ Estimate background to **high-significance ( $p\text{-value} < 10^{-6}$ )**  
For comparison: glitch occurrence  $\sim 1\text{--}10\%$  of observation time
  - **Empirical estimate from the data – resampling**
    - Data time-stamps are **artificially shifted by an offset** much larger than the inter-site propagation time
    - Repeat this operation million times with different offsets



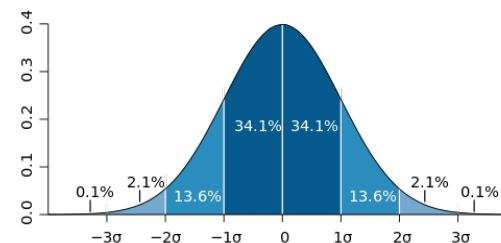
# Statistical significance (2)

Binary coalescence search  
Matched filtering



**> 5.1  $\sigma$**

Probability that this event is due to background alone is  $\sim 1/5\,000\,000$   
16 days of observation  $\rightarrow$  less than 1 noise event per 203 000 years

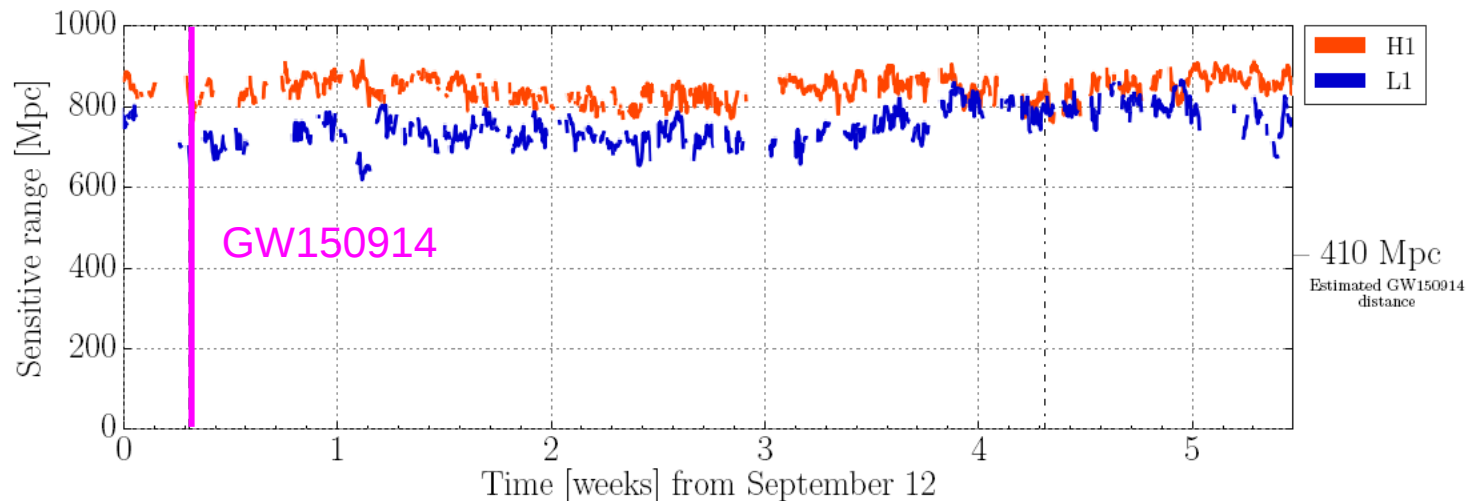


**5 $\sigma$**

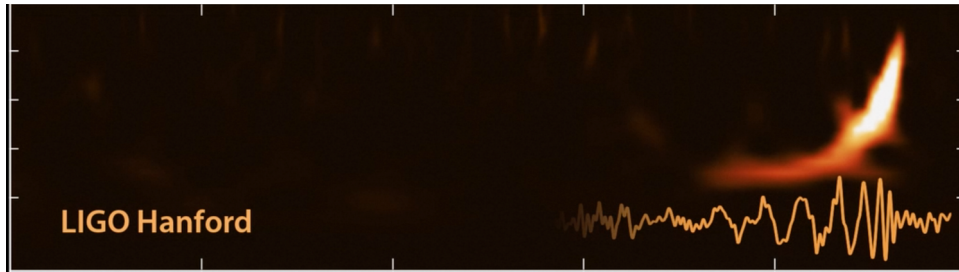


# Why are we confident in the detection?

- Event occurred in a **normal/stable operation period**
- **Monitor instrument and environment constantly**
  - ◆ 200 000 auxiliary channels
  - ◆ Seismometers, microphones, magnetometers, ...
  - ◆ Coupling measured between the instrument environment and  $h(t)$
- Environmental origin for GW150914 **ruled out**
  - ◆ Excess power in any auxiliary channel too small by factor  $> 17$  to account for GW150914
  - ◆ Would not match signal morphology anyway



# How do we know this is a black hole binary?



Over 200 ms, **frequency and amplitude increase** from 35 to 150 Hz ( $\sim 8$  cycles)

- GW-driven of two orbiting masses
- Inspiral evolution characterized by **chirp mass**

$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left[ \frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^{3/5}$$

