



Bundesministerium
für Bildung
und Forschung



Results on direct CP Violation on B decays in LHCb

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on behalf of the LHCb collaboration

Moriond EW 2012

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New measurements

CP asymmetry in $B \rightarrow \Psi\pi$

350 pb⁻¹

preliminary

LHCb-PAPER-2011-024

to be submitted to Phys.Rev.X

CP violation in $B \rightarrow K\pi$

350 pb⁻¹

[arXiv:1202.6251](https://arxiv.org/abs/1202.6251)

submitted to Phys.Rev.Lett

CP violation in $B \rightarrow D\bar{K}$

1.0 fb⁻¹ (full 2011 data)

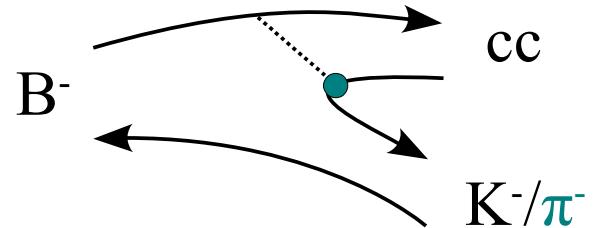
preliminary

LHCb-PAPER-2012-001

to be submitted to Phys.Lett.B

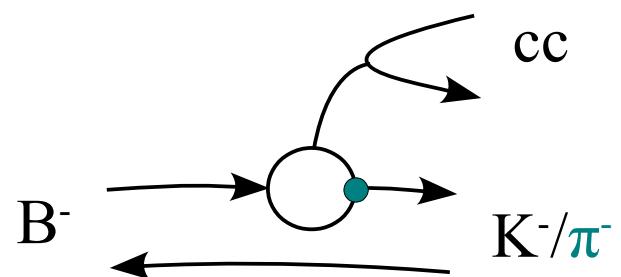
$B^- \rightarrow \psi h^-$

- $B^- \rightarrow J/\psi K^-$
 - abundant
 - Tree and Penguin have **same** weak phase
→ no CP violation expected, none found [PDG]
- $B^- \rightarrow J/\psi \pi^-$
 - Tree and Penguin have **different** weak phases, contribution may be $A_{CP} \sim 10^{-3}$
 - Decay is Cabibbo suppressed.
- $B^- \rightarrow \psi(2S) K/\pi$
 - less well explored



$$V_{cb} V_{cs} \sim A \lambda^2$$

$$V_{cb} V_{cd} \sim A \lambda^3$$



$$V_{tb} V_{ts} \sim A \lambda^2$$

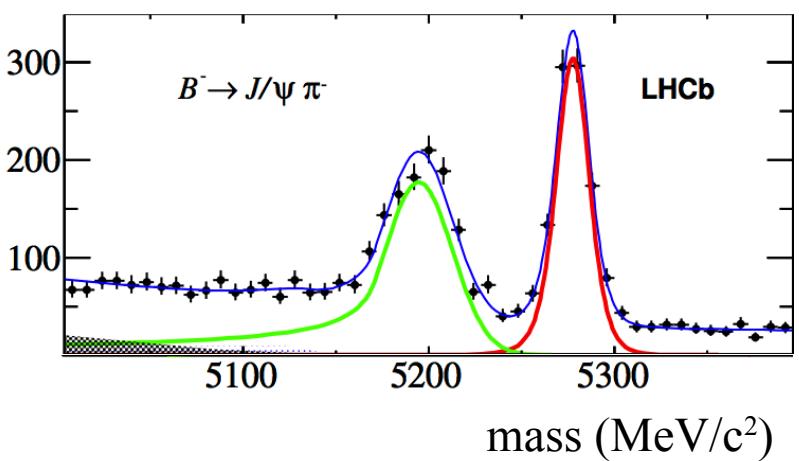
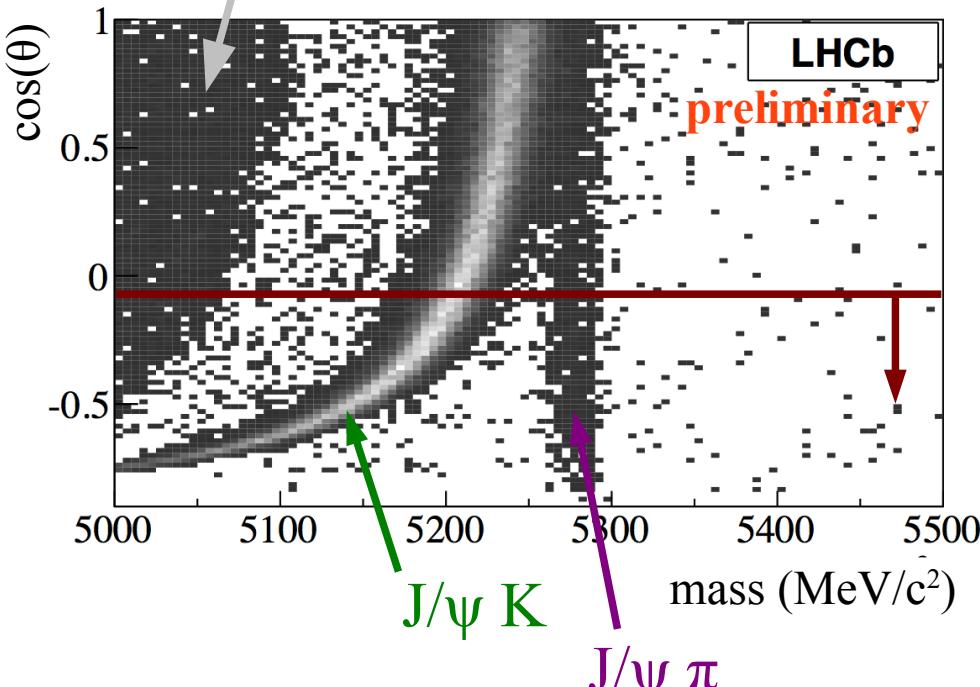
$$V_{tb} V_{td} \sim A \lambda^3 (1 - \rho - \eta)$$

$B^- \rightarrow \psi h^-$

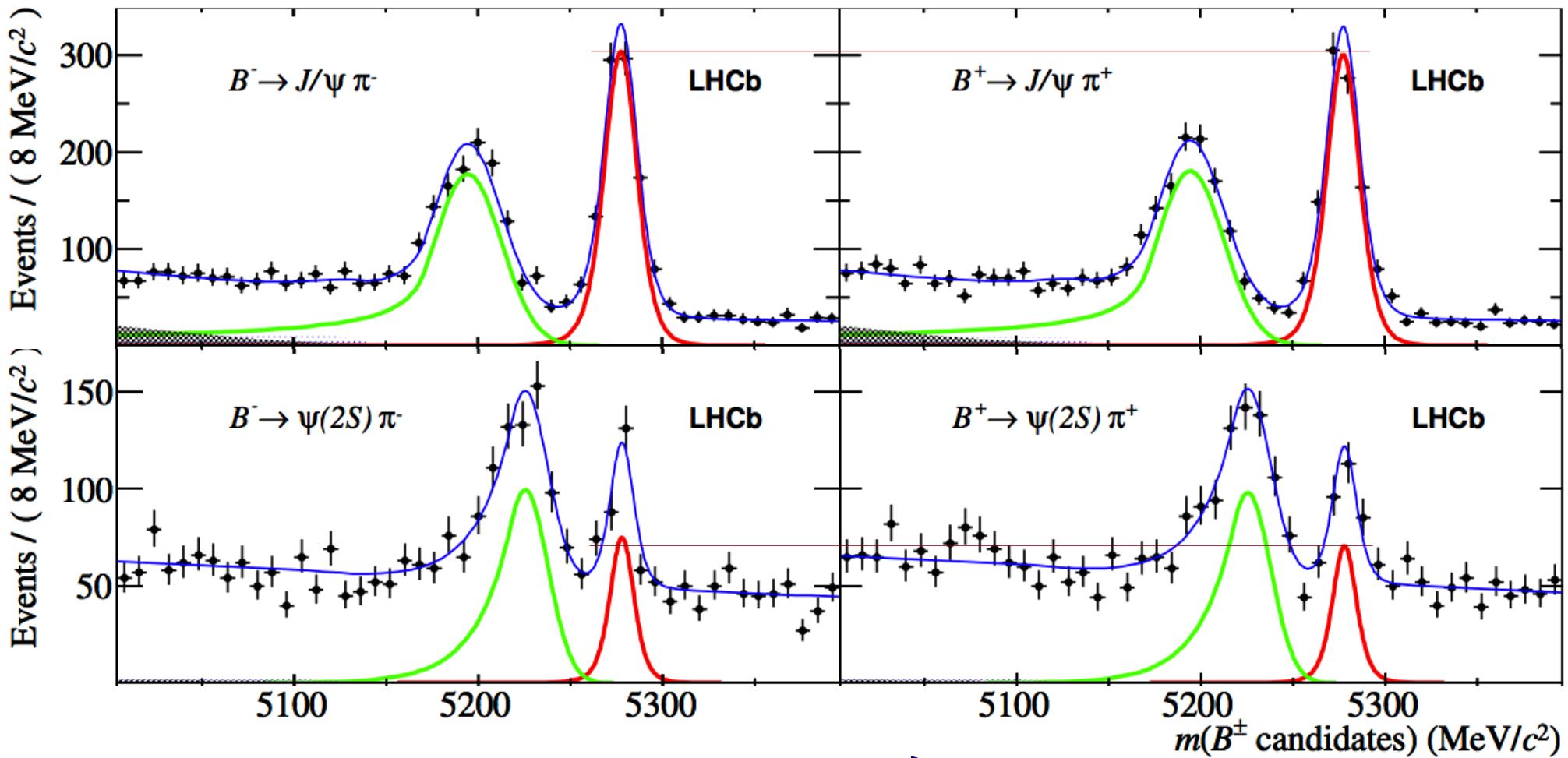
- Select ($\mu^+ \mu^- h^-$) candidates
- Separate $h = K, \pi$ by
 - helicity angle $\cos(\theta)$
 - RICH particle ID, split samples
- Simultaneous fit of 8 subsamples, extracting yields

$$R_\psi = \frac{\mathcal{B}(B^\pm \rightarrow \psi \pi^\pm)}{\mathcal{B}(B^\pm \rightarrow \psi K^\pm)}$$

$$A_{CP}^{\psi\pi} = \frac{\mathcal{B}(B^- \rightarrow \psi \pi^-) - \mathcal{B}(B^+ \rightarrow \psi \pi^+)}{\mathcal{B}(B^- \rightarrow \psi \pi^-) + \mathcal{B}(B^+ \rightarrow \psi \pi^+)}$$



$B^- \rightarrow \psi h^-$



$$\left. \begin{array}{lcl} A_{CP}^{J/\psi \pi^-} & = & 0.005 \pm 0.027 \pm 0.011 \\ A_{CP}^{\psi(2S)\pi^-} & = & 0.048 \pm 0.090 \pm 0.011 \\ A_{CP}^{\psi(2S)K^0} & = & 0.024 \pm 0.014 \pm 0.008 \end{array} \right\}$$

No evidence of CP violation.

