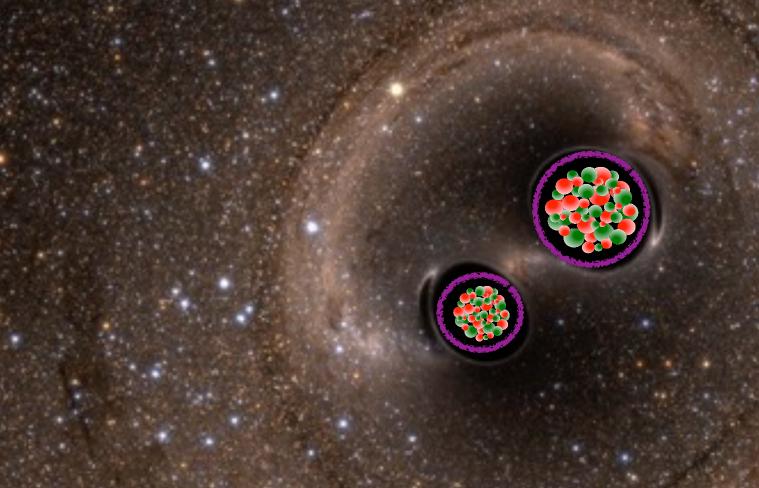
Holography and Black-Hole Microstate Structure



Second workshop on String Theory and GenderInstitut Henri Poincaré
Nick Warner, June 10, 2016

Research supported supported in part by DOE grant DE- SC0011687

Original photo credit: LIGO/Caltech

Outline: Holography and Black-Hole Microstate Structure

- Motivation and Challenges
- Microstate Geometries:

The only mechanism to avoid horizons

- Microstate Geometries as Holographic Phases
 - ★ New scales for Black Hole Physics
- Building BPS Microstate Geometries
 - ★ Scaling Microstate geometries
- Holography and Fluctuating Microstate Geometries
- Microstate Geometries as Backgrounds for New Physics
 - **★** W-branes

★ Tunneling

Motivation for Microstate Geometries I

General Relativity + Quantum mechanics ⇒

Non-unitary evolution arising from Hawking evaporation of black holes

An old conceit: Black hole evaporation time- scales are incredibly long: Fix with small corrections to GR?

e.g. via stringy or quantum gravity ($(Riemann)^n$) corrections to radiation?

New urgency

Mathur (2009): Using strong subadditivity of quantum information

 \Rightarrow There must be O(1) corrections to the Hawking states at the horizon

Microstate geometries/Fuzzballs

Find new structures and mechanisms in string theory that can address this issue by avoiding the formation of horizons

 $\underline{Microstate\ Geometry} \equiv Smooth, horizonless\ solutions\ to\ the\ bosonic\ sector$ of $\underline{supergravity}$ with the same asymptotic structure as a given black hole/ring

The Challenges for Horizon-Scale Structure

Old Story 1: Black-Hole Uniqueness (1960-1980's)

In General Relativity coupled to electromagnetism in 3+1 dimensions: Black holes are almost completely featureless

⇒ Microstate structure is invisible from outside the black hole

Once a black hole forms, matter (including a naive *firewall*) is swept away from horizon region in the light-crossing time of black hole ...

Old Story II: Solitons in GR

GR non-linearities:

Could there be interesting solitons = Smooth, classical lumps What could these represent in Nature?

Macroscopic/large scale, smooth, end-states for stars:

★ Time independent ★ Massless fields

In General Relativity coupled to massless fields:

Time-independent solutions with time-independent matter necessarily have horizons \Rightarrow They must have singularities

"No solitons without horizons"

Old Story III: The Fate of Weak-Coupling Resolutions

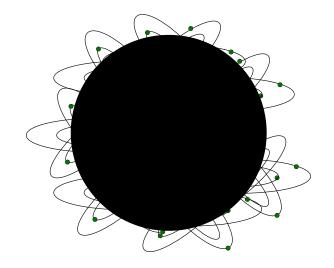
Set $G_{Newton} = 0$ and understand the microstate structure of material that will form a black hole at finite G_{Newton} ...

e.g. String theory: Strominger and Vafa: hep-th/9601029

Increase G_{Newton}, (or string coupling, g_s)

★ Matter/microstate structures shrink

$$\star$$
 Horizon areas grow: $R_S = \frac{2 G_{Newton} M}{c^2}$



The Horowitz-Polchinski Correspondence Principle

As G_{Newton} or g_s increases, whatever microstates you have found disappear behind a horizon: Microstates are Planck scale fuzz deep inside the black hole

The Many Faces of the Same Underlying Problem

Black holes

Uniqueness theorems ⇔ All matter swept from horizon region

Massive Matter: Consequences of Tolman-Oppenmeir-Volkov equation

Massive fields cannot produce a resolution at the horizon scale: No massive field is stiff enough to prevent collapse to black hole

- ★ Speed of sound > Speed of light
- ★ Buchdahl's Theorem: Central pressure/density infinite unless R_{matter} > 9/4 M