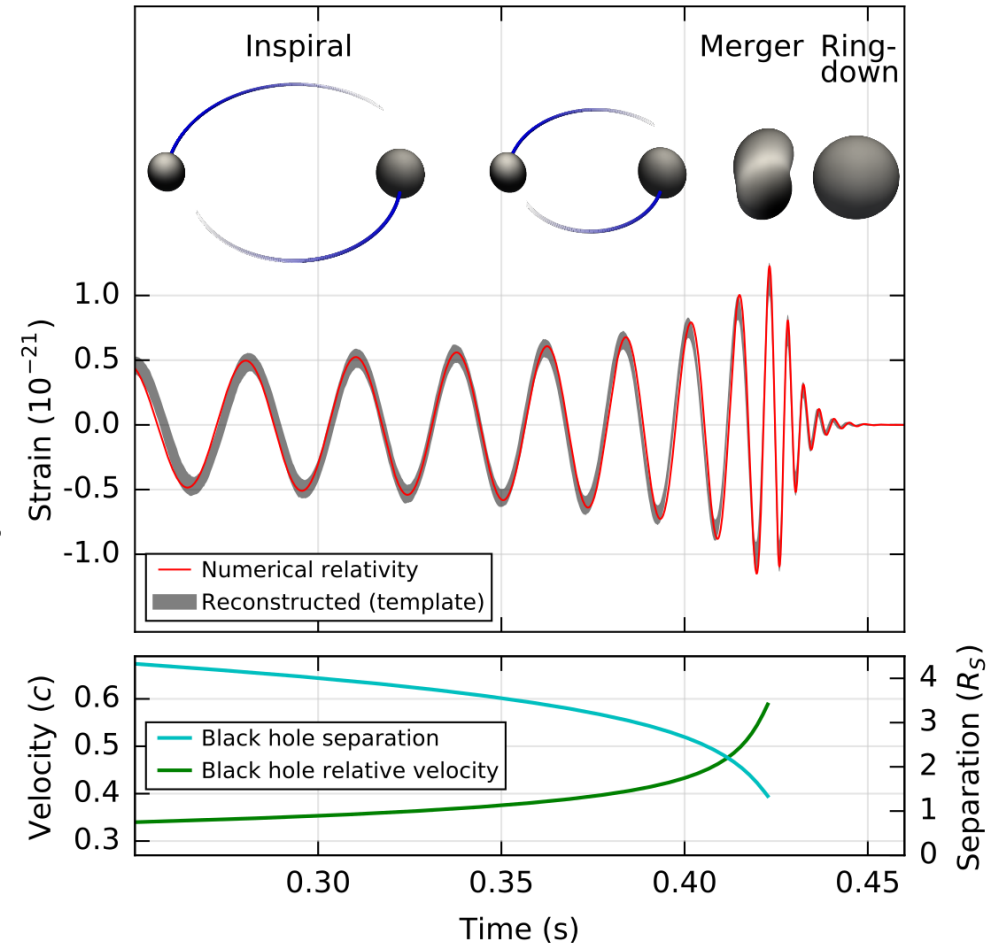
$$\mathcal{M} \approx 30 M_\odot \quad M > 70 M_\odot$$

Keplerian separation gets close to Schwarzschild radius

- BNS too light, NSBH would merge at lower frequencies

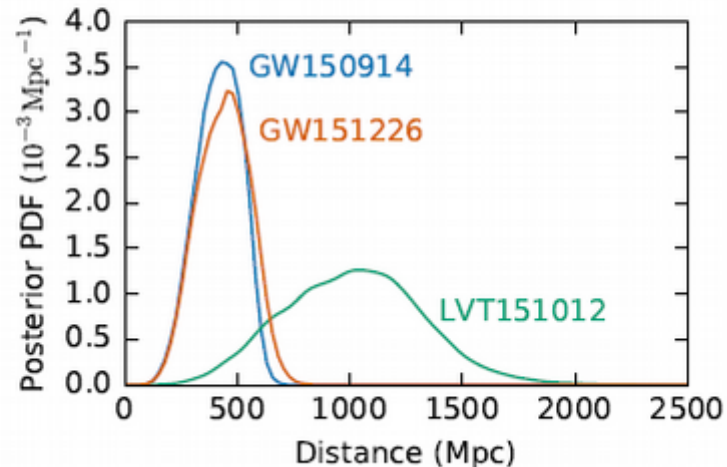
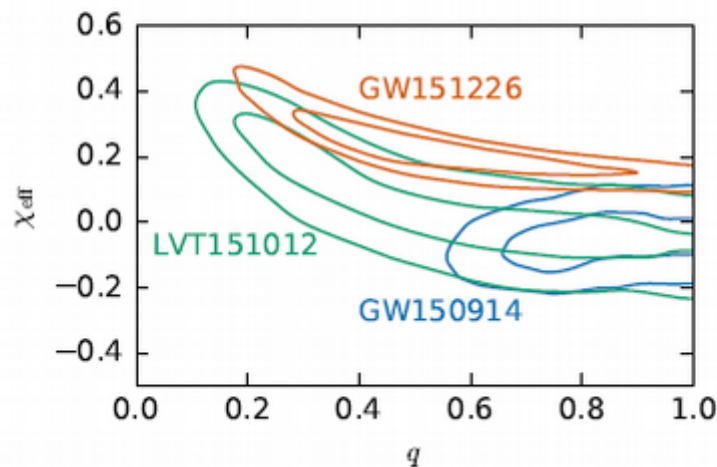
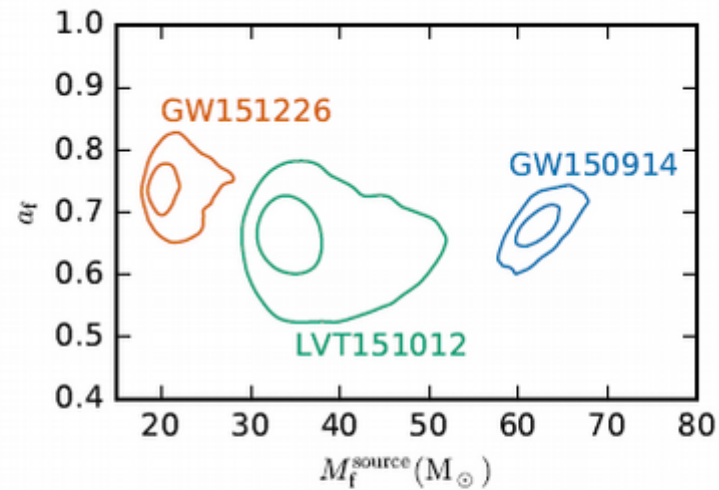
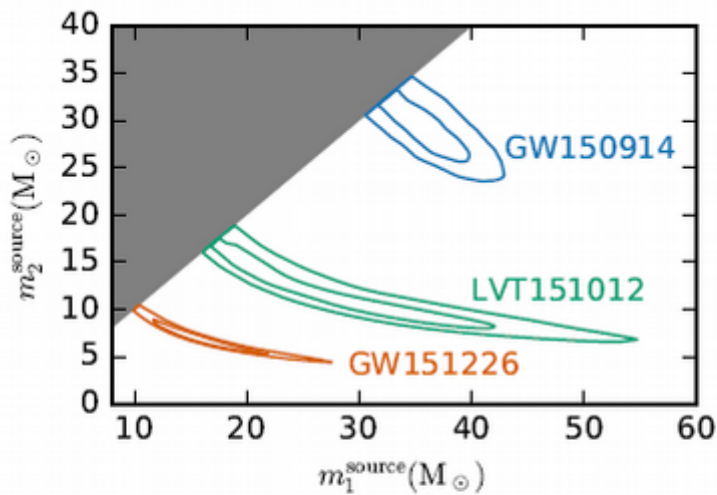
Decay of waveform after peak