$B_{(d,s)} \rightarrow K^- \pi^+$

350 pb⁻¹ @ 7 TeV

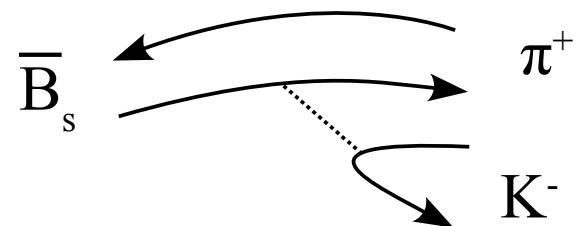
paper submitted to Phys.Rev.Lett.

arXiv:1202.6251

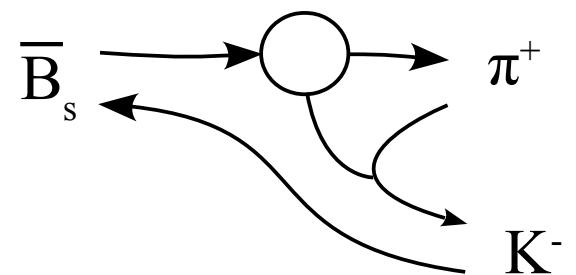
$$B_{(d,s)} \rightarrow K^- \pi^+$$

- Interference of tree and loop diagrams.
- Potentially sensitive to new physics.
- CP asymmetry in $B_d \rightarrow K\pi$ is established.
- Consider B_s system!
 - 14 times lower decay rate, 4 times lower production rate

$$A_{CP} = \frac{N(K^+ \pi^-) - N(K^- \pi^+)}{N(K^+ \pi^-) + N(K^- \pi^+)}$$



$$V_{ub} V_{cs} \sim A \lambda^3 (\rho - i \eta)$$



$$V_{tb} V_{td} \sim A \lambda^3 (1 - \rho - i \eta)$$

- Use RICH **particle ID** to define the charge subsamples.
 - carefully control the PID efficiencies and mis-ID rate from data:
large calibration samples of
 $D^* \rightarrow D\pi \rightarrow (K\pi)\pi$ and $\Lambda \rightarrow p\pi$ decays
- Use MC to predict **crossfeed** from $B \rightarrow \pi\pi$ and $B \rightarrow KK$
- Fits to the mass spectra to extract raw asymmetries:

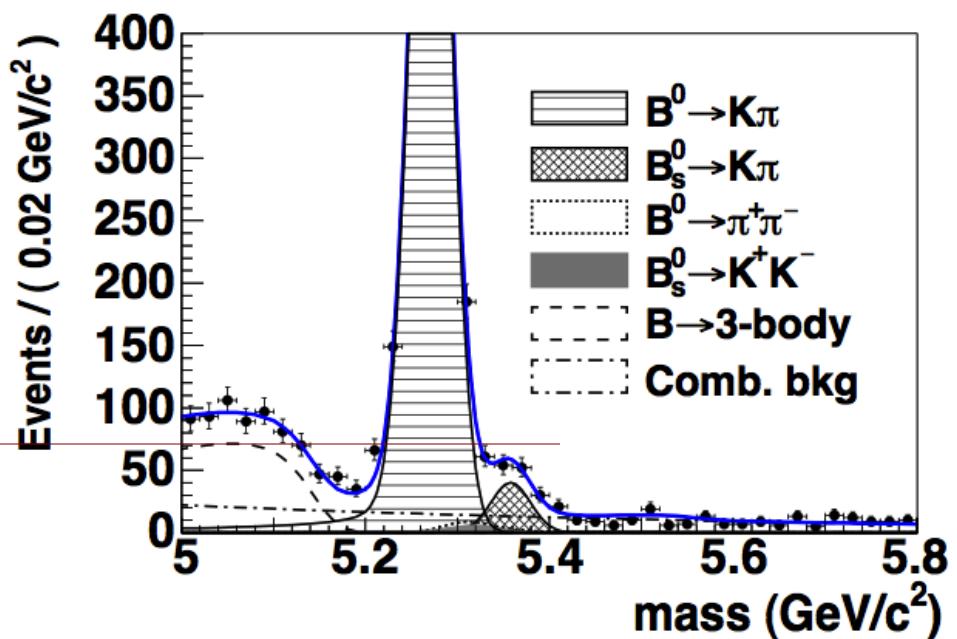
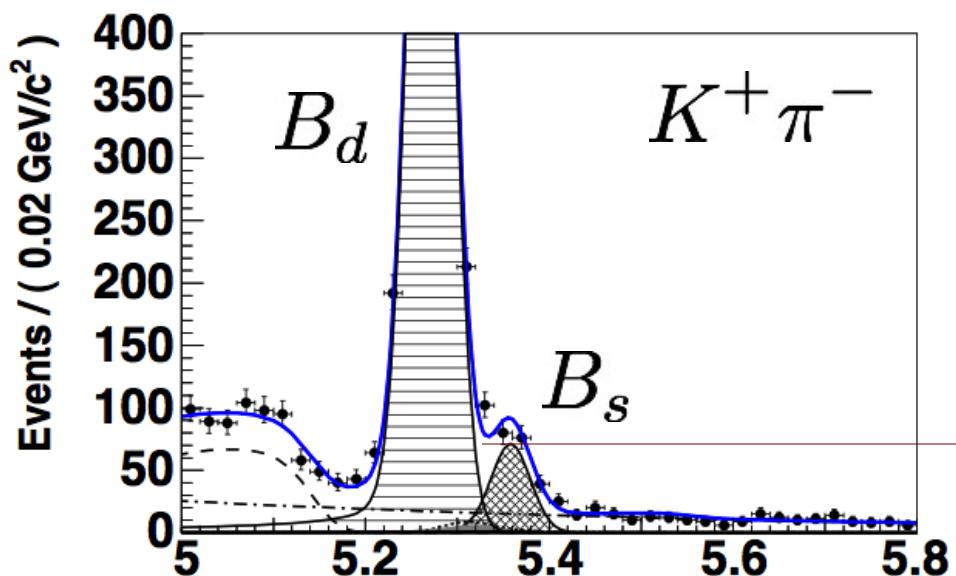
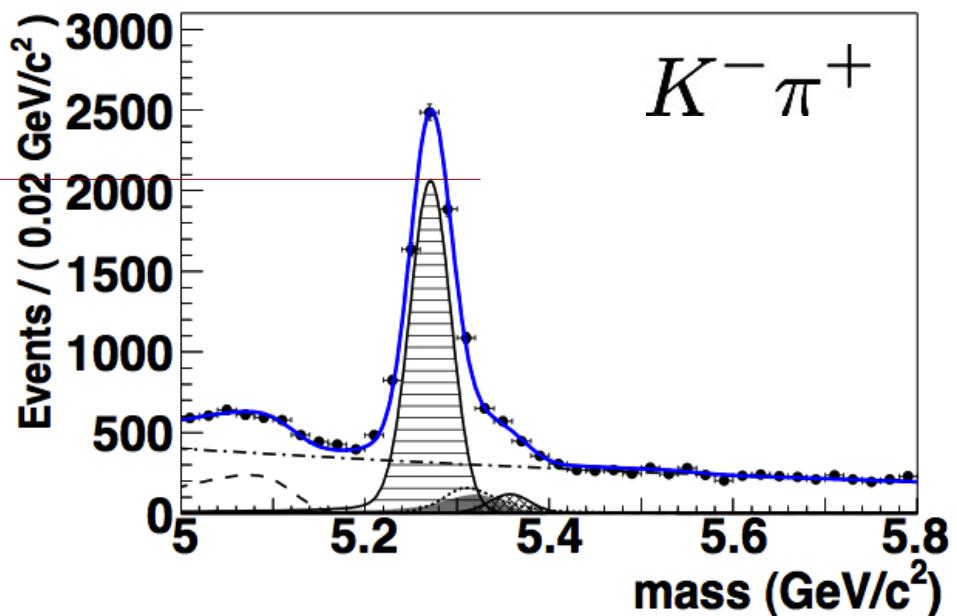
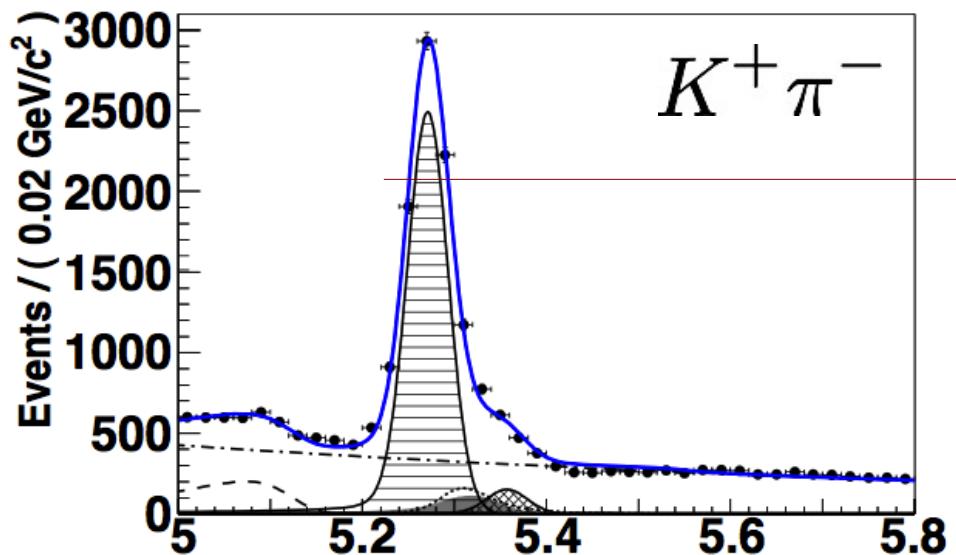
$$A_{\text{raw}}(B^0 \rightarrow K\pi) = -0.095 \pm 0.011$$

$$A_{\text{raw}}(B_s^0 \rightarrow K\pi) = \underline{0.28 \pm 0.08}$$

$B_{(d,s)} \rightarrow K^-\pi^+$

arXiv:1202.6251

LHCb
LHCb
~~FNAL~~



- Corrections:

$$A_{CP} = A_{\text{raw}} \pm A_D(K\pi) - \underbrace{\kappa_{d(s)} A_P(B_{(s)}^0)}_{\text{mixing}}$$

- detector asymmetry (from D^* samples): $A_D = -0.010 \pm 0.002$
- dilution due to B mixing:
 $\kappa_d = 0.303 \pm 0.005$
 $\kappa_s = -0.033 \pm 0.003$
- production asymmetry:
from $A_{\text{raw}}(B^0 \rightarrow J/\psi K^{*0})$ $A_p(B^0) = 0.010 \pm 0.0013$
- **total corrections:** $\Delta A_{CP}(B^0) = -0.007 \pm 0.006$
 $\Delta A_{CP}(B_s) = 0.010 \pm 0.002 (= -A_D)$

| Systematic uncertainty | $A_{CP}(B^0 \rightarrow K\pi)$ | $A_{CP}(B_s^0 \rightarrow K\pi)$ |
|------------------------------------------------------|--------------------------------|----------------------------------|
| ^(a) PID calibration | 0.0012 | 0.001 |
| ^(b) Final state radiation | 0.0026 | 0.010 |
| ^(b) Signal model | 0.0004 | 0.005 |
| ^(b) Combinatorial background | 0.0001 | 0.009 |
| ^(b) 3-body background | 0.0009 | 0.007 |
| ^(b) Cross-feed background | 0.0011 | 0.008 |
| ^(c) Instr. and prod. asym. (A_Δ) | 0.0078 | 0.005 |
| Total | 0.0084 | 0.019 |

Result

$$A_{CP}(B^0 \rightarrow K\pi) = -0.088 \pm 0.011 \text{ (stat)} \pm 0.008 \text{ (syst)}$$

Good agreement
with WA.

Most precise!

$$A_{CP}(B_s^0 \rightarrow K\pi) = 0.27 \pm 0.08 \text{ (stat)} \pm 0.02 \text{ (syst)}$$

First evidence of
CPV in last
neutral meson
system!



$B \rightarrow D\bar{K}$

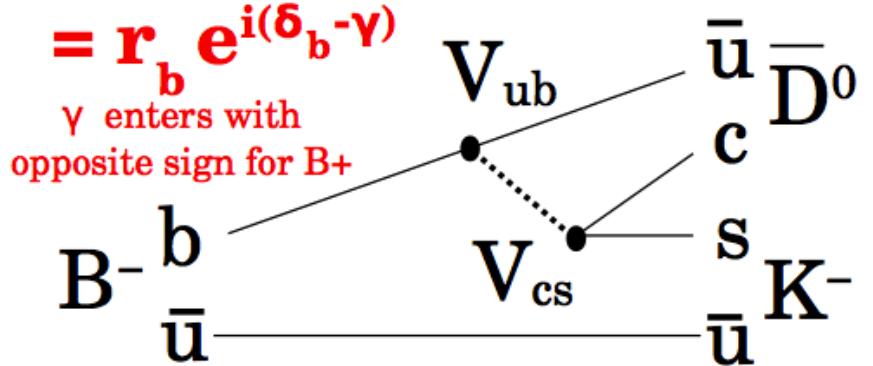
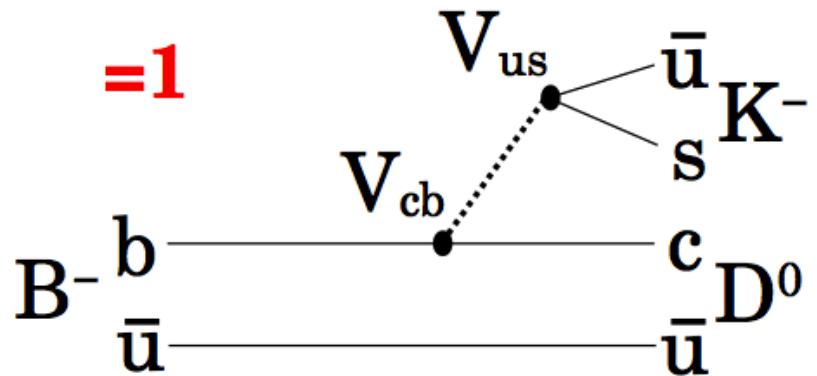
1.0 fb⁻¹ @ 7 TeV