Weak/vanishing coupling resolutions

Will not survive at strong coupling:

Configurations of massive fields shrink as G_{Newton} (or g_s) increases

Massless fields

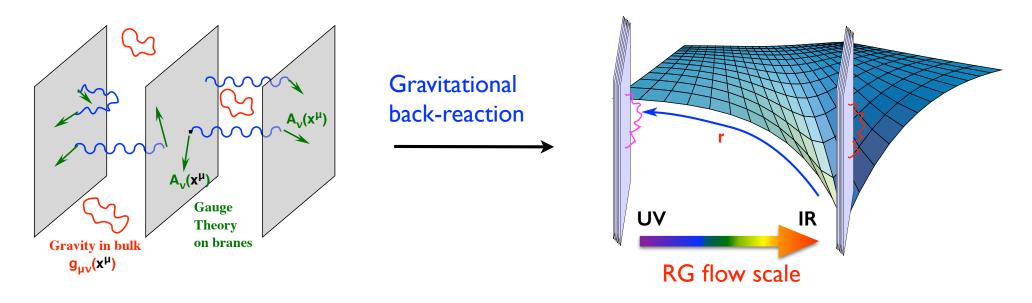
Appears hopeless: Massless fields travel at the speed of light

... only a "dark star" or black hole can hold such things into a star.

"No solitons without horizons"

Old Story IV: The Holographic Meta-Argument (~2000)

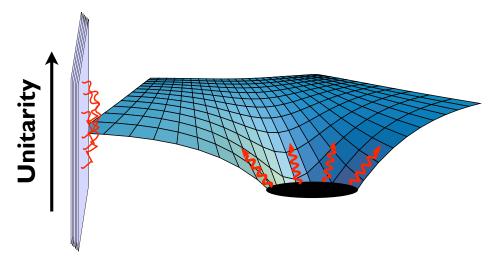
N=4 Yang-Mills on D3 branes is dual to String Theory in $AdS_5 \times S^5$



N=4 Yang-Mills is a unitary quantum field theory

⇒ Quantum gravity must be unitary within String Theory

In particular, string theory, via holography, must provide a unitary description of black-hole evaporation in asymptotically AdS spaces ..



Motivation for Microstate Geometries II

How does all this work in practice at strong coupling?

- What are the strong coupling phases of matter underlying stringy black-hole physics?
- How do you describe these phases holographically?
- What are the states underlying stringy black-hole physics?
- How do you see the microstates holographically?
- How does this relate to microstate descriptions at vanishing string coupling, for example, Strominger/Vafa?

What are the holographic duals of the Strominger-Vafa microstates?

· How do you count the microstates at strong coupling?

The study of Microstate Geometries is a systematic program that addresses these issues... at non-vanishing string coupling

The Microstate Geometry Program:

Find mechanisms and structures that resolve singularities and prevent the formation of horizons in Supergravity

Finite G_{Newton} (or g_s): Stringy resolution at/grow with horizon scale \Rightarrow Very long-range effects \Rightarrow Massless limit of string theory: Supergravity

<u>Microstate Geometry</u> = Smooth, horizonless solutions to the bosonic sector of <u>supergravity</u> with the same asymptotic structure as a given black hole/ring

How to evade: "No solitons without horizons theorems?"

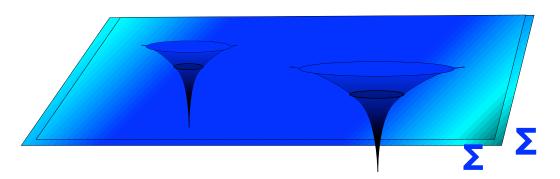
Solitons and Topology

Assume time-invariance: and there is a time-like Killing vector, K.

$$K^{\mu} \frac{\partial}{\partial x^{\mu}} = \frac{\partial}{\partial t}$$

Canonical energy-density

$$T_{00} \equiv K^{\mu}K^{\nu}T_{\mu\nu}$$



Unlike black-hole space-times, solitonic solutions are sectioned by smooth, space-like hypersurfaces, Σ .

Mass/energy is conserved and can be defined through a smooth integration over a regular surface: $M = \int_{\Sigma} T_{00} d\Sigma$

$$M = \int_{\Sigma} T_{00} d\Sigma$$

No solitons without horizons:

Equations of motion for massless field theory + Time-independent matter

$$ightarrow$$
 $\int_{\Sigma} T_{00} d\Sigma \sim \int_{\Sigma} d[F \wedge B]$ where $i_{K}(*F - F \wedge A) = dB$

In general: $T_{00} = \text{total derivative in } \Sigma \Rightarrow M \equiv 0$

 \Rightarrow If asymptotic to $\mathbb{R}^{D-1,1}$, then space-time must be globally flat, $\mathbb{R}^{D-1,1}$