- Consistent with damped oscillations of BH relaxing to final stationary Kerr configuration
- But SNR too low to claim observation of normal modes



$$R_S = 2GM/c^2 \geq 210 \text{ km}$$

# Beyond detection: Parameter estimation

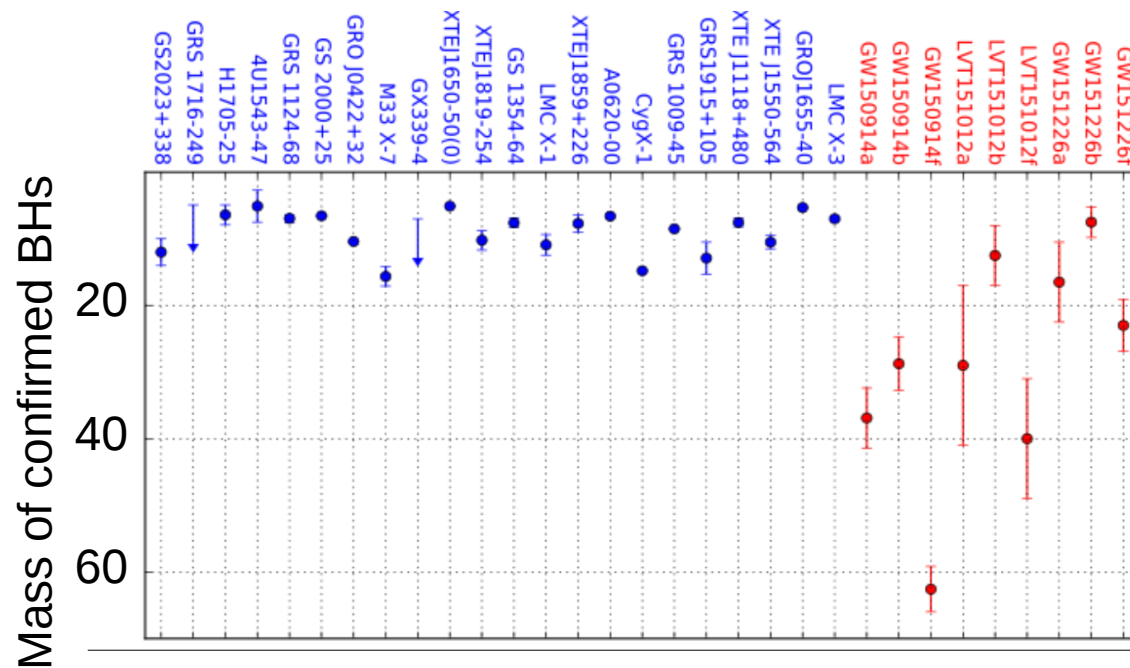




Event	GW150914	GW151226	LVT151012
Signal-to-noise ratio $\rho$	23.7	13.0	9.7
False alarm rate FAR/yr <sup>-1</sup>	$< 6.0 \times 10^{-7}$	$< 6.0 \times 10^{-7}$	0.37
p-value	$7.5 \times 10^{-8}$	$7.5 \times 10^{-8}$	0.045
Significance	$> 5.3\sigma$	$> 5.3\sigma$	$1.7\sigma$
Primary mass $m_1^{\text{source}}/M_\odot$	$36.2^{+5.2}_{-3.8}$	$14.2^{+8.3}_{-3.7}$	$23^{+18}_{-6}$
Secondary mass $m_2^{\text{source}}/M_\odot$	$29.1^{+3.7}_{-4.4}$	$7.5^{+2.3}_{-2.3}$	$13^{+4}_{-5}$
Chirp mass $\mathcal{M}^{\text{source}}/M_\odot$	$28.1^{+1.8}_{-1.5}$	$8.9^{+0.3}_{-0.3}$	$15.1^{+1.4}_{-1.1}$
Total mass $M^{\text{source}}/M_\odot$	$65.3^{+4.1}_{-3.4}$	$21.8^{+5.9}_{-1.7}$	$37^{+13}_{-4}$
Effective inspiral spin $\chi_{\text{eff}}$	$-0.06^{+0.14}_{-0.14}$	$0.21^{+0.20}_{-0.10}$	$0.0^{+0.3}_{-0.2}$
Final mass $M_f^{\text{source}}/M_\odot$	$62.3^{+3.7}_{-3.1}$	$20.8^{+6.1}_{-1.7}$	$35^{+14}_{-4}$
Final spin $a_f$	$0.68^{+0.05}_{-0.06}$	$0.74^{+0.06}_{-0.06}$	$0.66^{+0.09}_{-0.10}$
Radiated energy $E_{\text{rad}}/(M_\odot c^2)$	$3.0^{+0.5}_{-0.4}$	$1.0^{+0.1}_{-0.2}$	$1.5^{+0.3}_{-0.4}$
Peak luminosity $\ell_{\text{peak}}/(\text{erg s}^{-1})$	$3.6^{+0.5}_{-0.4} \times 10^{56}$	$3.3^{+0.8}_{-1.6} \times 10^{56}$	$3.1^{+0.8}_{-1.8} \times 10^{56}$
Luminosity distance $D_L/\text{Mpc}$	$420^{+150}_{-180}$	$440^{+180}_{-190}$	$1000^{+500}_{-500}$
Source redshift $z$	$0.09^{+0.03}_{-0.04}$	$0.09^{+0.03}_{-0.04}$	$0.20^{+0.09}_{-0.09}$
Sky localization $\Delta\Omega/\text{deg}^2$	230	850	1600