paper to be submitted to PLB

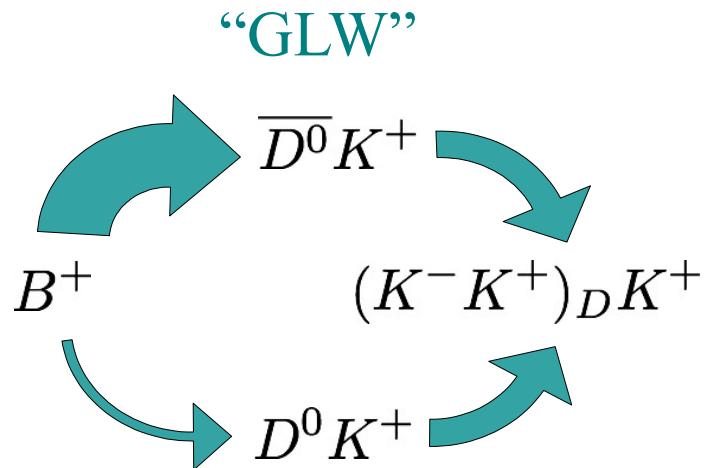
LHCb-PAPER-2012-001

$B \rightarrow DK$

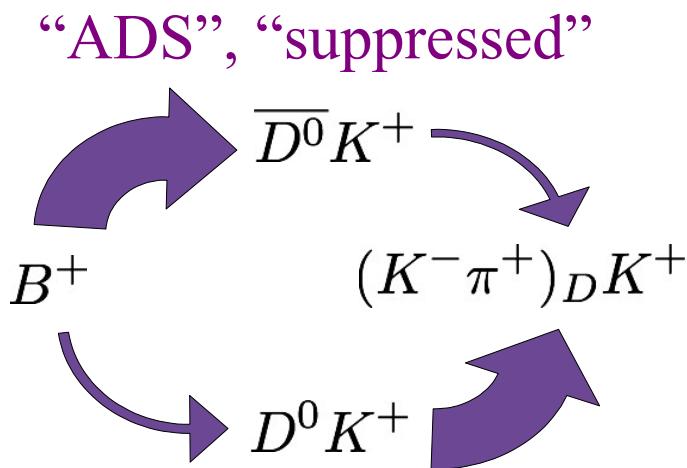
- Standard mode to measure weak phase γ .



- Tree decays, theoretically clean.

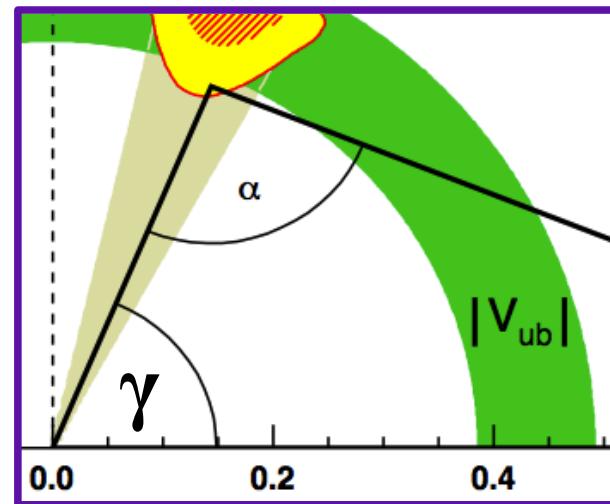


Phys.Lett. B253 (1991) 483
Phys.Lett. B265 (1991) 172



Phys.Rev.Lett 78 (1997) 3257
Phys.Rev. D63 (2001) 036005

$$\gamma = \arg \left(-\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right)$$



$B \rightarrow DK$: Observables

- Define observables as yield ratios (some systematics cancel).
- Charge **asymmetries**:

$$A_h^f = \frac{\Gamma(B^- \rightarrow [f]_D h^-) - \Gamma(B^+ \rightarrow [f]_D h^+)}{\Gamma(B^- \rightarrow [f]_D h^-) + \Gamma(B^+ \rightarrow [f]_D h^+)}$$

final states $[f]_D$:
 $KK, \pi\pi$
 $K\pi, \pi K$

- Charge averaged **Kaon/pion** ratio:

$$R_{K/\pi}^f = \frac{\Gamma(B^\pm \rightarrow [f]_D K^\pm)}{\Gamma(B^\pm \rightarrow [f]_D \pi^\pm)}$$

- **Suppressed/favored** decay ratio:

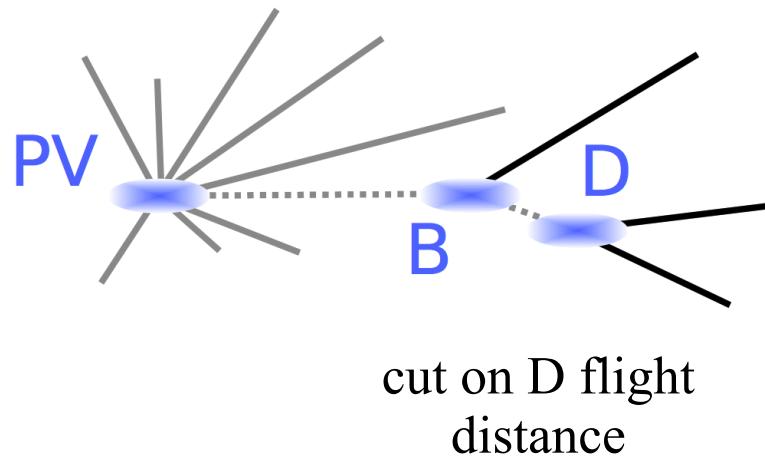
$$\begin{aligned} R_h^\pm &= \frac{\Gamma(B^\pm \rightarrow [\pi^\pm K^\mp]_D h^\pm)}{\Gamma(B^\pm \rightarrow [K^\pm \pi^\mp]_D h^\pm)} \\ &= r_B^2 + r_D^2 + 2r_B r_D \cos(\underbrace{\pm\gamma + \delta_B + \delta_D}_{\text{strong phase diff.}}) \end{aligned}$$

13 observables

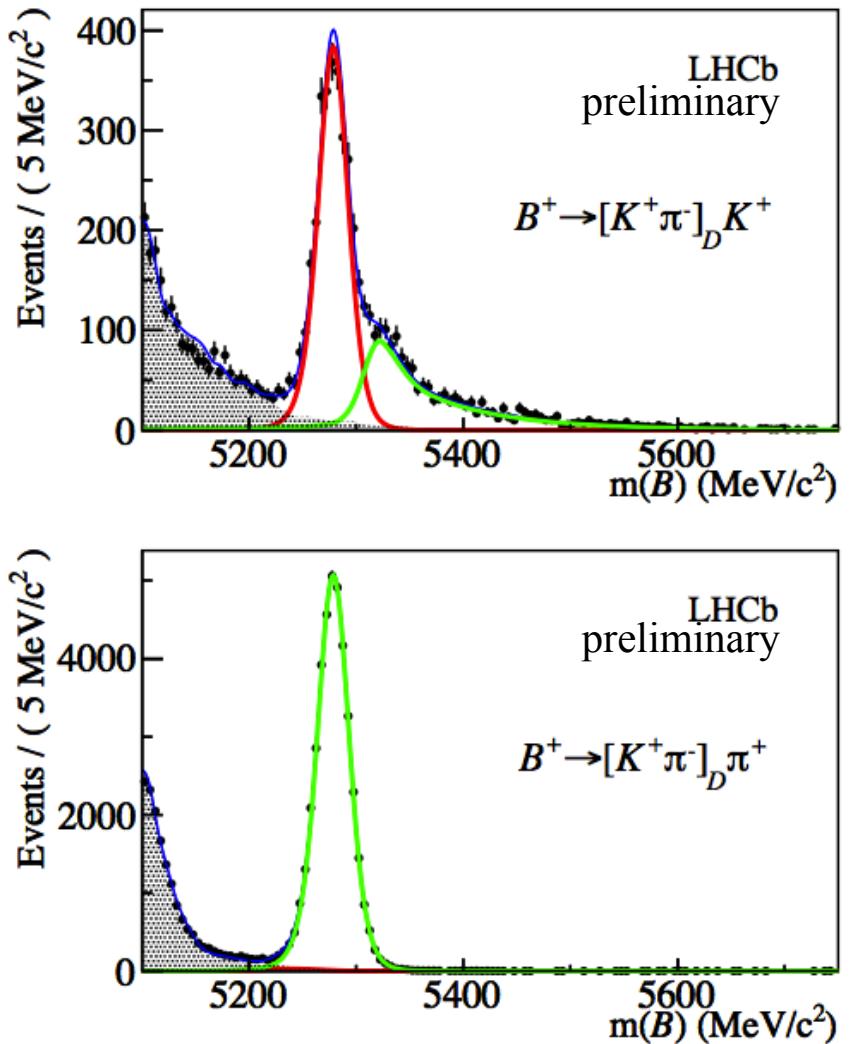
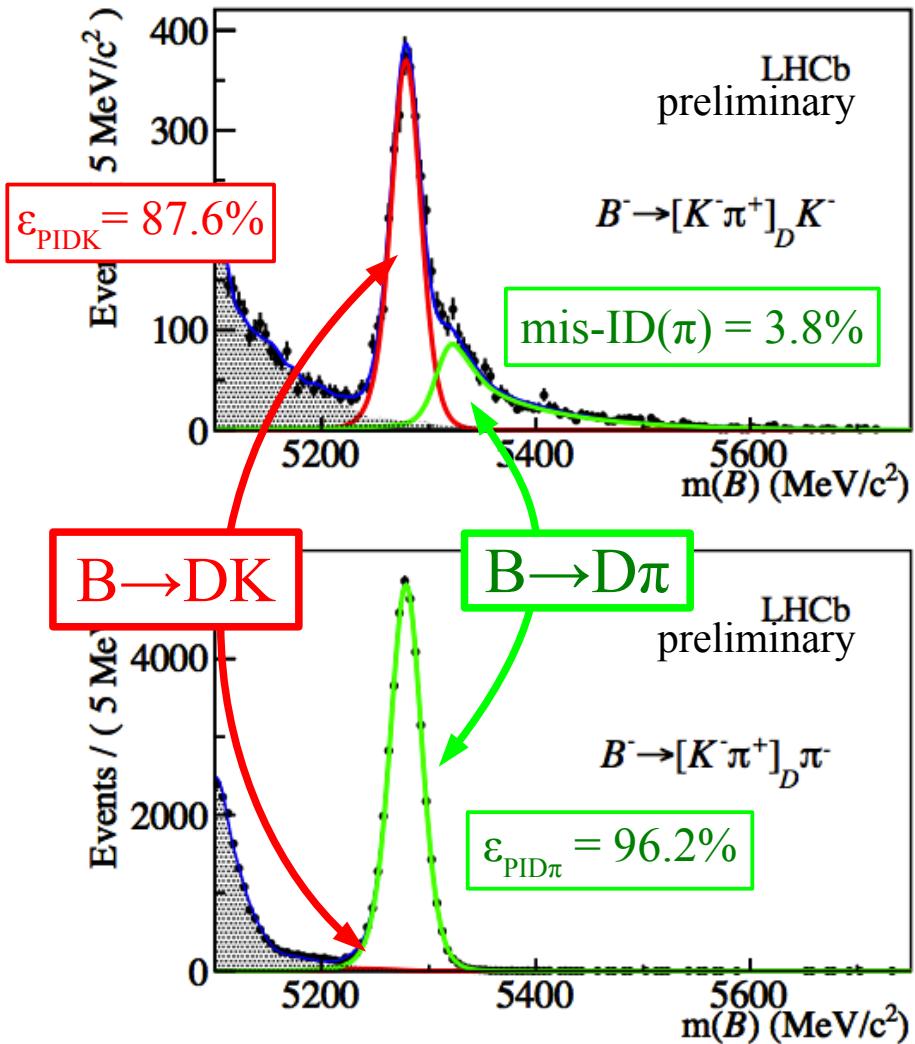
$B \rightarrow D\bar{K}$: Analysis method