The Error: This argument neglects topology

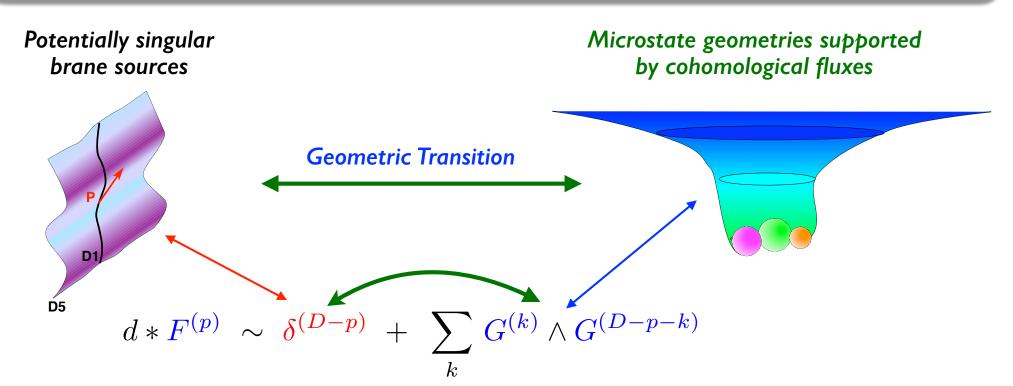
 T_{00} = total derivative in Σ only locally ...

Correct calculation \Rightarrow

Gibbons and NPW

$$M \sim \sum_p \int_{\Sigma} F^{(p)} \wedge H^{(D-p-1)}$$
 where $H^{(D-p-1)} \equiv harm(i_K(*_D F^{(p)} + \dots))$

Correct conclusion: No solitons without topology



A phase transition driven by the Chern-Simons interaction

Conclusions

- 1) Solitons CAN be supported by cohomological magnetic fluxes
- 2) This is the only way to support solitons/microstate geometries for asymptotically Minkowskian geometries

Correct mantra: "No solitons without topology"

Is this also true for space-times asymptotic to $\mathbb{R}^{d-1,1} \times (\mathbb{S}^1)^n$?

Geometric transitions to Microstate Geometries provide the only possible

Supergravity mechanism that can support horizon-scale structure!

What is the holographic interpretation of this result?

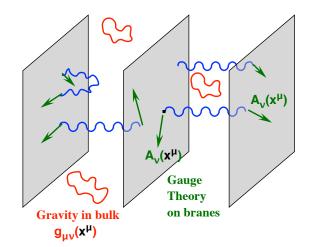
Some General Principles of Holographic Field Theory

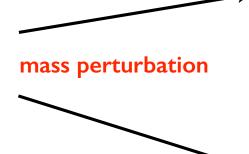
- ★ Radial behavior in gravity → RG flows in the holographic field theory
- ★ Normalizable fluxes in gravity → States in the holographic field theory
- ★ Core of the gravity solution → Deep Infra-red Limit of Field Theory

 - ❖ Scales of gravitational core structures → IR scales of field theory
 - Fluxes in the gravitational core structures
 Order parameters of the infra-red physics
- * Families of phase transitions represented by brane sources, as seen from infinity/UV, replaced by smooth cohomological fluxes in the IR
 - Many important examples
 Gopakumar-Vafa; Dijkgraaf-Vafa; Lin-Lunin-Maldacena; Klebanov-Strassler
 - ★ Physically meaningful IR limits for holography:
 - Smooth supergravity solutions
 - Singular sources that can be identified in terms of branes
 - Stringy excitations around supergravity/brane backgrounds

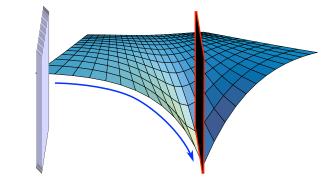
The holographic dual of a flow to a confining gauge theory