**~50 x more luminous than all the stars in the Universe!**

# Astrophysical implications



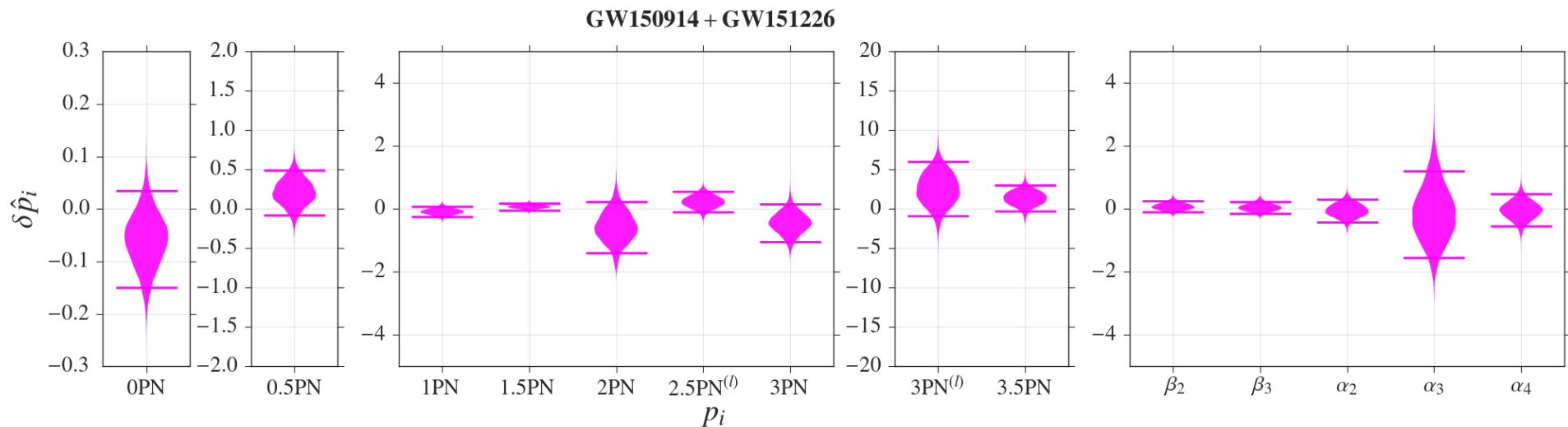
Courtesy: Salvatore Vitale (MIT)

Reveals a yet unobserved population of heavy stellar-mass black holes ( $> 15 M_{\text{sun}}$ )

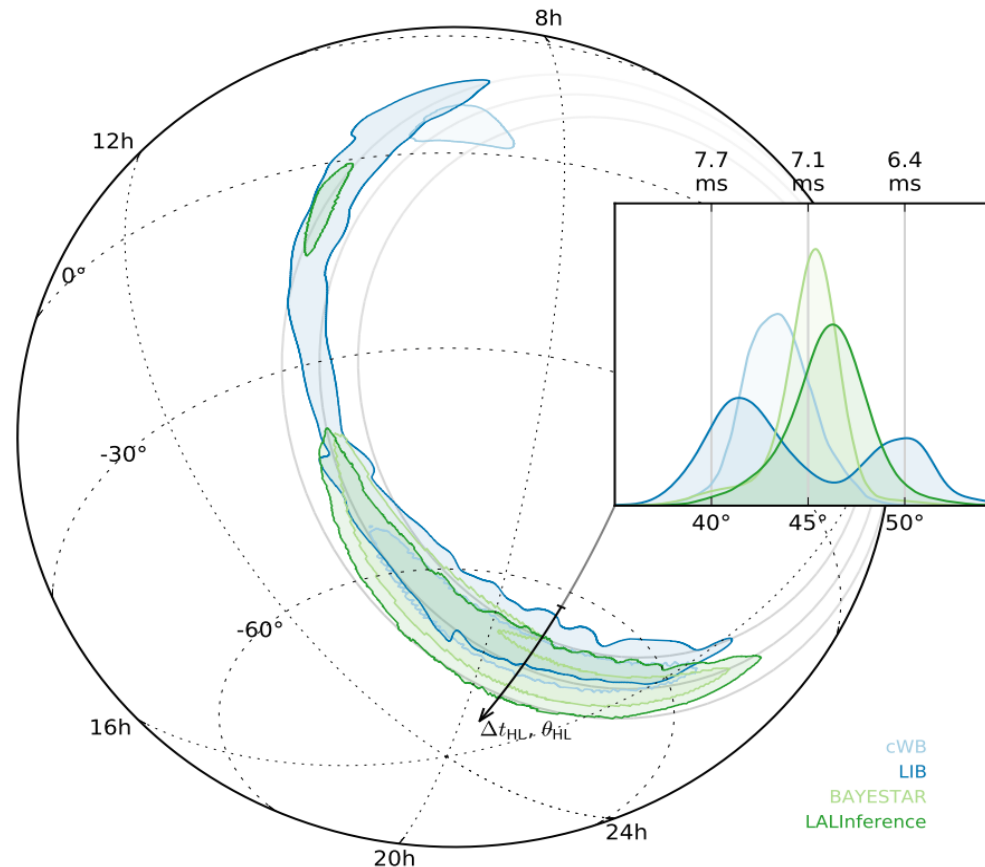
Formation channel?

# Tests of General Relativity

- **Most relativistic binary pulsar** known today
  - J0737-3039, orbital velocity:  $v/c \sim 2 \times 10^{-3}$
- GW150914 and GW151226
  - **Strong field**, non linear, high velocity regime:  $v/c \sim 0.5$
- **No evidence for deviation** from general relativity