- Most backgrounds are combinatorial multivariate analysis (BDT) with 20 variables
- Charmless backgrounds exploit large forward boost of the D
- Simultaneous fit on 16 slices
2 (charges) x 4 (D modes) x 2 (K/ π)
- Dominant systematics
intrinsic charge asymmetries (A_{CP})
particle ID ($R_{K\pi}$)

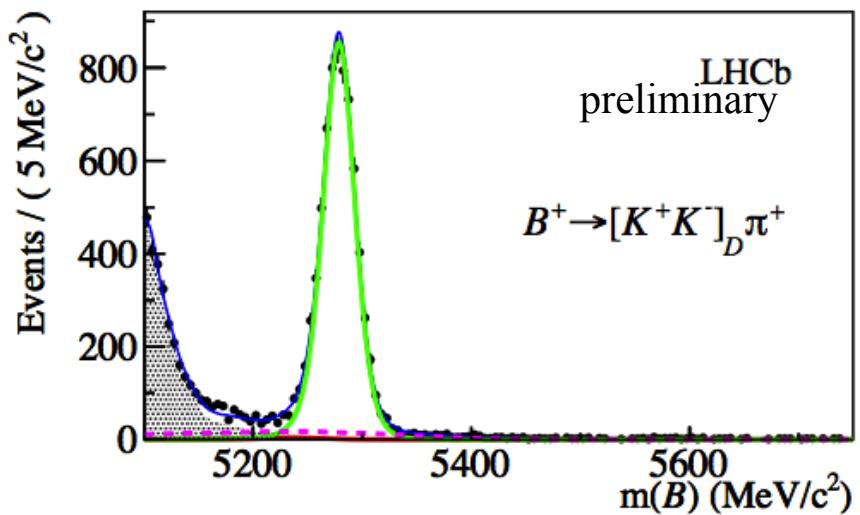
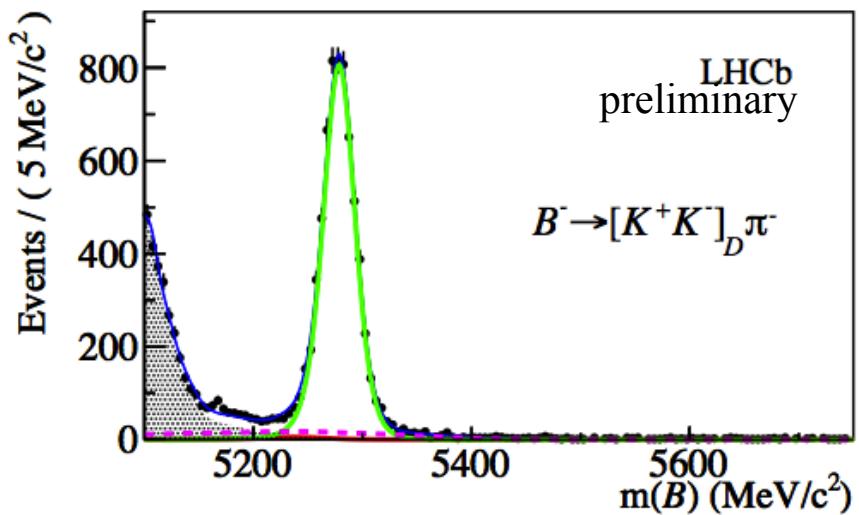
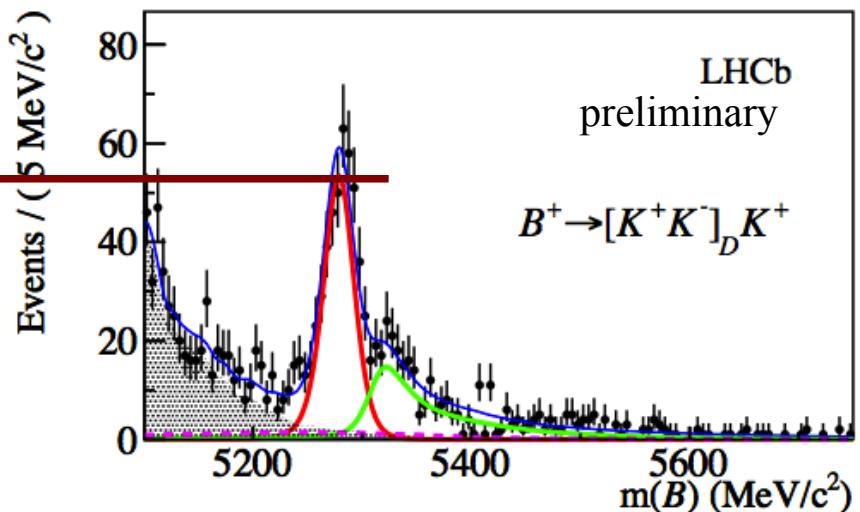
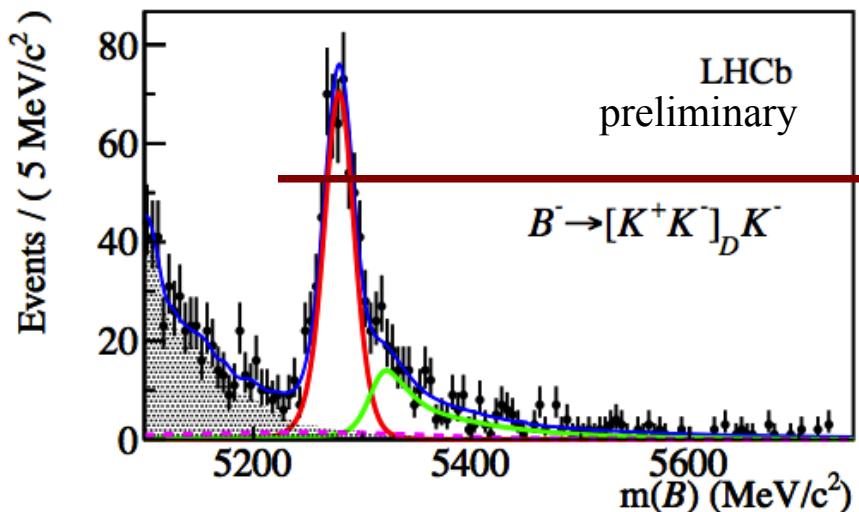


$B \rightarrow DK$: favored ADS mode



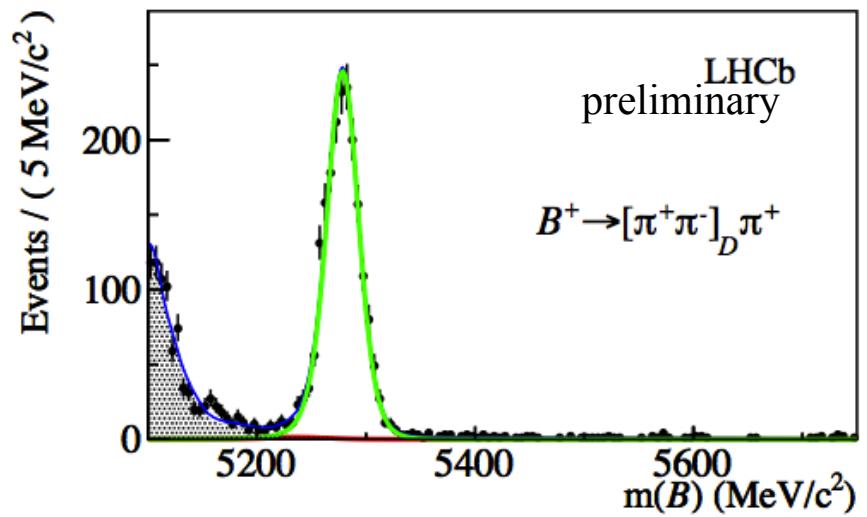
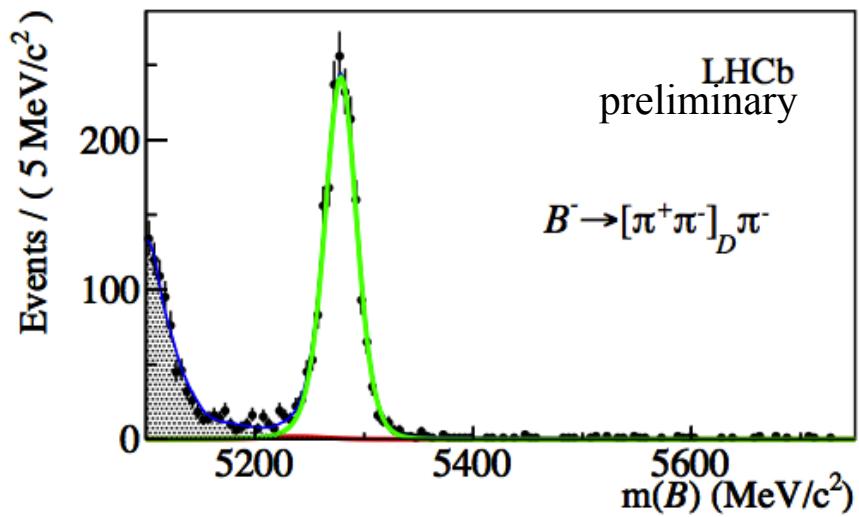
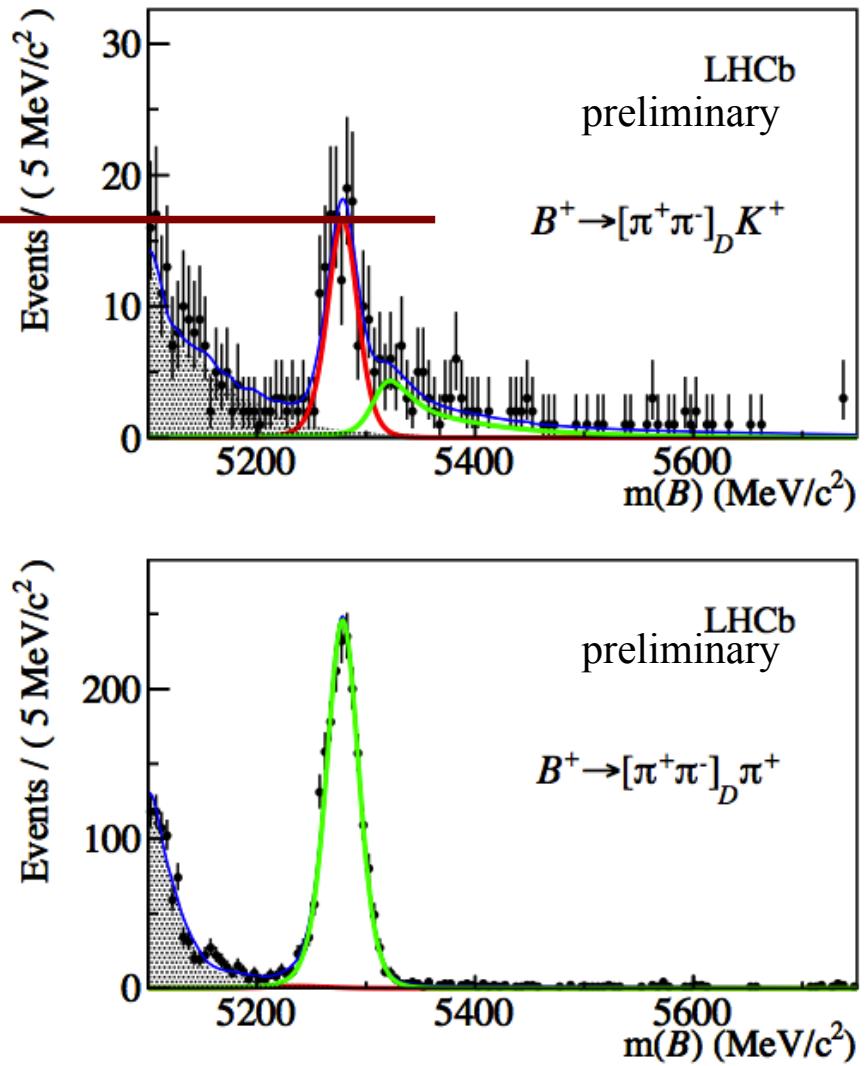
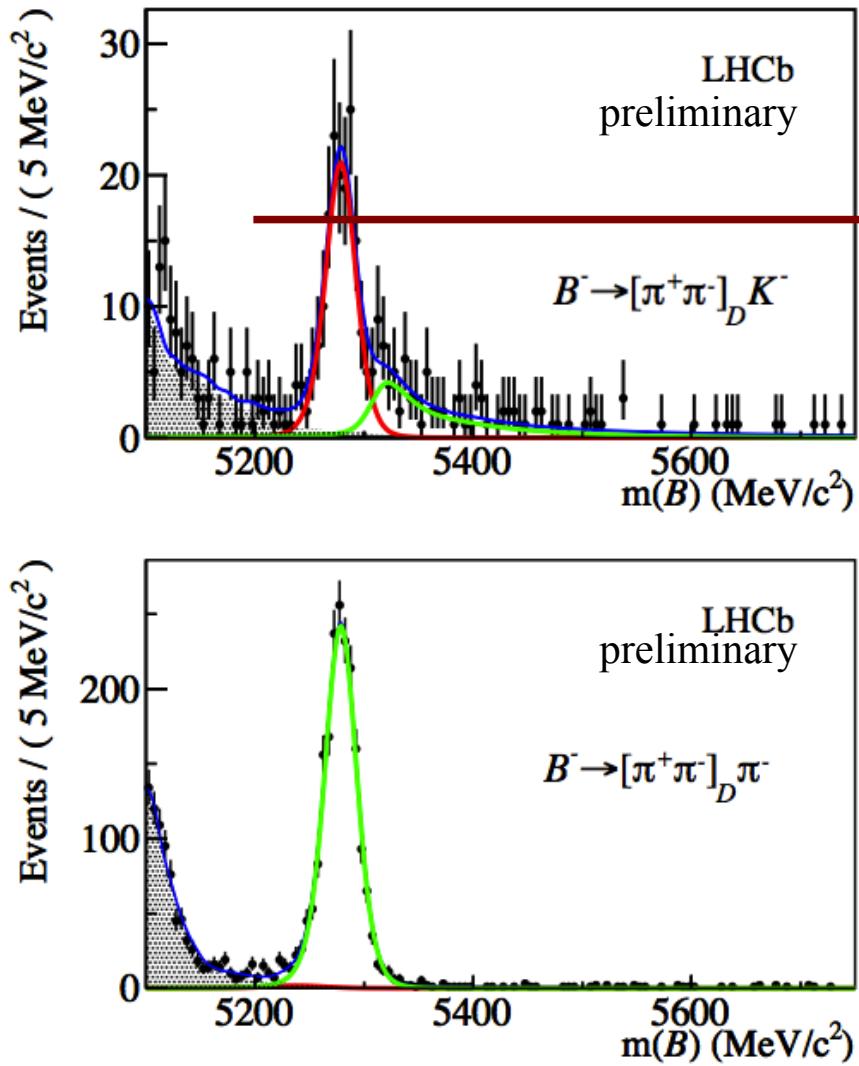
LHCb-PAPER-2012-001