N = 2 or 4 Yang-Mills SCFT on D3 branes



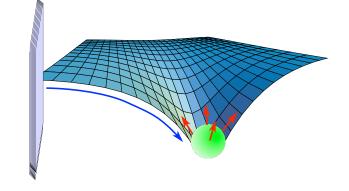


Klebanov-Tseytlin: Singular flow



N = 1 Confining Gauge Theory

Klebanov-Strassler: Smooth limit

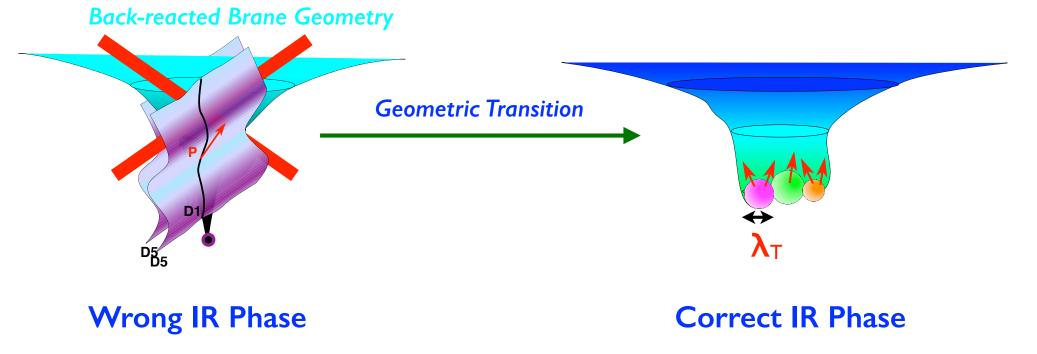


Correct holographic description

- ★ IR geometry: Branes undergo phase transition to "bubbled geometry"
- ★ Singular IR Geometry: wrong physics/ wrong IR phase of the gauge theory
- ★ Confining phase of field theory ⇔ Fluxed IR geometry:
 Fluxes dual to gaugino condensates = order parameter of confining phase
- * Scale of the bubble $\sim \lambda_{SQCD}$

Apply exactly the same holographic principles to black holes ...

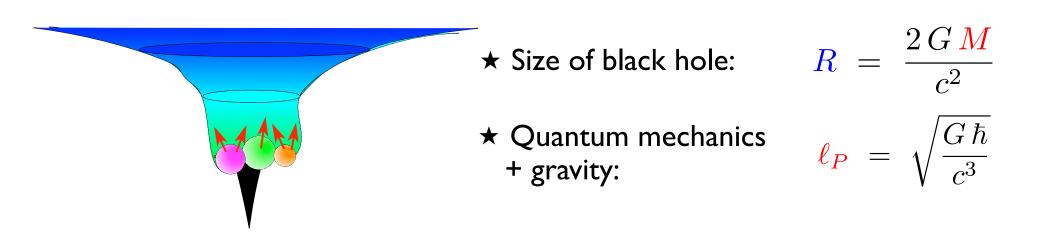
Microstate Geometries represent new phases of black-hole physics:



Features of the new phase

- \star Size, λ_T , of a typical cycle \leftrightarrow Scale of phase transition
- **★** Fluxes through cycles **↔** Order parameters of new phase
- * "Physical Depth" defined by $z_{max} = maximum redshift$ between infinity and the bubbles at the bottom that resolve the black hole

Traditional black-hole physics misses all the rich complexity of truly stringy black holes ... with new emergent phases of matter



Stringy Black Holes

New physics, new phases, new order parameters and two new scales (at least)

★ Scale of a typical cycle, λ_T ★ "Depth" of the "throat," Z_{max}

Traditional black holes: $\lambda_T = 0$, $z_{max} = \infty$

No solitons without topology ↔ Only these phases of stringy matter can give structure at the horizon scale

Two distinct and independent ideas from microstate geometries

- 1) A string theory *mechanism* to support structure at the horizon scale
 - The bubbled geometry provides a background to study other string phenomena, like fluctuations and brane wrapping
 - Holography: Such geometries describe a phases of the black-hole physics
- 2) Microstates: Fluctuations/Configurations in these phases
 - Supergravity fluctuations/moduli of microstate geometries

 = Coherent semi classical description of detailed microstate structure.
 - = Coherent semi-classical description of detailed microstate structure
 - Other structures in microstate geometries (like W-branes)
 description of other microstate structures (like Higgs branch states)
 - Holography: Understand the Microstates that are being captured

Note: Discussion so far is general ... not just BPS/supersymmetric

BPS Microstate Geometries

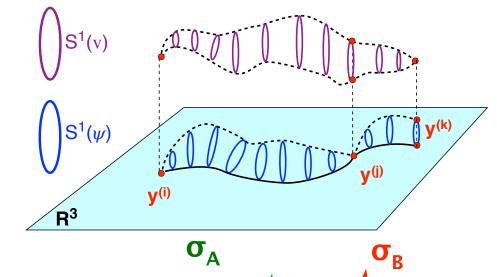
Phase structure and the supergravity mechanism

Building BPS Microstate Geometries

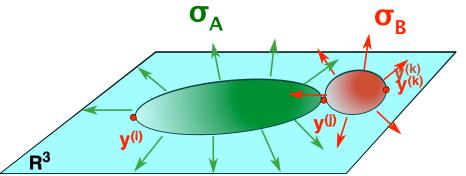
IIB Supergravity on T^4 : Supergravity in six-dimensions + BPS \Rightarrow Six dimensional metric ansatz: Gutowski, Martelli and Reall

$$ds_6^2 = -\frac{2}{\sqrt{\mathcal{P}}} \left(\frac{dv + \beta}{du + \omega - \frac{1}{2} Z_3 (dv + \beta)} \right) + \sqrt{\mathcal{P} V^{-1}} (d\psi + A)^2 + \sqrt{\mathcal{P} V} d\vec{y} \cdot d\vec{y}$$

u = null time; $(v, \overline{\psi})$ define a double S^1 fibration over a flat R^3 base with coordinates, y.