# Electromagnetic follow-up (1)



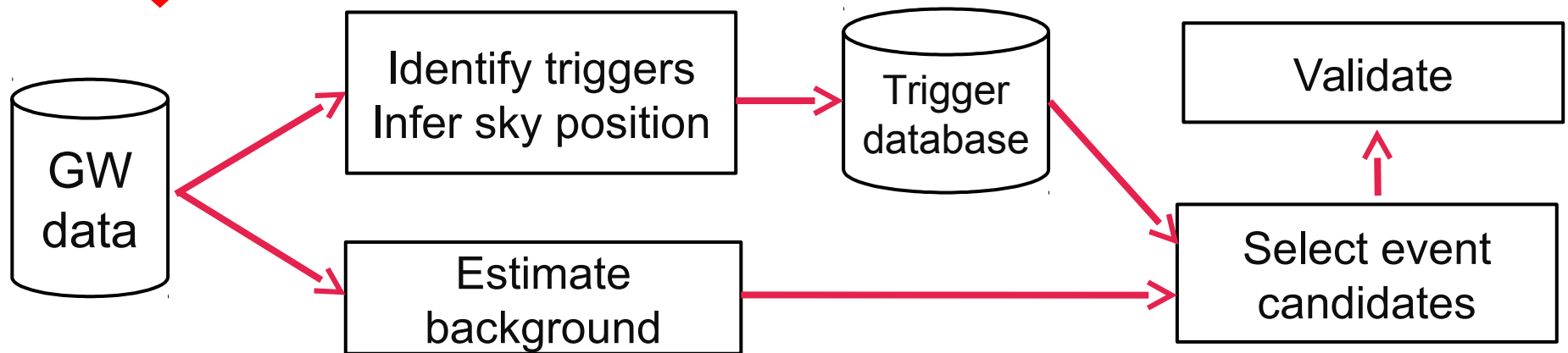
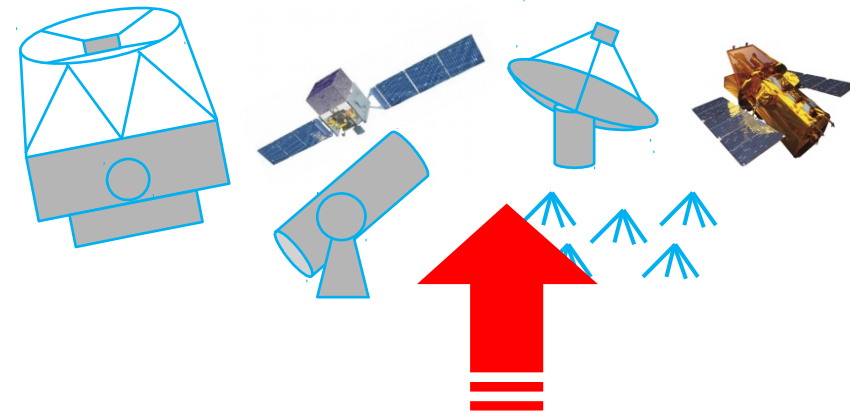
From time-delay, amplitude and phase  
**~600 square degrees – 3000 full moons!**



# Electromagnetic follow-up (2)



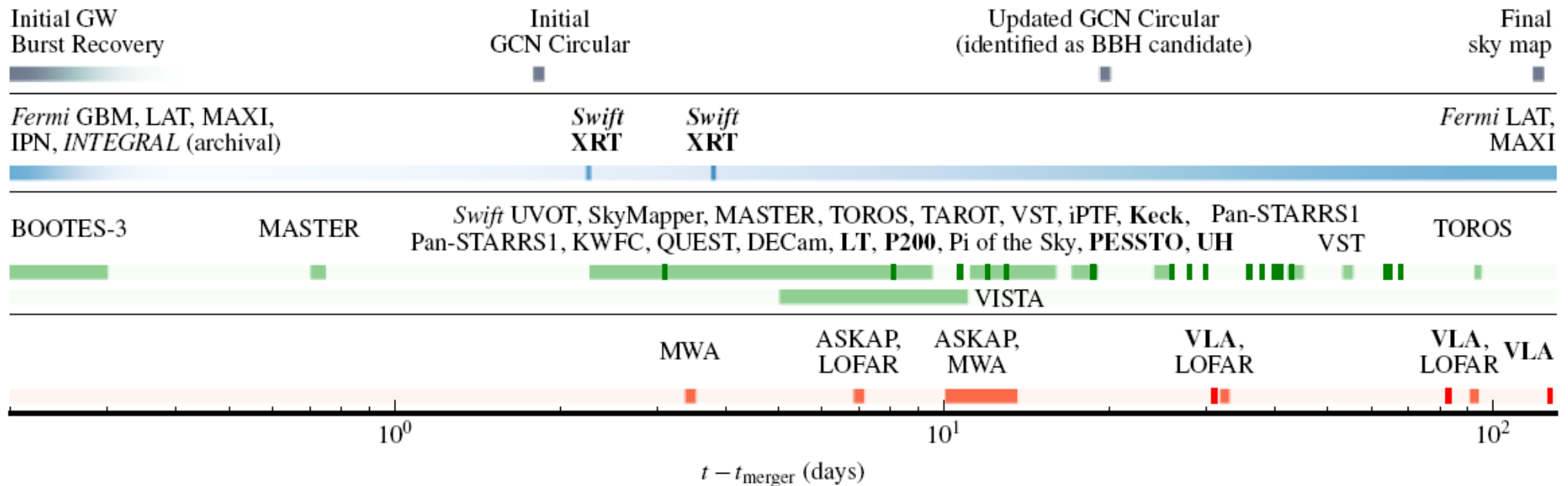
Worldwide network of telescopes and community of observers