$B \rightarrow DK$: GLW CP+ mode



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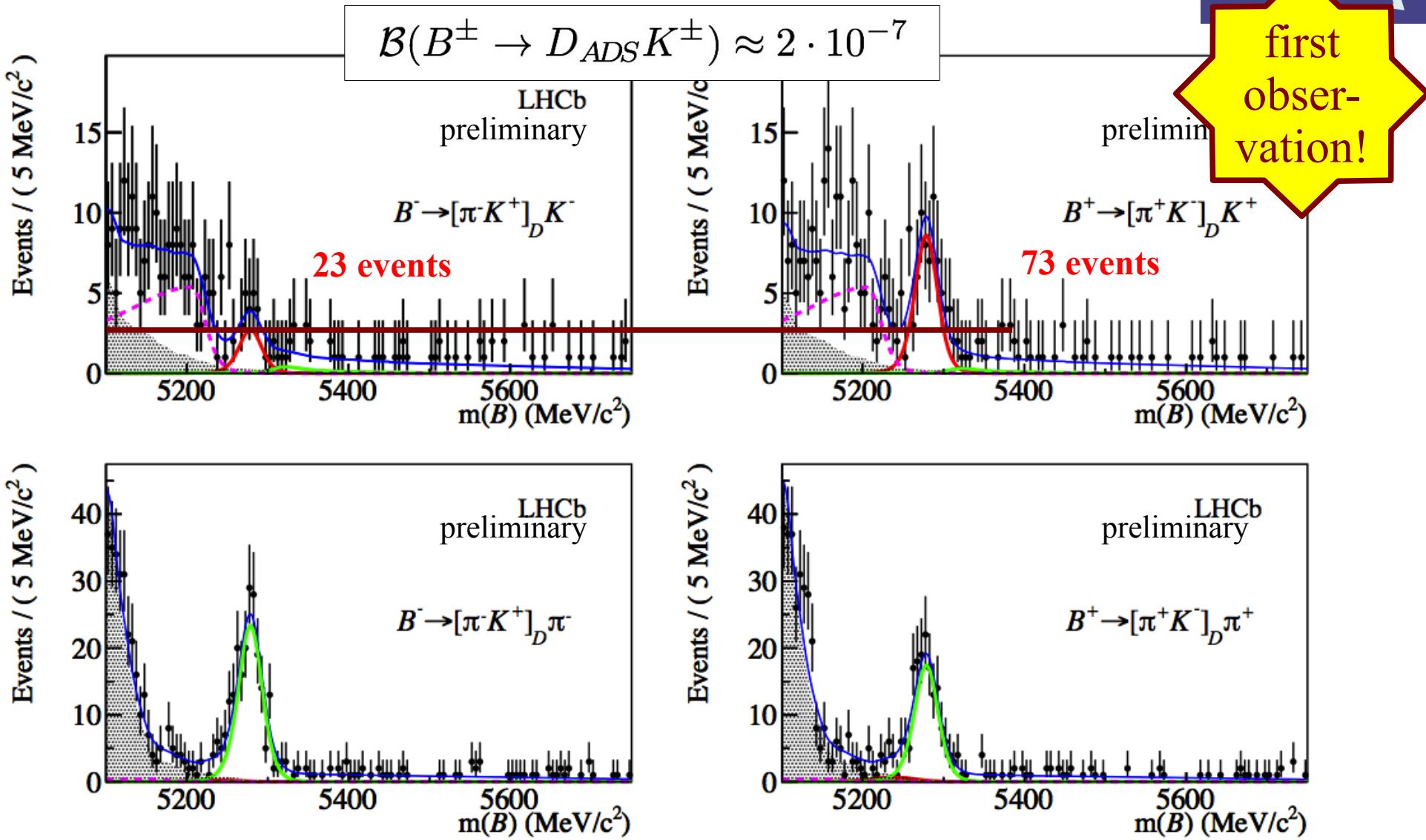
$B \rightarrow DK$: GLW CP+ mode (II)



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$B \rightarrow DK$: suppressed ADS mode

LHCb
FHCb



LHCb-PAPER-2012-001

B → DK: Results

$$R_{K/\pi}^{K\pi} = 0.0774 \pm 0.0012 \pm 0.0018$$

$$R_{K/\pi}^{KK} = 0.0773 \pm 0.0030 \pm 0.0018$$

$$R_{K/\pi}^{\pi\pi} = 0.0803 \pm 0.0056 \pm 0.0017$$

$$A_\pi^{K\pi} = -0.0001 \pm 0.0036 \pm 0.0095$$

$$A_K^{K\pi} = 0.0044 \pm 0.0144 \pm 0.0174$$

$$A_K^{KK} = 0.1480 \pm 0.0369 \pm 0.0097$$

$$A_K^{\pi\pi} = 0.1351 \pm 0.0661 \pm 0.0095$$

$$A_\pi^{KK} = -0.0199 \pm 0.0091 \pm 0.0116$$

$$A_\pi^{\pi\pi} = -0.0009 \pm 0.0165 \pm 0.0099$$

$$R_K^- = 0.0073 \pm 0.0023 \pm 0.0004$$

$$R_K^+ = 0.0232 \pm 0.0034 \pm 0.0007$$

$$R_\pi^- = 0.00469 \pm 0.00038 \pm 0.00008$$

$$R_\pi^+ = 0.00352 \pm 0.00033 \pm 0.00007$$

$B \rightarrow DK$: Results

| | | |
|----------------------|---|--------------------------------|
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$$R_{CP+} \approx \langle R_{K/\pi}^{\pi\pi}, R_{K/\pi}^{KK} \rangle / R_{K/\pi}^{K\pi} = 1.007 \pm 0.038 \pm 0.012$$

The GLW
charge-averaged ratio,
D(CP) over D(flavor).

B → DK: Results

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The GLW
charge asymmetry

$$A_{CP+} \approx < A_{K/\pi}^{\pi\pi}, A_{K/\pi}^{KK} > = 0.145 \pm 0.032 \pm 0.010$$



B → DK: Results

$$R_{K/\pi}^{K\pi} = 0.0774 \pm 0.0012 \pm 0.0018$$

$$R_{K/\pi}^{KK} = 0.0773 \pm 0.0020 \pm 0.0019$$

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$$R_{ADS(K)} = 0.0152 \pm 0.0020 \pm 0.0004$$

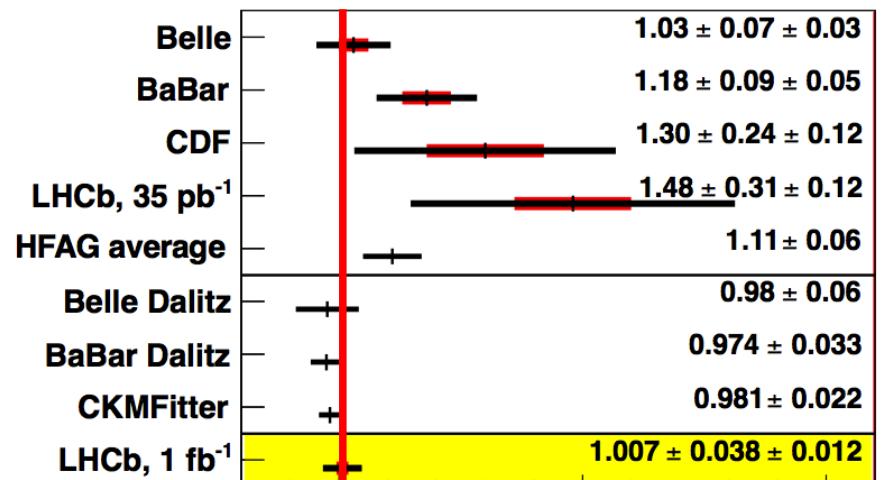
$$A_{ADS(K)} = -0.520 \pm 0.150 \pm 0.021$$