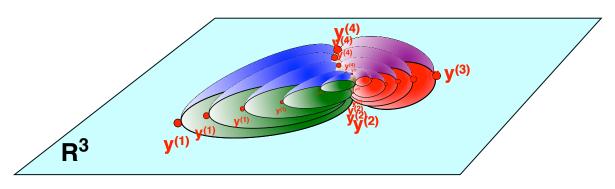
The non-trivial homology cycles are defined through the pinching off of the $S^1 \times S^1$ fibration at special points in the R^3 base.



Cycles support non-trivial cohomological fluxes ...

The scale of everything is set by the "warp factors:" V, P and Z_3

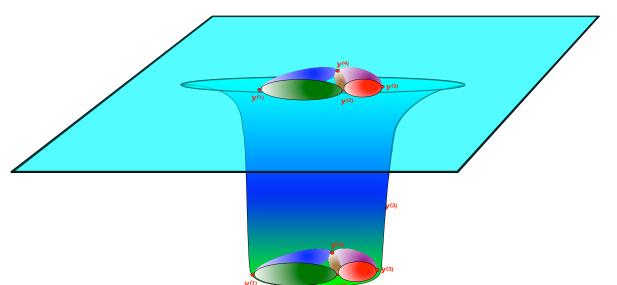
Scaling solutions



Fix charges and fluxes:

One can tune the orientation of the homology cycles so that the configuration remains *smooth* but *scales to an arbitrarily small size* in the R³ base ...

In the full six-dimensional geometry this scaling process:

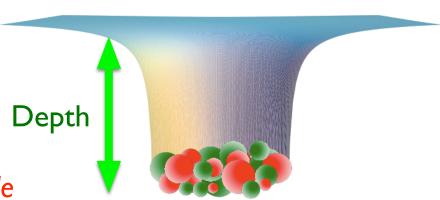


- ★ The bubbles descend and AdS throat
- ★ The bubbles retain their physical size
- ★ The diameter of the throat limits to a fixed size determined by the charges and angular momentum of the configuration

End result: Looks almost exactly like a BPS black hole to as close to the horizon as one likes ... but then it caps off in a smooth microstate geometry.

A Decade of BPS Microstate Geometries

- ★ There are vast families of smooth, horizonless BPS microstate geometries
- ★ New physics at the horizon scale
 - ⇒ The cap-off and the non-trivial topology, "bubbles," arise at the original horizon scale



★ Scaling microstate geometries with AdS throats that can be made arbitrarily long but cap off smoothly

Look exactly like a BPS black hole as close as one likes to the horizon Length/depth is classically free parameter

Long AdS throat: One can do holography in the AdS throat

- ⇒ BPS black-hole physics/microstate structure described by a CFT
- ★ Six-Dimensional Microsite Geometries → D1-D5 CFT Goal: construct precise map:

Bubbled geometry \leftrightarrow Phase of CFT

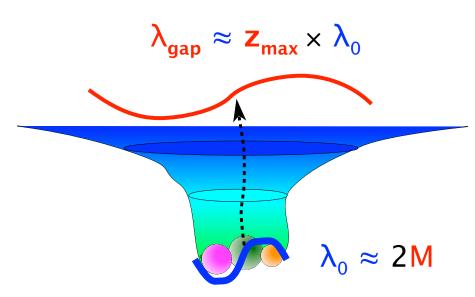
Geometric fluctuations ←→ Coherent combinations of microstates

The Energy Gap

 λ_{gap} = maximally redshifted wavelength, at infinity of lowest collective mode of bubbles at the bottom of the throat.

$$E_{gap} \sim (\lambda_{gap})^{-1}$$

Egap determines where microstate geometries begin to differ from black holes



BPS: Semi-classical quantization of the moduli of the geometry:

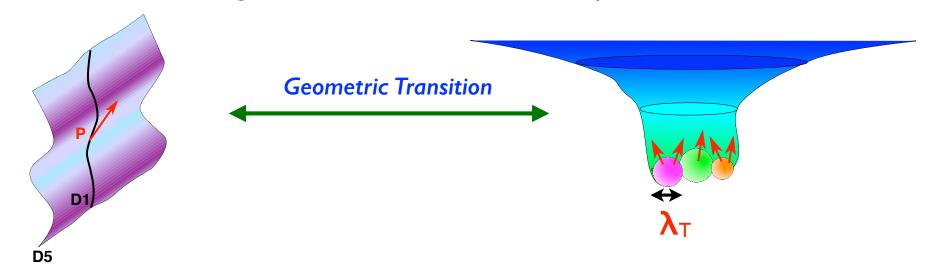
- \star The throat depth, or Z_{max} , is **not** a free parameter
- \star E_{gap} is determined by the flux structure of the geometry
- * E_{gap} Longest possible scaling throat: $E_{gap} \sim (C_{cft})^{-1}$

Bena, Wang and Warner, arXiv:hep-th/0608217 de Boer, El-Showk, Messamah, Van den Bleeken, arXiv:0807.4556

Exactly matches Egap for the stringy excitations underlying the original state counting of Strominger and Vafa

⇒ Scaling microstate geometries are phases/representatives of states in the "typical sector" that provides the dominant contribution to the entropy ...