# Electromagnetic follow-up (3)

## 25 teams of observers responded to the GW alert

Multiwavelength: from radio to gamma-rays



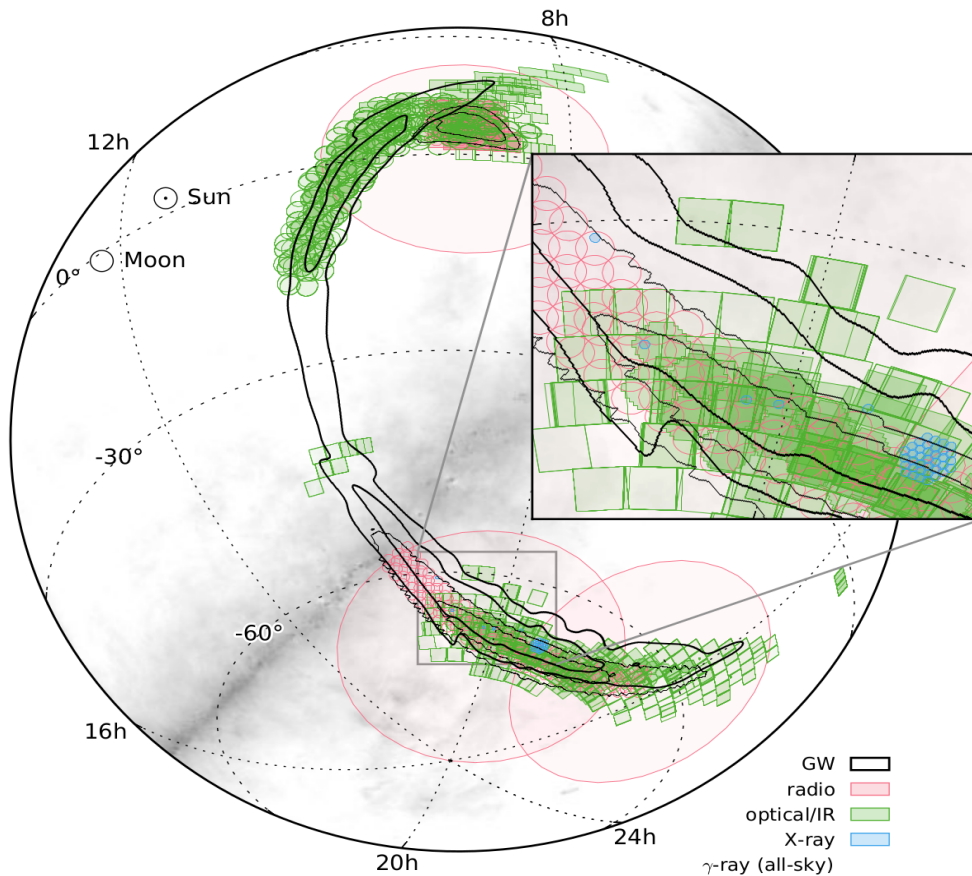
**T0+2 days**

# Electromagnetic follow-up (4)

Follow-up by conventional astronomical observatories

~25 observatories  
from radio waves (100 MHz) ...  
to gamma-rays (300 GeV)

No convincing counterpart has been found so far



# Outline

Primer on gravitational waves

Path to first detection: historical review

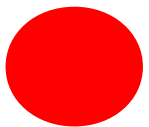
Interferometric detectors: from principles to sensitivity

Results from first aLIGO science run

Search summary

Science beyond detection

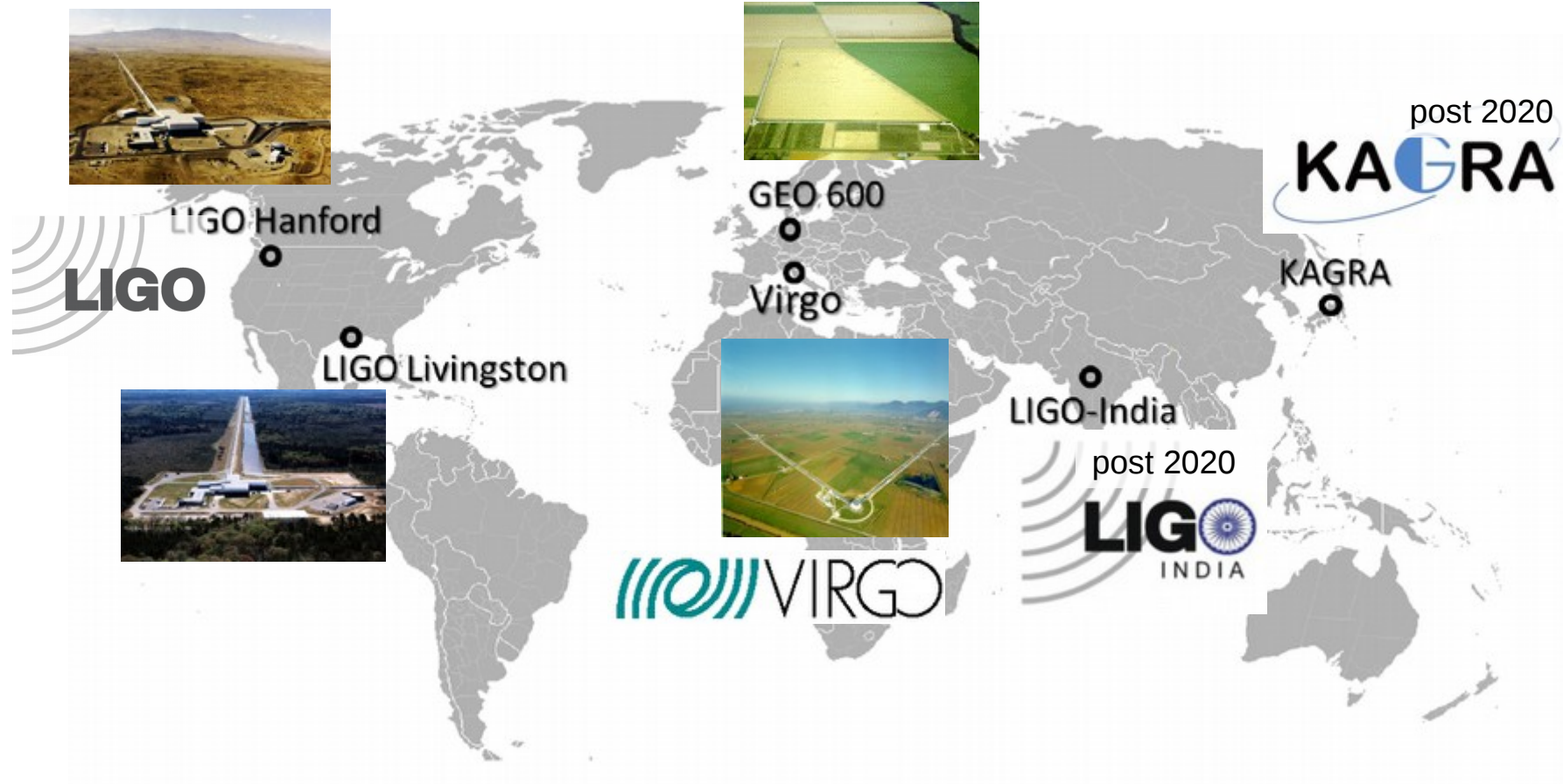
Multimessenger astronomy



Outlook



# What next?



# What next?

- **Immediate future**

- ✓ O2 (starting in September for 6 months)  
Sensitivity  $\times \sim 3 - 10$  BBH?
- ✓ Virgo joining – Better sky resolution

- **1 year**

- ✓ O3 (2017-2018) – another  $\times 2-3 - 10-100$  BBH? BNS? NS-BH?