10 σ

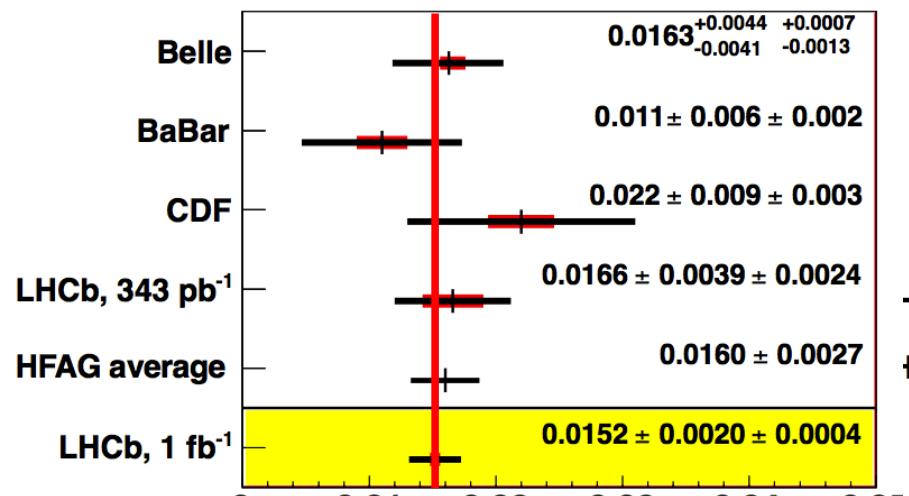
4 σ

2.4 σ

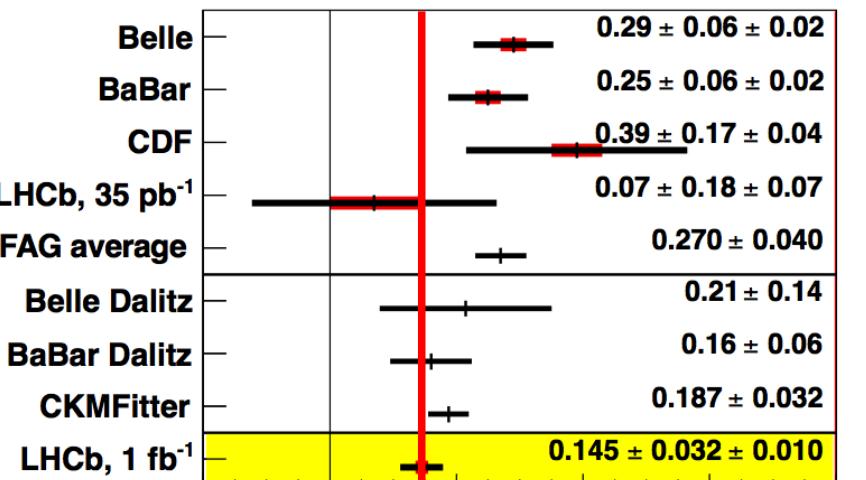
The ADS observables



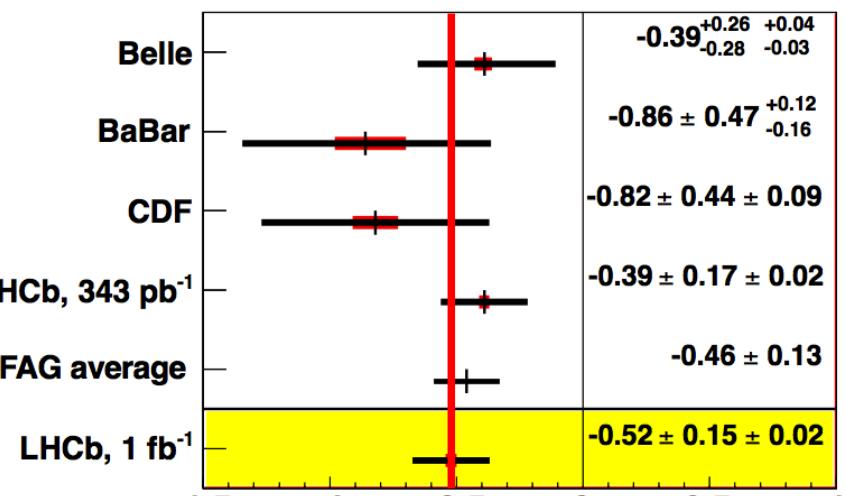
R_{CP+}



R_{ADS}



A_{CP+}



A_{ADS}

Conclusion

- CP asymmetry in $B \rightarrow \psi\pi$

No evidence for CP violation.

350 pb⁻¹ @ 7 TeV

to be submitted to Phys.Rev.X
 LHCb-PAPER-2011-024
 preliminary

- CP violation in $B \rightarrow K\pi$

First evidence of CPV in B_s !

$$A_{CP}(B_s^0 \rightarrow K\pi) = 0.27 \pm 0.08 \text{ (stat)} \pm 0.02 \text{ (syst)}$$



350 pb⁻¹ @ 7 TeV

submitted to Phys.Rev.Lett.
 arXiv:1202.6251

- CP violation in $B \rightarrow D\bar{K}$

$$A_{ADS(K)} = -0.520 \pm 0.150 \pm 0.021$$



1.0 fb⁻¹ @ 7 TeV

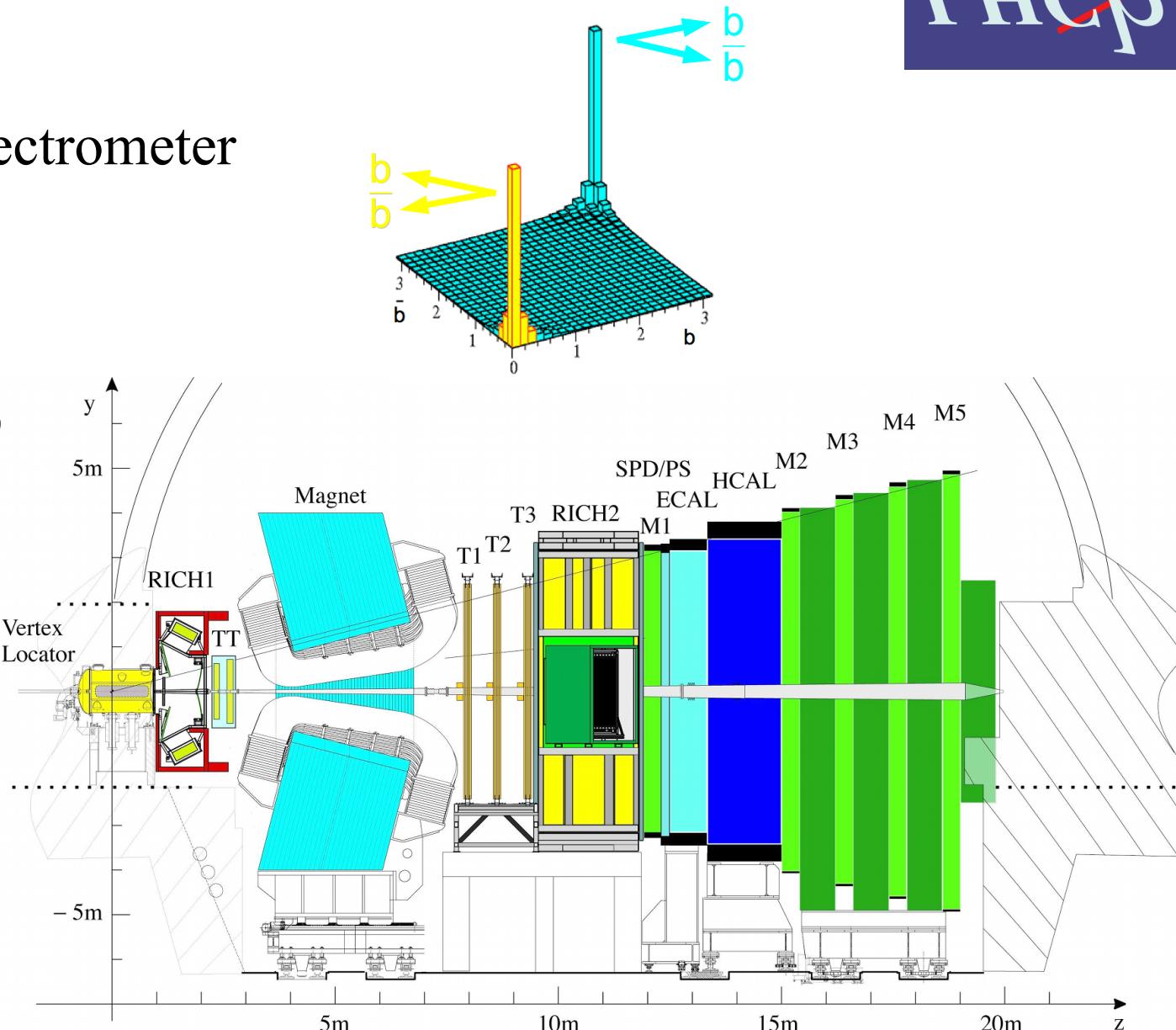
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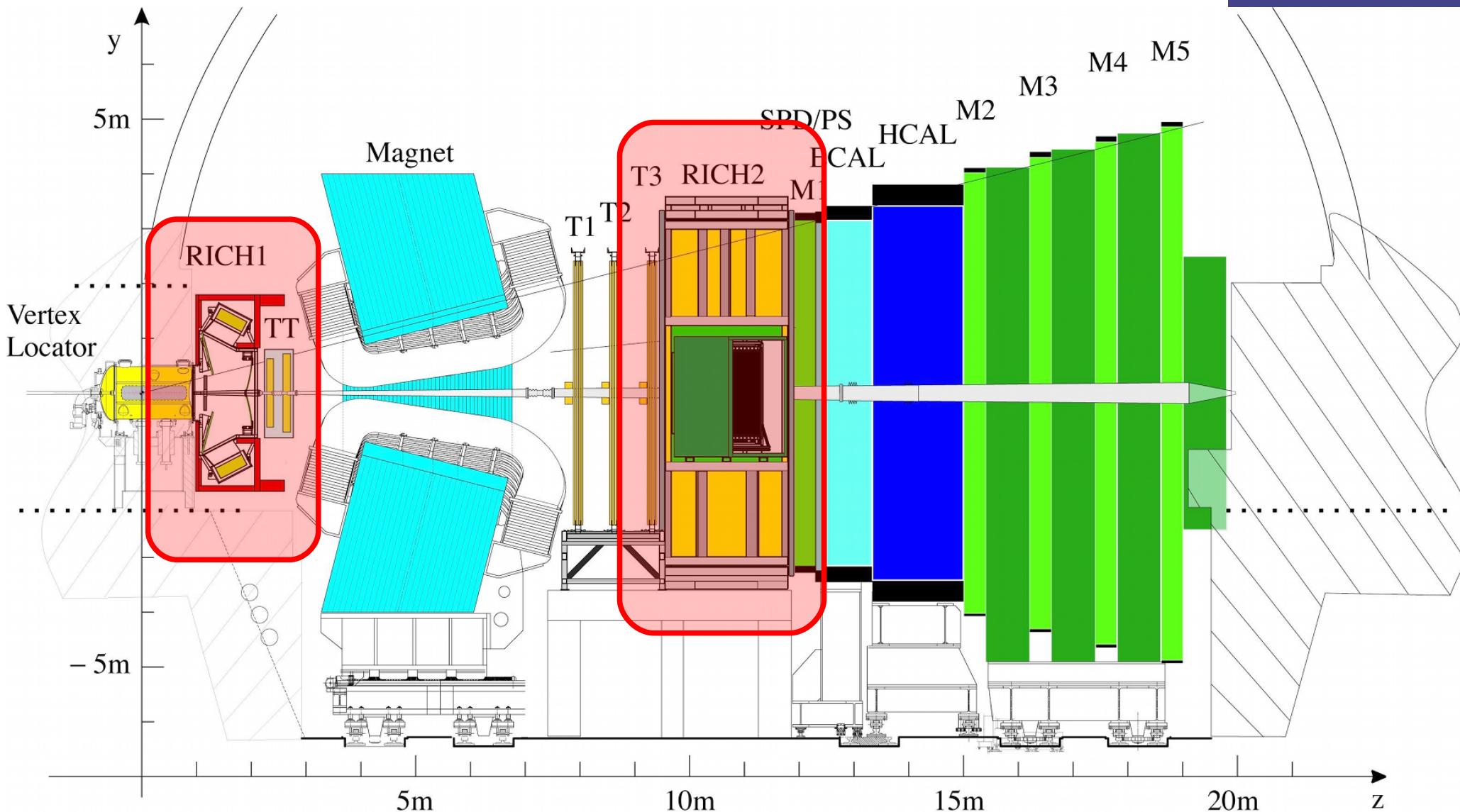
First observation of ADS mode!



Backup.

- one arm forward spectrometer
- b pair production correlated
- covers $1.9 < \eta < 4.9$
- tracking stations before and after magnet
- particle identification by two RICH detectors