Complete realization of geometric transition to new phases



Supergravity balance: Gravitational attraction in bubbles ←→ Flux expansion force

 \Rightarrow Transition Scale, λ_T ~ Magnitude of fluxes

Field theory: Scale of new phase ~ vevs of order parameters

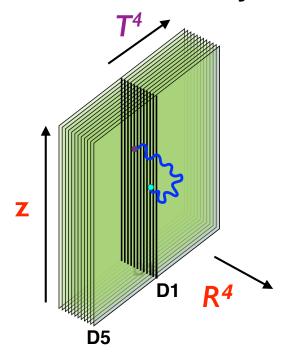
Classically: Freely choosable geometry and scale parameter. Can have $\lambda_T >> \ell_p$ Field theory: Phase structure and order-parameter vevs are freely choosable

Open issues:

- Are the phases selected by dynamics/phase space volume?
- What sets λ_T ? Is large λ_T be entropically favored?

BPS Microstate Geometries Semi-Classical Microstate structure

The D1-D5 System: ¹/₄ BPS = 8 supersymmetries



IIB Superstring on $T^4 \times S^1(z) \times R^{4,1}$

- * N_5 D5 branes wrap a $T^4 \times S^1(z)$
- ★ N₁ D1 branes wrap S¹(z)
- ★ (1+1)-dimensional CFT on S¹(z) from open strings stretched between D1's and D5's

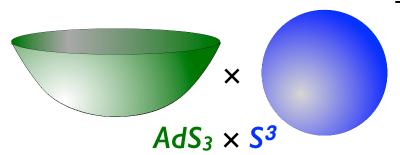
$$X_{(r)}^{\dot{A}A}(z,\bar{z}) \quad \psi_{(r)}^{\alpha\dot{A}}(z) \quad \widetilde{\psi}_{(r)}^{\dot{\alpha}\dot{A}}(\bar{z})$$

Chan-Paton labels: $r = 1,..., N = N_1 N_5$

*(4,4) supersymmetry and $c = 6N = 6 N_1 N_5$

Holographic Dual: IIB Supergravity on $T^4 \times S^1(z) \times R^{4,1}$

⇒ Supergravity in six-dimensions



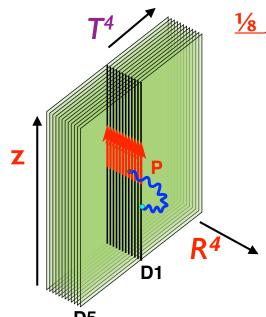
Geometric transition:

- ★ D1/D5 replaced by RR 3-form flux
- ★ Conformal vacuum: global AdS₃ × S³

Rich $\frac{1}{4}$ BPS ground state structure: The $\sim N_1 N_5$ RR ground states

1/4 BPS Holographic Dictionary: Lunin and Mathur; Kanitscheider, Skenderis and Taylor

The D1-D5-P System: ½ BPS = 4 supersymmetries



1/8 BPS States: Add Left-moving momentum

Right-movers: RR vacua (4 susies)

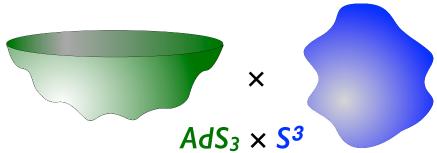
<u>Left-movers</u>: Any CFT excitation, $L_0 = N_P =$ momentum charge

Count states: Count partitions of N_P in a CFT with $c = 6 N_1 N_5$ \Rightarrow Black-hole entropy

$$S = 2\pi \sqrt{\frac{c}{6}L_0} = 2\pi \sqrt{N_1 N_5 N_P}$$

Strominger and Vafa: hep-th/9601029

Holographic Dual of the Strominger-Vafa (Index) States?



 $\frac{1}{8}$ BPS Shape modes on AdS₃ × S³

Goals:

- Construct fully-back-reacted fluctuating microstate geometries
- Holographic dictionary for these ½ BPS states
- Determine the stringy microstate structure visible within supergravity?

Status of BPS Microstate Geometries

BPS Microstate geometries define strongly interacting phases of the D1-D5 CFT

• Microstate geometries accessing correct phase and typical black-hole microstates with correct $E_{gap} \sim (C_{cft})^{-1}$

Where we are computationally with classical microstate geometries:

- Single Bubble/Two-centered geometries: Difficult but manageable
- Holographic dictionary for these ½ BPS states is now quite well-developed
- Constructing the holographic duals of the complete supergraviton gas on single bubble is within reach

Semi-classical geometries cannot see all string states, however:

- Arguments suggest that semi-classical structure can see enough black-hole microstates to obtain correct entropy growth $S\sim \sqrt{N_1\,N_5\,N_P}$
- Broader goal: Identify semi-classical moduli spaces whose quantization can describe all the microstates of the black hole