- **5 years**

- ✓ Kagra – LIGO India joining – (sub-)degree sky resolution!

- **10 years A+**

- ✓ Upgrade to advanced detector

- **15-20 years**

- ✓ 3<sup>rd</sup> generation – target:  $\times 10$  sensitivity
- ✓ Observe the whole Universe in gravitational waves

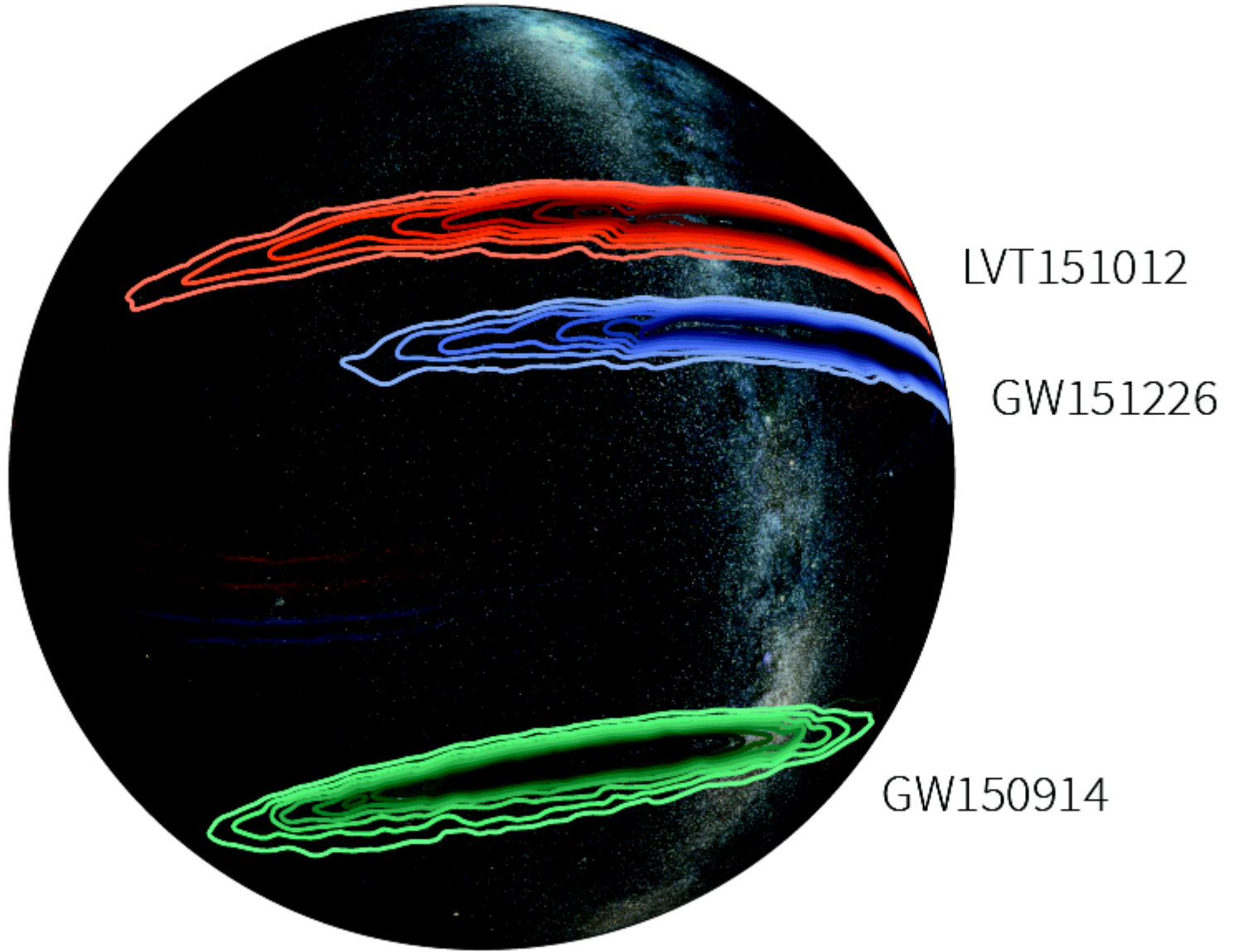


image credit: LIGO/Leo Singer (Milky Way image: Axel Mellinger)