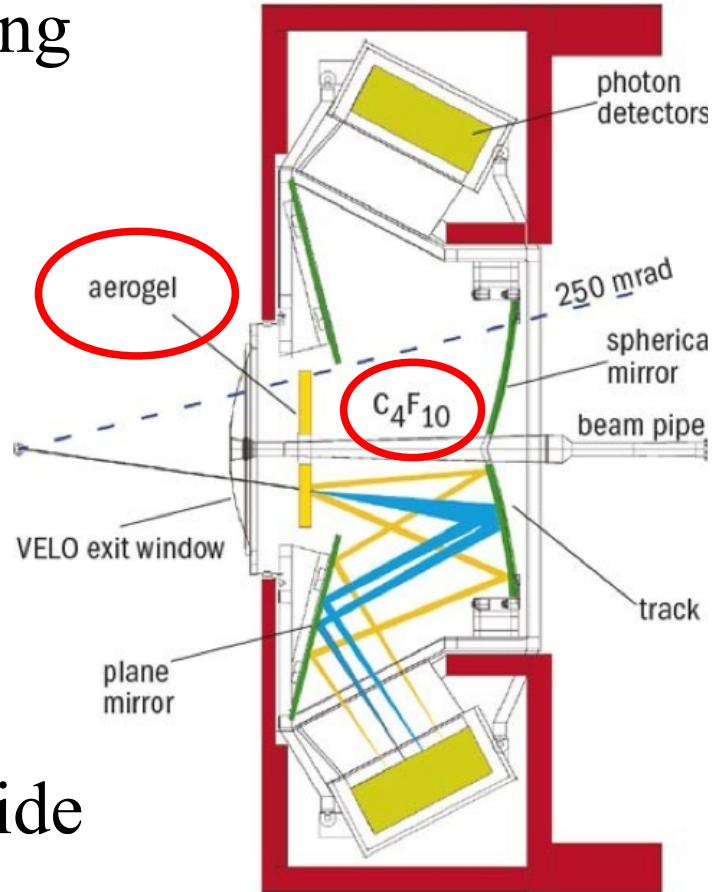




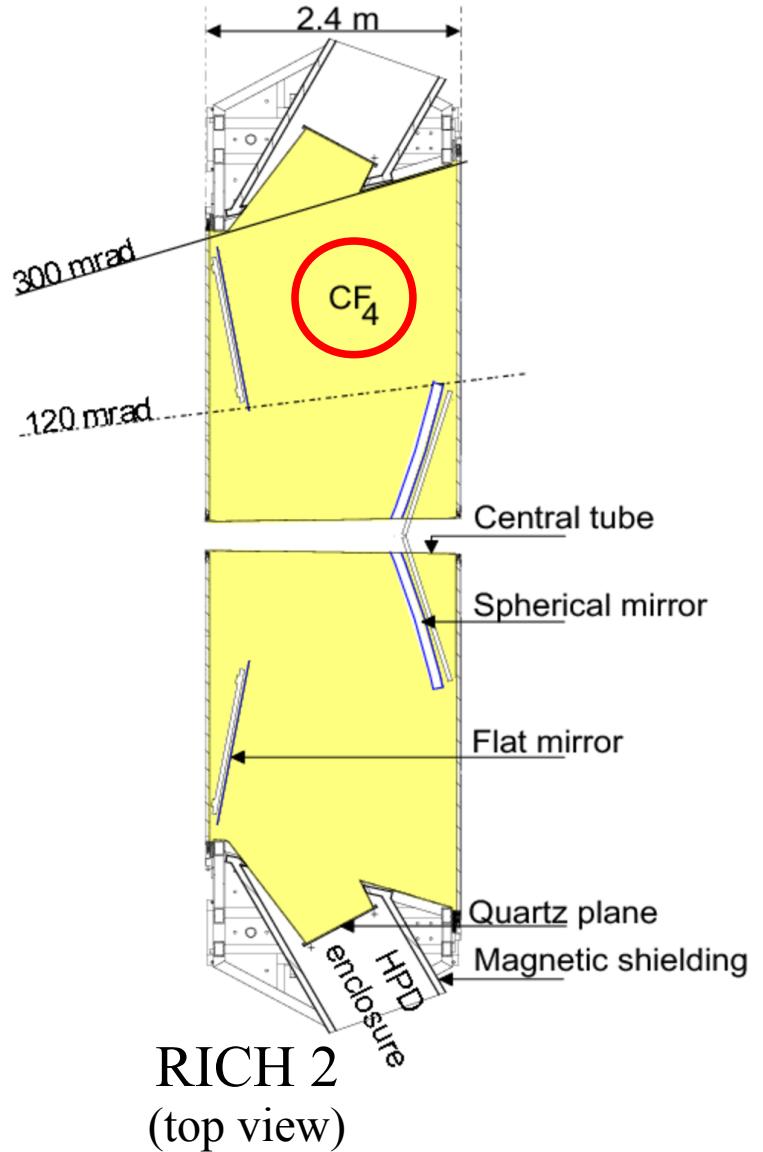
PID system

- Ring Imaging Cherenkov Detectors

$$\cos \theta = \frac{1}{\beta n}$$

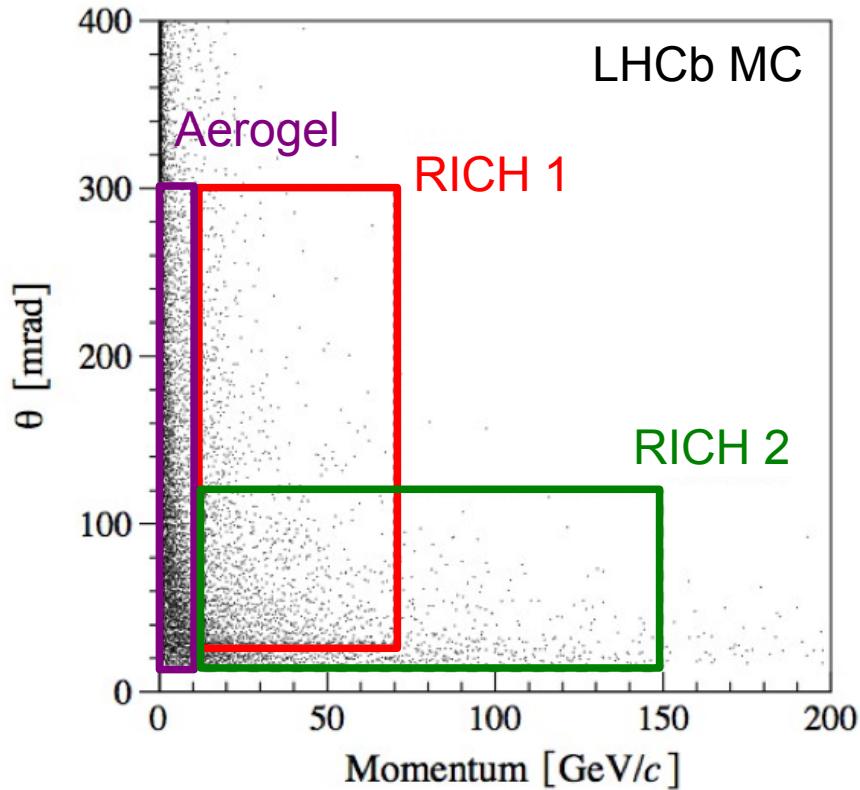


RICH 1
 (side view)

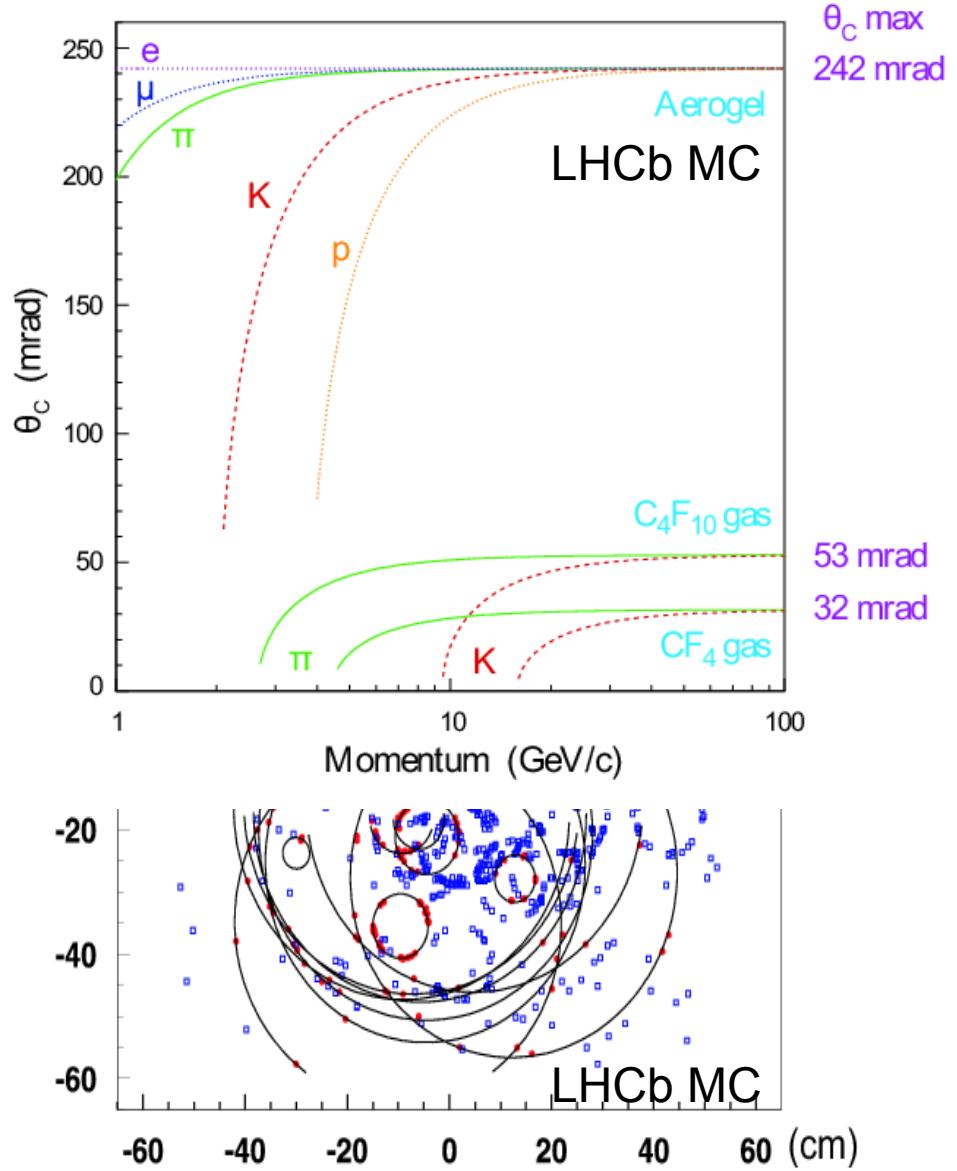


RICH 2
 (top view)

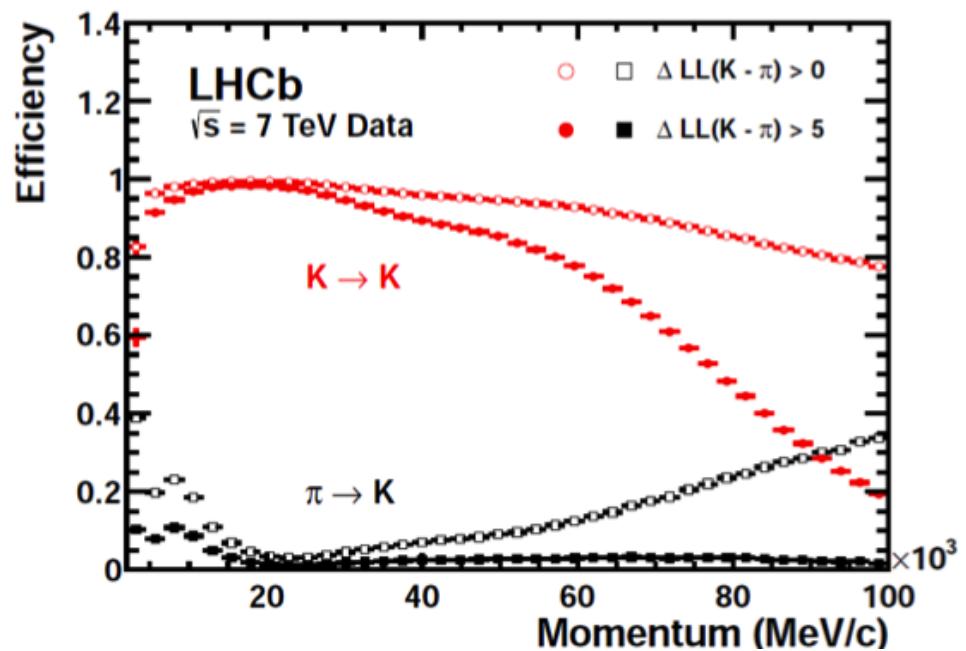
PID system



- Aerogel, $n = 1.03$, $p < 10 \text{ GeV}/c$
- C_4F_{10} , $n = 1.0014$, p intermediate
- CF_4 , $n = 1.0005$, $p > 20 \text{ GeV}/c$
[comparison: Air, $n = 1.0003$]



PID system



$B^- \rightarrow \psi h^-$

$$R^{J/\psi} = (3.83 \pm 0.11 \pm 0.07) \times 10^{-2} \longrightarrow \text{3}\sigma \text{ lower than WA}$$

$$(5.2 \pm 0.4) \times 10^{-2} \text{ [PDG]}$$

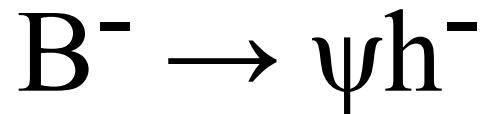
$$R^{\psi(2S)} = (3.95 \pm 0.40 \pm 0.12) \times 10^{-2} \longrightarrow \text{compatible w/ Belle}$$

$$(3.99 \pm 0.36 \pm 0.17) \times 10^{-2} \text{ [6]}$$

- [6] Belle collaboration, V. Bhardwaj *et al.*, *Observation of $B^\pm \rightarrow \psi(2S)\pi^\pm$ and search for direct CP-violation*, Phys.Rev. **D78** (2008) 051104, arXiv:0807.2170.