Where we need to go next

- Strominger-Vafa: Most of the black-hole entropy comes from the highly-twisted sectors of the underlying CFT
- Deep, scaling geometries access these highly-twisted sectors (Egap ~(N₁N₅)⁻¹)
 ★ Necessarily involve multi-center, multi-bubble solutions
- Most general fluctuating geometries (superstrata) only constructed for shallow, single-bubble/two-centered geometries
 - Understand the links and holographic dictionary between deep, scaling geometries and twisted sectors of CFT
 - ♦ Construct generic, multi-centered families of superstrata in scaling geometries ($E_{gap} \sim (N_1N_5)^{-1}$)
 - → Holographic duals of twisted sector states

New ideas:

- * W-Branes and the Higgs Branch
- * Quantum Tunneling and Microstate Geometries

Old Story V: Heterotic-Type II duality

Abelian Maxwell fields arise directly in compactification of perturbative type II strings/supergravity: $F_{(p)} = \sum_{J} F_{(2),space-time}^{J} \wedge \omega_{(p-2),internal}^{J}$

Where can one get the non-Abelian Maxwell fields, "W-bosons," of $E_8 \times E_8$?

Hull and Townsend: Brane-wrapping of homology cycles.

The harmonic forms, ω , are dual to (p-2)-cycles in the compactification manifold and wrapped branes carry vector-multiplets in supergravity ...

- Mass of vector multiplets ~ Volumes of dual (p-2)-cycles
- Interactions of vector multiplets ~ Intersection form of cycles

When the size of cycles in the shrink to the string scale then the vector bosons become massless \rightarrow massless W-bosons

For K_3 there is a point in the moduli space where 16 2-cycles shrink to zero size and where the intersection form of these cycles is given by the Dynkin diagram of $E_8 \times E_8 \rightarrow non$ -Abelian Maxwell fields, "W-bosons," of $E_8 \times E_8$

Vanishing cycles ⇒

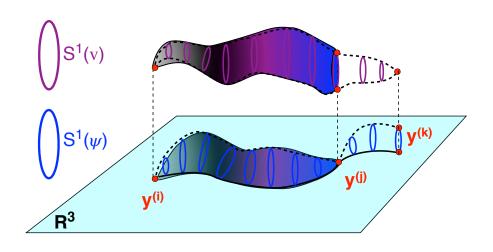
 $E_8 \times E_8$ heterotic string emerges as a new phase of type II strings

W-branes in Scaling Microstate Geometries

Martinec and Niehoff: arXiv:1509.00044

Topological Structure Microstate Geometry
New Field Theory Phases

New low-mass excitations in these phases



W-branes = branes wrapped around non-trivial cycles.

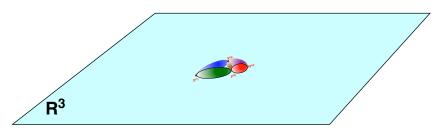
D-p brane wrap p-cycles can yield new BPS states of the system

These solitonic branes look like particles in remaining dimensions.

Duals of "Higgs Branch states"

Base geometry

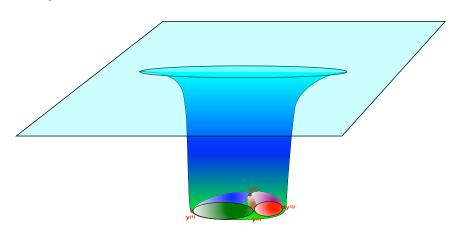
Cycles shrink to zero size



Which geometry governs the masses of these W-brane states?

Complete space-time geometry

Cycles retain finite size but descend AdS throat

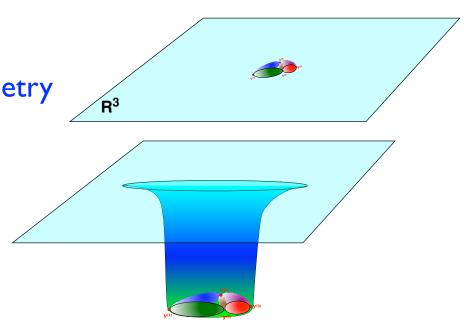


Massless W-branes

DBI action:

Mass of W-brane states ~ Scale in base geometry

- ~ Scale in full geometry
 - × (Red Shift from scaling BPS throat)
- ⇒ Deep scaling geometries have new classes of low mass/massless states



How many such states?

Naive count: One per cycle. A brane can wrap each non-trivial cycle

Actual count: Vastly larger number.

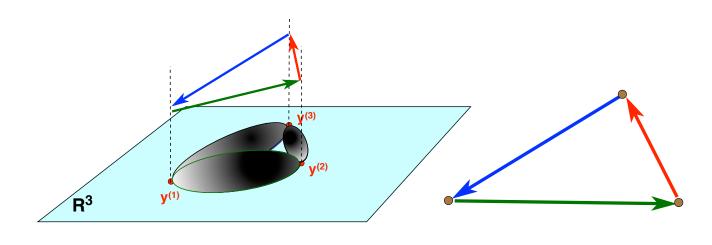
<u>Crucial insight:</u> Solitonic W-branes look like particles on the T^4 but this T^4 is threaded by magnetic fluxes and so each W-brane wrapping cycles in the space-time actually occupies <u>distinct Landau levels</u> on the T^4 .