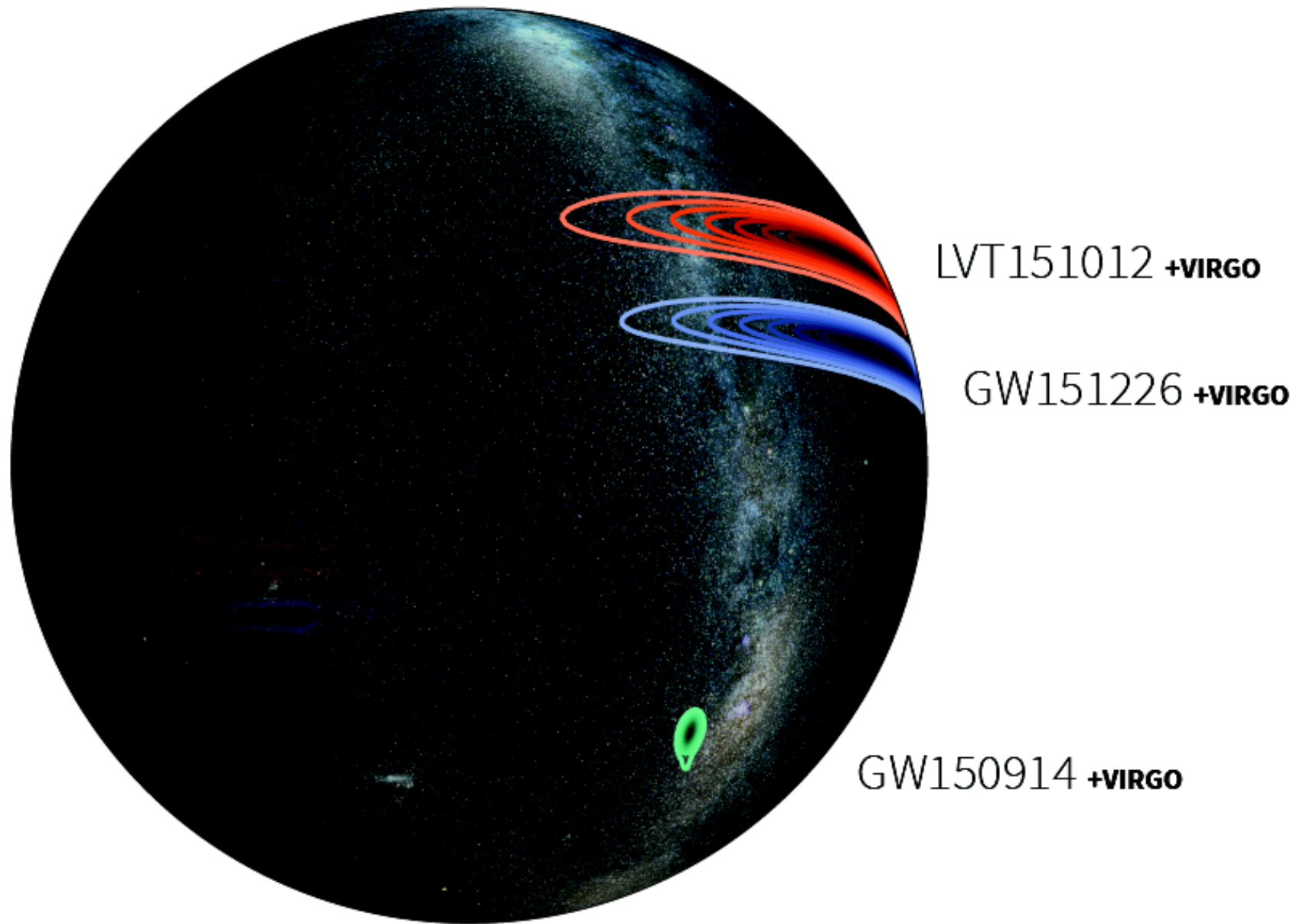


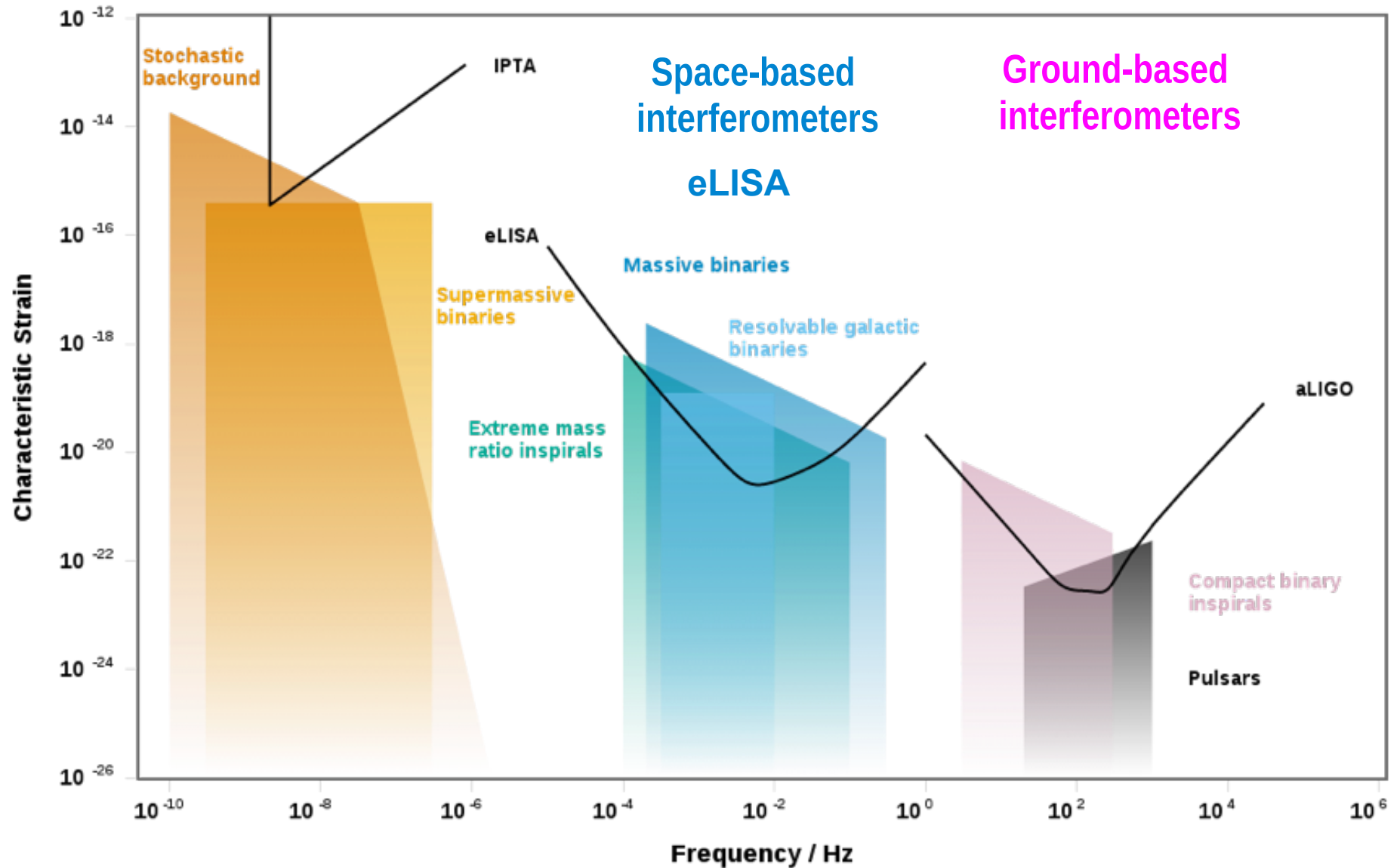
image credit: LIGO/Leo Singer (Milky Way image: Axel Mellinger)

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# Gravitational wave astronomy

## Pulsar Timing Array



# This is just the beginning!

L'UNIVERS DE L'ASSOCIATION FRANÇAISE D'ASTRONOMIE

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