$$\mathcal{B}(B^\pm \rightarrow J/\psi \pi^\pm) = (3.88 \pm 0.11 \pm 0.15) \times 10^{-5}$$

$$\mathcal{B}(B^\pm \rightarrow \psi(2S)\pi^\pm) = (2.52 \pm 0.26 \pm 0.15) \times 10^{-5}$$



Systematics

Table 3: A summary of systematic uncertainties. The fit errors are included for comparison.

| | $R^{J/\psi} (\times 10^{-2})$ | $A^{J/\psi \pi}$ | $R^{\psi(2S)} (\times 10^{-2})$ | $A^{\psi(2S)\pi}$ | $A^{\psi(2S)K}$ |
|-----------------------------------------------|-------------------------------|------------------|---------------------------------|-------------------|-----------------|
| Simulation uncertainty | 0.045 | - | 0.088 | - | - |
| PID efficiencies | 0.043 | - | 0.052 | - | - |
| $A^{J/\psi K}$ (PDG [3]) | - | 0.0070 | - | 0.0070 | 0.0070 |
| $A_{\text{Raw}}^{J/\psi K}$ statistical error | - | 0.0046 | - | 0.0046 | 0.0046 |
| Detection asymmetries | - | 0.0056 | - | 0.0056 | - |
| Relative trigger efficiency | 0.020 | 0.0031 | 0.050 | 0.0036 | 0.0003 |
| Fixed fit parameters | 0.005 | 0.0006 | 0.017 | 0.0013 | 0.0001 |
| Sum in quadrature (syst.) | 0.065 | 0.0106 | 0.115 | 0.0108 | 0.0084 |
| Fit error (stat.) | 0.110 | 0.0268 | 0.404 | 0.0901 | 0.0136 |

B mixing dilution factor:

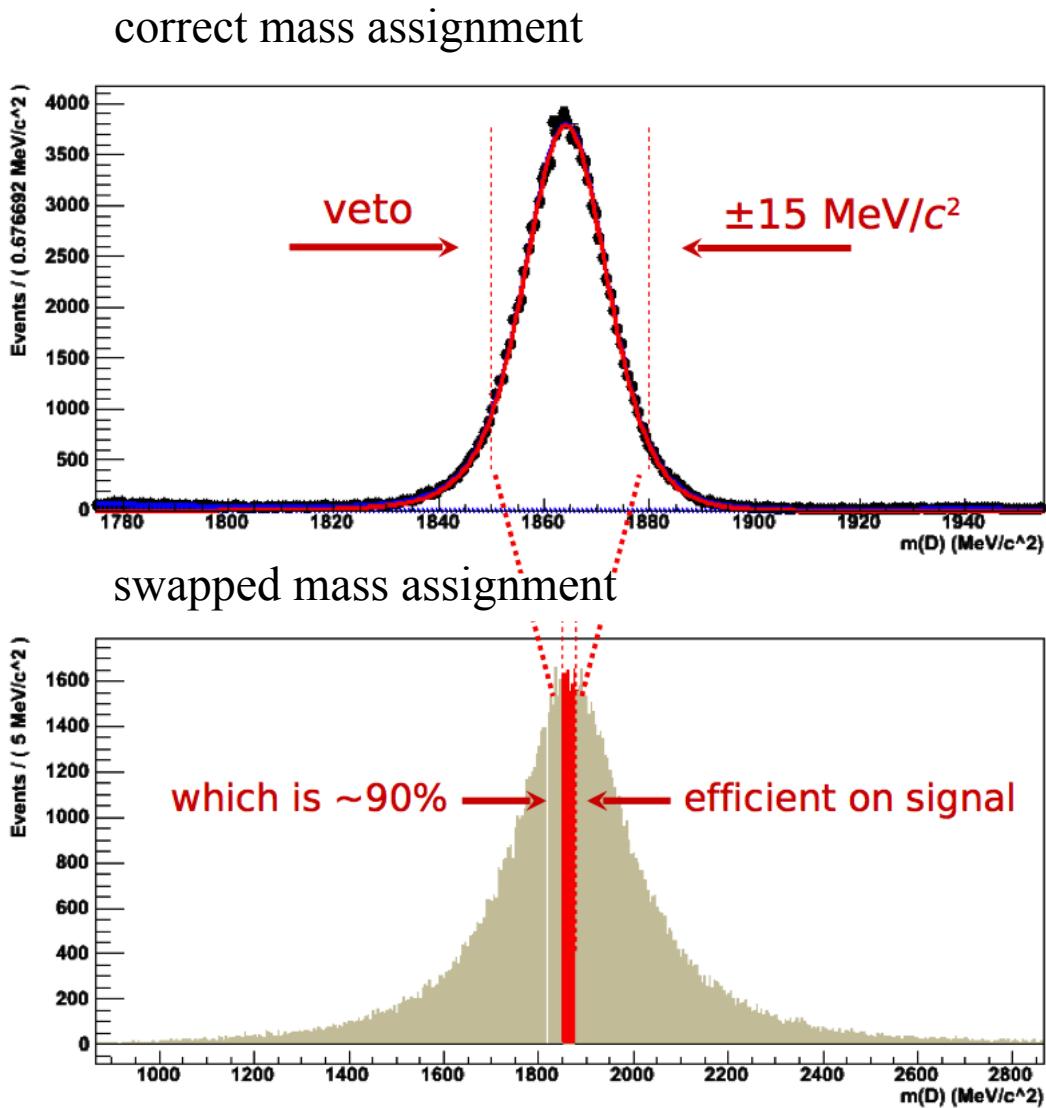
$$A_{CP}^{\text{int}} = \frac{\int \Gamma(B)dt - \int \Gamma(\bar{B})dt}{\int \Gamma(B)dt + \int \Gamma(\bar{B})dt}$$

$$\kappa_{d(s)} = \frac{\int_0^\infty e^{-\Gamma_{d(s)}t} \cos(\Delta m_{d(s)} t) \varepsilon(B_{(s)}^0 \rightarrow K\pi; t) dt}{\int_0^\infty e^{-\Gamma_{d(s)}t} \cosh\left(\frac{\Delta\Gamma_{d(s)}}{2}t\right) \varepsilon(B_{(s)}^0 \rightarrow K\pi; t) dt}$$

$B_{(d,s)} \rightarrow K^- \pi^+$: Crossfeeds

Double mis-ID
veto

$B^\pm \rightarrow [K\pi]h^\pm$
 $B^\pm \rightarrow [\pi K]h^\pm$



B → DK: Results

$$R_{K/\pi}^{K\pi} = 0.0774 \pm 0.0012 \pm 0.0018$$

$$R_{K/\pi}^{KK} = 0.0773 \pm 0.0030 \pm 0.0018$$

$$R_{K/\pi}^{\pi\pi} = 0.0803 \pm 0.0056 \pm 0.0017$$

$$A_\pi^{K\pi} = -0.0001 \pm 0.0036 \pm 0.0095$$

$$A_K^{K\pi} = 0.0044 \pm 0.0144 \pm 0.0174$$

$$A_K^{KK} = 0.1480 \pm 0.0369 \pm 0.0097$$

$$A_K^{\pi\pi} = 0.1351 \pm 0.0661 \pm 0.0095$$

$$A_\pi^{KK} = -0.0199 \pm 0.0091 \pm 0.0116$$

$$A_\pi^{\pi\pi} = -0.0009 \pm 0.0165 \pm 0.0099$$

$$R_K^- = 0.0073 \pm 0.0023 \pm 0.0004$$

$$R_K^+ = 0.0232 \pm 0.0034 \pm 0.0007$$

$$R_\pi^- = 0.00469 \pm 0.00038 \pm 0.00008$$

$$R_\pi^+ = 0.00352 \pm 0.00033 \pm 0.00007$$

CP asymmetries in favored modes **consistent with 0** (as expected).

$B \rightarrow DK$: Results

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preliminary



$$\begin{aligned} R_{ADS(K)} &= (R_K^- + R_K^+)/2 \\ &= 0.0152 \pm 0.0020 \pm 0.0004 \\ A_{ADS(K)} &= (R_K^- - R_K^+)/(R_K^- + R_K^+) \\ &= -0.520 \pm 0.150 \pm 0.021 \\ R_{ADS(\pi)} &= (R_\pi^- + R_\pi^+)/2 \\ &= 0.00410 \pm 0.00025 \pm 0.00005 \\ A_{ADS(\pi)} &= (R_\pi^- - R_\pi^+)/(R_\pi^- + R_\pi^+) \\ &= 0.1426 \pm 0.0621 \pm 0.0110 \end{aligned}$$

$B \rightarrow DK$: ADS relations



$$R_{\text{ADS}} = \frac{\Gamma(B^- \rightarrow D[\rightarrow K^+\pi^-]K^-) + \Gamma(B^+ \rightarrow D[\rightarrow K^-\pi^+]K^+)}{\Gamma(B^- \rightarrow D[\rightarrow K^-\pi^+]K^-) + \Gamma(B^+ \rightarrow D[\rightarrow K^+\pi^-]K^+)}$$
$$A_{\text{ADS}} = \frac{\Gamma(B^- \rightarrow D[\rightarrow K^+\pi^-]K^-) - \Gamma(B^+ \rightarrow D[\rightarrow K^-\pi^+]K^+)}{\Gamma(B^- \rightarrow D[\rightarrow K^+\pi^-]K^-) + \Gamma(B^+ \rightarrow D[\rightarrow K^-\pi^+]K^+)}$$

$$R_{\text{ADS}} = r_B^2 + r_D^2 + 2r_B r_D \cos \gamma \cos(\delta_B + \delta_D)$$

$$A_{\text{ADS}} = 2r_B r_D \sin \gamma \sin(\delta_B + \delta_D) / R_{\text{ADS}}$$

$$R_{\pm} \equiv \frac{\Gamma(B^\pm \rightarrow [K^\mp \pi^\pm]_D K^\mp)}{\Gamma(B^\pm \rightarrow [K^\pm \pi^\mp]_D K^\pm)} = r_B^2 + r_D^2 + 2r_B r_D \cos(\pm \gamma + \delta_B + \delta_D)$$

$B \rightarrow D K$: GLW relations



$$R_{CP\pm} = \frac{2[\Gamma(B^- \rightarrow D_{CP\pm} K^-) + \Gamma(B^+ \rightarrow D_{CP\pm} K^+)]}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)} = 1 + r_B^2 \pm 2r_B \cos \delta_B \cos \gamma$$
$$A_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm} K^-) - \Gamma(B^+ \rightarrow D_{CP\pm} K^+)}{\Gamma(B^- \rightarrow D_{CP\pm} K^-) + \Gamma(B^+ \rightarrow D_{CP\pm} K^+)} = \frac{\pm 2r_B \sin \delta_B \sin \gamma}{1 + r_B^2 \pm 2r_B \cos \delta_B \cos \gamma}$$

$B \rightarrow DK$: Systematics



| | PID | PDFs | MC | $A_{instr.}$ | $\sqrt{\sum \sigma_i^2}$ |
|----------------------|--------|--------|--------|--------------|--------------------------|
| $R_{K/\pi}^{K\pi}$ | 0.0014 | 0.0009 | 0.0008 | 0.0 | 0.0018 |
| $R_{K/\pi}^{KK}$ | 0.0013 | 0.0008 | 0.0009 | 0.0 | 0.0018 |
| $R_{K/\pi}^{\pi\pi}$ | 0.0013 | 0.0006 | 0.0008 | 0.0 | 0.0017 |
| $A_\pi^{K\pi}$ | 0.0 | 0.0010 | 0.0 | 0.0094 | 0.0095 |
| $A_K^{K\pi}$ | 0.0002 | 0.0041 | 0.0 | 0.0169 | 0.0174 |
| A_K^{KK} | 0.0016 | 0.0013 | 0.0005 | 0.0095 | 0.0097 |
| $A_K^{\pi\pi}$ | 0.0019 | 0.0023 | 0.0 | 0.0090 | 0.0095 |
| A_π^{KK} | 0.0001 | 0.0066 | 0.0 | 0.0095 | 0.0116 |
| $A_\pi^{\pi\pi}$ | 0.0001 | 0.0004 | 0.0 | 0.0099 | 0.0099 |
| R_K^- | 0.0002 | 0.0004 | 0.0 | 0.0001 | 0.0004 |
| R_K^+ | 0.0004 | 0.0005 | 0.0 | 0.0001 | 0.0007 |
| R_π^- | 1e-05 | 3e-05 | 0.0 | 7e-05 | 8e-05 |
| R_π^+ | 1e-05 | 3e-05 | 0.0 | 7e-05 | 7e-05 |