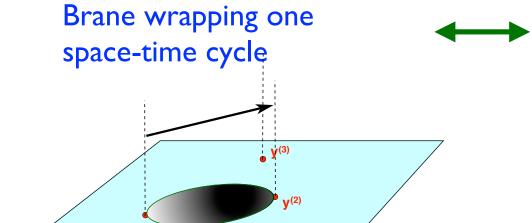
Martinec and Niehoff: arXiv:1509.00044

Three-node quiver

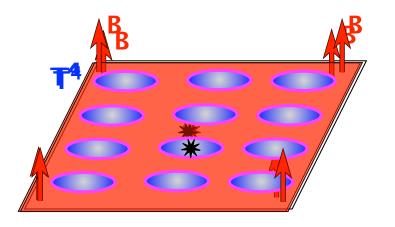
Naive count:

Three distinct W-branes





A point particle in the compactified directions



Internal space threaded by constant magnetic flux

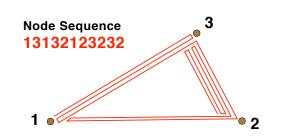
⇒ Each brane wrapping a space-time cycle

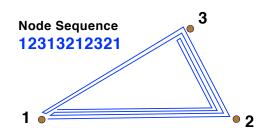


Many states labeled by internal Landau levels

Actual count: Brane wrappings are distinguished by Landau levels

W-branes ⇔ Walks on the three node quiver





Every distinct node sequence = Independent W-brane

Martinec and Niehoff: arXiv:1509.00044

Distinct W-branes

⇔ Higgs branch states of quiver quantum mechanics

This gives a semi-classical, solitonic description of the Higgs branch states

Count strings of sausages:

Number of such W-branes ⇔ Number of 3-derangements
3-derangements count Higgs Branch states in quiver quantum mechanics

Bena, Berkooz, de Boer, El-Showk, Van den Bleeken: arXiv:1205.5023

Number of W-branes $e^{\alpha Q^{3/2}}$

= The correct parametric entropy growth of the black hole

The Invisible Quantum Elephant of Black-Hole Physics

Curvature at horizon:
$$R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma}|_{horizon} = \frac{3}{16}\frac{G^2}{M^4}$$
 \Rightarrow Large black hole is classical at horizon scale

Fermi Golden Rule:
$$\mathcal{T}_{i \to f} = \frac{2\pi}{\hbar} <\psi_f |\mathcal{H}_{int}|\psi_i>|^2 \rho$$
 density of states

Number of states inside black hole

$$\sim e^{+16\pi M^2/m_P^2}$$

Number of states in the black hole in the middle of Milky Way:

It is the extreme density of states that makes an apparently classical black hole behave as a quantum object Mathur: 0805.3716; 0905.4483 Mathur and Turton: 1306.5488

Macroscopic tunneling probabilities $\sim O(1)$?

Iosif Bena, Daniel R. Mayerson, Andrea Puhm, Bert Vercnocke, arXiv:1512.05376

Final thought...

Maybe in spite of its macroscopic size, the near-horizon properties of black holes are dominated by quantum effects ... and this is what makes the O(1) changes to horizon-scale physics

So what good is all this classical supergravity analysis?

Obvious, boring answer:

Microstate Geometries are the semi-classical limit of these quantum effects: The gravitational expression of coherent sets of black-hole quantum states ...

Much more interesting "holographic" answer:

Supergravity identifies the long-range, large scale degrees of freedom that control physics at the horizon scale ...

- Supergravity controls the phase structure of the new black-hole physics
- Maybe we only have to perform the semi-classical quantization of all these relatively simple degrees of freedom to get a good picture of what is really happening at the horizon of a black hole ..

Supergravity is the emergent description of horizon-scale physics.

Conclusions

- Solving the information problem requires O(1) changes to the physics at the horizon scale
- Large scale resolutions must be based on microstate geometries with non-trivial topology and fluxes
- Microstate geometries define, holographically, new phases of black-hole physics
- Solving the information paradox via holography in supergravity requires the new black-hole phases described by microstate geometries
- New scales in black-hole physics: Transition scale, λ_T , and maximum red-shift, Z_{max} ; related to E_{gap} of fluctuation spectrum
- BPS solutions:
 - **★** Vast families of explicit examples
 - ★ Remarkably good laboratory for developing all these ideas
 - ★ Holographic dictionary for geometric fluctuations and CFT states is becoming well-developed
 - ★ Holographic duals of "Strominger-Vafa" states under construction
 - **\star** Semi-classical description of entropy with $S \sim \sqrt{N_1 \, N_5 \, N_P}$ is within reach
 - Lots of exciting new ideas: W-branes and Higgs branches; tunneling calculations; non-BPS; Investigations of infall ...